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Assured Reinforcement Learning for Safety-Critical Applications

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1 RESEARCH PROBLEM

Reinforcement learning (RL) is a branch of machine learning used to solve sequential decision making problems. This is achieved by using an autonomous agent to explore an initially unknown problem environment in order to learn a set of actions (known as an *optimal policy*) to perform in the environment's states that will return the maximum possible expected reward from the system (Wiering and Otterlo, 2012).

Despite RL having successes in areas such as robotics (Kober et al., 2013) and gaming (Szita, 2012) it has had little appeal in the domain of safety critical applications since RL has no guarantees that a learned solution will satisfy safety, legal or regulatory requirements. This limitation has prevented RL from being adopted in the domain of safety-critical applications such as in healthcare, business or legal systems, where behaviours by the agent can be dangerous to itself, other systems or humans. Furthermore, the agent may learn a set of behaviours that are unpredictable or unfamiliar to human operators, therefore making the system difficult to trust even if its operation may ultimately prove correct.

In recent years there has been growing interest in this limitation with research emerging with the aim to resolving it (García and Fernández, 2015). However, current approaches are still largely theoretical, suffer from scalability issues, have difficulty in expressing non-trivial safety properties, or are unable to offer firm guarantees that their RL solutions will satisfy specific requirements.

The root of the problem lies in how objectives are expressed in RL. Objectives are specified through a *reward function* that returns a numerical “reward” to the RL learning agent according to how beneficial an action it performs in a system state is to achieving its objectives. Those actions that will cause the agent to complete an objective will yield rewards that are greater than those actions that do not. The problem with this mechanism is that it can be infeasible to express complex requirements using rewards alone. Furthermore, it can necessitate introducing more de-

tails into the underlying RL environment, which will exacerbate the state-space explosion problem that affects RL (García and Fernández, 2015) and therefore will significantly reduce the rate of learning. When objectives conflict with each other, there is the additional issue of how to assign a reward function to simultaneously reward the agent and punish it. The nature of RL is to maximize a reward (or minimize a cost), so traditional RL is inherently unable find a solution that lies in the middle of these two extremes.

A further problem of this learning approach is that since the agent is motivated solely through accumulating as much reward as possible it can learn a solution that, despite being optimal with respect to maximizing reward acquisition, may not follow conventional human behaviours. Unfamiliar, “quirky” behaviours by the system further reduce its appeal in scenarios where it is crucial that the system can be trusted (Lange et al., 2012).

This project aims to address the problem of how to develop assurances that an RL system will a) find a solution that can guarantee to satisfy a wide range of safety requirements, and b) learn solutions can be trusted to conform to conventional behaviours of domain where the system is deployed.

2 OUTLINE OF OBJECTIVES

Research towards safe RL faces two common problems. Firstly, complex safety properties are often difficult to express using a reward function. Secondly, current safe RL approaches do not actually provide guarantees that the solution they generate will satisfy the safety requirements, and instead only offer a solution that is “safer” than the one learned by traditional RL.

The overarching aim of our project is to address these limitations by developing a generic approach for *assured reinforcement learning* (ARL) that achieves two key objectives:

1. ARL should support the specification and realisation of a broad range of complex requirements

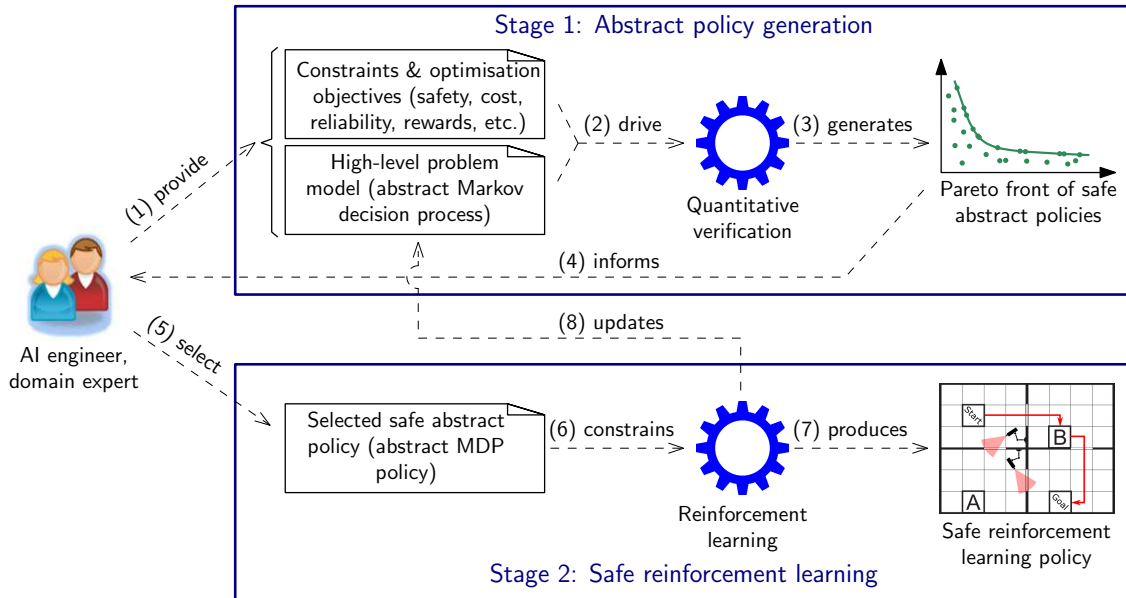


Figure 1: The envisaged approach for assured reinforcement learning.

(including constraints and optimisation objectives for the RL solution) without impacting the size of the underlying model.

2. ARL solutions should be *guaranteed* to satisfy requirements within pre-specified probability boundaries and execution costs.

The envisaged two-stage operation of our ARL approach is depicted in Figure 1. In Stage 1, termed *abstract policy generation*, we propose the use of an abstract Markov decision process (AMDP) (Marthi, 2007; Li et al., 2006; Sutton et al., 1999) to model a high-level representation of the RL problem. Also, a set of safety constraints and optimisation objectives are specified using probabilistic computation tree logic (PCTL) (Hansson and Jonsson, 1994), an expressive temporal logic that allows complex properties of Markov decision processes to be formulated as concise formulae. Devising the AMDP and the PCTL-encoded constraints and optimisation criteria for the RL problem requires both domain knowledge and AI expertise. Accordingly, teams comprising both an AI engineer and a domain expert provide (1) these inputs for the first ARL stage. The problem AMDP and constraints/optimisation criteria are then used to drive (2) the search for safe AMDP policies using *quantitative verification* (QV), a variant of model checking for the analysis and verification of stochastic models (Kwiatkowska et al., 2007). By exploring different areas of the AMDP parameter spaces, QV generates (3) a set of abstract policies for the AMDP, with the policies that are verified as satisfying all the constraints organised into a Pareto front.

This Pareto front captures the safe abstract policies that are Pareto optimal with respect to the optimisation criteria, and can therefore be used to inform (4) the users’ selection (5) of a suitable safe abstract policy.

In Stage 2 of ARL, termed *safe reinforcement learning*, the selected safe abstract policy is translated into a set of safety rules that constrains (6) the RL agent’s exploration to low-level states and actions that map to the high-level states and actions of the AMDP known to be safe. As a result, the RL agent produces (7) a safe reinforcement learning policy, i.e. an RL policy that when followed will have equal safety levels to those verified for the abstract policy, thus meeting the safety requirements.

The two-stage ARL approach described above makes two important assumptions: i) the AMDP model will contain all necessary information for abstract safe policies to fully apply to the low-level RL model, and ii) this information will accurately reflect the RL model. Should one or both of these assumptions not be satisfied, e.g. because the initial knowledge is incomplete or the parameters of the system change during runtime, then an abstract policy may not necessarily provide the levels of safety that it was verified to give. This necessitates a means of being able to detect inaccuracies in the AMDP model and to then find an alternate safe abstract policy for it. We therefore intend to extend the basic ARL approach to incorporate *knowledge revision* of the AMDP (Efthymiadis and Kudenko, 2015; Calinescu et al., 2011), with the RL agent identifying discrepan-

cies between the safe abstract policy and the explored environment and updating (8) the AMDP accordingly.

3 STATE OF THE ART

Research into safe RL is scant but has had growing interest in recent years. Existing approaches generally fall in to one of two categories (García and Fernández, 2015). The first looks into modifying how the accumulation of rewards is optimised. The second focuses on adjusting the strategies employed by the agent to explore the environment.

3.1 Preliminaries

RL uses a Markov decision process (MDP) as its underlying framework. Formally an MDP is a tuple (S, A, T, R) , where: S is a finite set of states; A is a finite set of actions; $T : S \times A \times S \rightarrow [0, 1]$ is a state transition function such that for any $s, s' \in S$ and any action $a \in A$ that is allowed in state s , $T(s, a, s')$ gives the probability of transitioning to state s' when performing action a in state s ; and $R : S \times A \times S \rightarrow \mathbb{R}$ is a reward function such that $R(s, a, s') = r$ is the reward received by the agent when action a performed in state s leads to state s' (Wiering and Otterlo, 2012).

Supplemental to this definition are *policies*, denoted π . A policy is a mapping of states of actions such that for each state $s \in S$ there is a corresponding action $a \in A$. The notion of solving an MDP is to find a policy that when followed will return the maximum possible expected reward from the MDP environment, such a policy is *optimal* and is denoted π^* . MDPs can be solved using dynamic or linear programming, however, when the transition and/or reward functions are initially unknown RL is used.

RL uses an autonomous agent to explore the environment to learn about its dynamics and whereabouts of rewards contained within it. This exploration is initially through the arbitrary selections of actions in states and over time the agent encounters rewards in the environment. Knowledge of these rewards is retained in the form of Q-values, a state-action pair $Q(s, a)$ that specifies the utility of performing action a in state s . In subsequent learning episodes the agent can then reuse this information by selecting the action in a state which has the highest utility value. These Q-values are updated each time the agent revisits the state according to an update function such as Q-learning (Watkins and Dayan, 1992). Given sufficient learning episodes the agent will converge to accurate (i.e. unchanging) utility values, when this eventuality is reached the agent has learned an optimal solution.

3.2 Optimisation Strategies

An intuitive approach for safe RL is to give a negative reward (i.e. a *cost*) to the agent if it performs actions which lead to the agent entering states which are denoted as unsafe. However, this simplistic approach suffers from several limitations. Firstly, it requires knowing a priori exactly which states of the RL environment are unsafe which may not be possible. Secondly, assigning a cost of suitable magnitude is not always obvious and requires trial and error to determine, especially if safety objectives conflicts with mission objectives. Finally, often it can be difficult to define complex safety requirements in the reward function and may necessitate significantly expanding the state space of the model to accommodate the properties.

Therefore, instead of focussing on how to define rewards for unsafe behaviours, various approaches have been proposed that consider the criterion for how the accumulation of rewards is optimised.

Ultimately we desire the agent to accumulate as much reward as possible for achieving mission objectives, but if the agent's behaviour means it enter states where it cannot achieve the objectives then it will not acquire these rewards. Even though *on average* the learned solution may receive the highest reward possible from the system, the variance of this reward indicates how risky the solution is. I.e., if the agent regularly receives a low reward for not achieving all mission objectives then the solution is not one that is particularly reliable. Therefore, redefining how the agent optimises its reward accumulation is one avenue of safe RL approaches.

One method is to optimise a policy so that no actions are irreversible, i.e. no actions can be done which the agent cannot recover from and are thus safe. Such an example is (Moldovan and Abbeel, 2012) where a set of ergodic policies are identified and the agent optimises over them. Whilst this approach guarantees that a solution will never lead to the agent being unsafe, the solution is often significantly far from being optimal. As significant rewards can be gained often at very low risk of danger, since this risk is not zero the rewards are not considered.

The *worst-case* criterion (Heger, 1994) optimises a solution so that the worst possible outcome when following it offers the maximum reward from the system relative to all other possible solutions' worst possible outcomes. This approach ensures that a solution will guarantee a minimum level of return will always be achieved, however, solutions typically yield drastically lower returns than an optimal solution would. Even though the probability of a worst-case scenario

occurring may be very low, this optimisation approach will disregard potentially large future rewards.

A similar approach is the *risk-sensitive* criterion (Mihatsch and Neuneier, 2002) uses a parameter to specify what amount of variability of return is permissible. This parameter can be tuned so that a solution is optimised to avoid variability or seek it. Through this approach a solution can be found that satisfies the level of risk that the user is comfortable with. However, as with the worst-case criterion, low variability can be produce solutions that are far from optimal.

3.3 Exploration Strategies

An alternative to modifying how the agent’s solutions are optimised is to modify how the agent actually explores the environment. Traditionally, an RL agent starts with no knowledge of the environment and must initially explore it randomly. This can lead to the agent finding solutions which traverse unsafe states. To ameliorate this problem, the exploration strategy of the agent can be influenced so that it has some knowledge of which states to transition to and which to avoid.

The *Lyapunov design* (Perkins and Barto, 2003) uses control Lyapunov functions to measure the distance from a safe system state to a failure (unsafe) state. By constricting the set of actions to only ones that cause the system to descend on a control Lyapunov function, i.e. towards a stable equilibrium, safe RL can be achieved. However, finding appropriate Lyapunov functions is often a difficult task and are bespoke for every problem scenario.

García and Fernández (García and Fernández, 2012) proposed *The Policy Improvement through Safe Reinforcement Learning* (PI-SRL) algorithm. This is a two-stage process where the first stage has a predefined safe baseline policy that is assumed to be sub-optimal and the next stage is to learn. The approach differs from policy iteration as it uses two new components, a risk function to determine the risk of a particular state and a baseline behaviour which can be used when in states of risk. However, in areas where there is no area of risk and only a discrete change from safe to unsafe states the algorithm can still result in failure.

Another approach is to use a series of *demonstrations* to aid the agent discover an initial solution (Argall et al., 2009) for the problem. This initial solution provide a basis for the agent so that it need not explore unnecessary or unsafe states. The solution derived from demonstrations will typically be sub-optimal so the agent uses it only as guidance and optimises it using traditional RL techniques. This approach is limited, though, by the fact that it is not always feasi-

ble to provide a safe demonstration for every possible scenario. In such an eventuality the agent must rely on conventional exploration techniques, falling back to the problem of the agent unknowingly exploring dangerous states.

4 METHODOLOGY

To achieve our project objectives we have decomposed the research work into the following tasks.

1. Review existing literature on safe RL to learn the current state of research and the limitations of existing approaches. Specifically, we aimed to identify limitations of existing RL solutions in order to determine the trajectory of our research.
2. Form a theoretical method as a potential solution for the identified limitations.
3. Implement the theoretical method as an actual application. This can be done in an interleaving fashion with task 2.
4. Evaluate the method using at least two qualitatively different case studies taken from benchmark RL experiments and real-world applications. Evaluation will focus on how well safety levels have been assured using our method compared to traditional RL.
5. Extend the approach to accommodate incorrect knowledge contained in the initial high-level problem model. Information that is different in the RL model can be relayed back to the high-level model and an updated solution is generated.
6. Further evaluate the full framework for scalability and generality by expanding existing case studies and develop new ones.

To implement the RL experiments we will be using the York Reinforcement Learning Library (YORLL)¹, which supports a wide range of environments and learning algorithms. To perform QV we will use the PRISM model checker (Kwiatkowska et al., 2011), which supports the verification of reward-extended PCTL properties for MDPs. QV and PRISM have been successfully used to analyse similar models of systems ranging from cloud infrastructure (Calinescu et al., 2012) and service-based systems (Calinescu et al., 2013) to unmanned vehicles (Gerasimou et al., 2014), and thus we expect them to also work well for ARL.

¹YORLL is programmed in Java and is developed by the University of York. It is free to download from <http://www.cs.york.ac.uk/rl/software.php>

The evaluation of approach will focus on how closely the learned RL policy adheres to the safety requirements, relative to a control experiment using traditional RL. Validating the policies can be done empirically by running the learned safe RL policy and comparing the outcome to the safety levels of the selected high-level policy. Given the stochastic nature typical of RL experiments it is necessary running the safe RL policy numerous times to obtain an average result (Arcuri and Briand, 2011).

5 EXPECTED OUTCOME

The expected outcome of our project is a general framework to provide an assured RL solution that will satisfy a broad range of safety requirements. Our novel approach will mitigate the existing limitation in safe RL research that safety cannot be guaranteed to fulfil specific safety requirements. By using QV to provably verify the properties of solution constraints our assured RL framework will guarantee to satisfy safety requirements.

We intend that the framework can be used across multiple domains and will support large-scale scenarios. The framework will require a set of requirements expressed using PCTL as well as a high-level model of the problem scenario. The end result will be a set of rules specifying which actions the agent should, or should not, perform in specific states of the RL model. The outcome being that the RL agent will learn a solution such that it will behave in a way that is guaranteed not to violate safety requirements whilst also being optimal subject to the constraints.

Our framework will contribute to the ongoing research into safe RL. Specifically, our approach will mitigate the recurring limitation that safety assurances can not be guaranteed, or when guarantees are given they are at an undesirably large detriment to optimality of the solution.

6 STAGE OF THE RESEARCH

So far, steps (1)–(7) of the approach shown in Figure 1 have been developed and evaluated. Preliminary work on these steps is summarised in (Mason et al., 2016), and the formalisation of this part of the approach and experimental results of its evaluation are presented in (Mason et al., 2017). Our current work is towards developing the knowledge-revision algorithm for updating the AMDP as discussed in Section 2 and shown by step (8) from Figure 1.

6.1 Completed Work

For our high-level model we use an AMDP, which is an abstract version of the low-level RL MDP. AMDPs differ to conventional MDPs by being significantly smaller in terms of their state space and action set (Marthi, 2007). To achieve this, superfluous states of the MDP are ignored and similar states conflated, only those states with significant features, such as those containing rewards, are retained (Li et al., 2006). The low-level action set can be abstracted so that instead of requiring a series of individual actions to enter the next state of interest, high-level *options* are used instead (Sutton et al., 1999). These options replace the actions with single transitions between states. The end AMDP has several orders of magnitude fewer states than the RL MDP, and therefore can be formally analysed using QV. This allows the rapid verification of candidate high-level policies against the PCTL-encoded problem requirements.

An algorithm has been developed to automate the process of generating and verifying abstract policies and assembling a Pareto-front of those policies that were verified as being safe; this algorithm is presented in (Mason et al., 2017). To generate candidate abstract policies, the algorithm can utilize a range of search techniques, including as hill climbing, genetic algorithms, e.g. (Gerasimou et al., 2015), or a simple random search. As different search techniques can perform better than others for certain types of problem scenarios, experiments are planned to identify suitable techniques for different classes of RL problems (e.g., planning and navigation).

We have evaluated the method in two qualitatively different case studies. The first case study is based on the benchmark RL flag-collection experiment (Dear den et al., 1998) which we have extended by introducing the risk of the agent being captured. Details of this case study are given below. The second case study is based on an assisted living system for dementia patients (Boger et al., 2006). In this experiment an autonomous agent must give voice prompts to a dementia sufferer to instruct them on what task to do next when undertaking the activity of washing their hands. The system learns what style of voice prompt is most appealing to the patient, considering the volume of the prompt, the gender of the voice and the explicitness of the instructions. This system must not overload the patient with prompts as this can become stressful for them; conversely the agent must minimize the necessity of summoning a carer to intervene should the patient not progress effectively.

The environment for the guarded flag-collection case study is shown in Figure 2; the objective in this

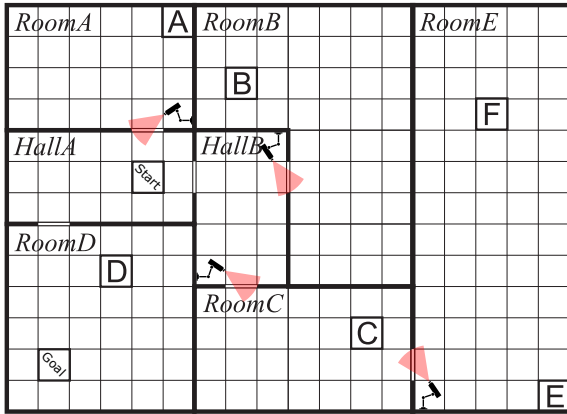


Figure 2: The layout of the guarded flag collection environment. The areas of risk are illustrated by security cameras which with a certain probability can detect the agent as it traverses the doorways.

benchmark RL experiment is to learn a route through the environment to collect the flags A-F. In our case study we have augmented the environment with security cameras which can detect the agent as it passes through certain doorways. Detection of the agent results in its capture and the experiment ending in failure, regardless of any flags already collected.

Each of the cameras has a different probability of detecting the agent. Therefore, along with the original optimisation objective to maximize the number of flags collected we also have the conflicting safety objective of minimizing the probability that the agent is captured. For our case study we specify the following constraints:

- C_1 The agent should reach the ‘goal’ area with probability at least 0.75.
- C_2 The agent should cumulate more than two flags before it reaches the ‘goal’ area.

Furthermore, we aim to maximise:

- O_1 The probability that the agent reaches the ‘goal’.
- O_2 The number of collected flags.

After constructing an AMDP for the problem we used QV to identify a set of abstract policies that satisfy the constraints C_1 and C_2 . From these safe policies we identified a *Pareto front*, i.e. a “front” of policies whose expected reward and probability of reaching ‘goal’ cannot be both bettered by any other safe policy. These safe policies and their associated Pareto front are shown in Figure 3.

From this Pareto front three policies were selected to be used for safe ARL; these are labelled A, B and C on the Pareto front. These safe policies were translated into safe RL rules for ARL. The results of the evaluation of the learned ARL policies are presented

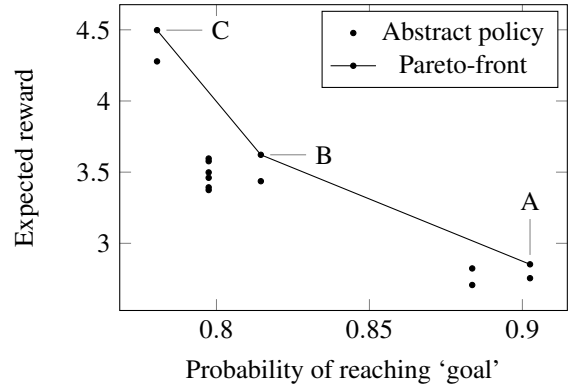


Figure 3: Plot of abstract policies that satisfy the safety constraints C_1 and C_2 , and the Pareto front of safe policies A, B and C.

in Table 1 alongside a baseline experiment using traditional RL, which we carried out in order to establish the effects of ARL.

In both case studies our approach was successful at satisfying the safety requirements (Mason et al., 2017). Furthermore, the learned policy matched the specific safety results that were verified for the high-level safe policy. From these results we show that our approach can achieve the levels of safety that were required.

6.2 Ongoing Work

Currently, research is progressing with development on a knowledge-revision algorithm as discussed in Section 2. An algorithm is being formulated where an RL agent first attempts ARL using what is presumed to be a suitable abstract policy. Should the agent discover that the policy is not viable (e.g. the abstract policy dictates the RL agent should perform an action in a state where the action is not available), then knowledge of the error is fed back to the AMDP and a revised model is constructed.

Work is currently focussing on a means of recy-

Table 1: The results for safe abstract policies A, B and C when used for ARL along with a baseline, traditional RL experiment for the guarded flag-collection.

Abstract Policy	Probability of Reaching ‘goal’	Standard Error	Expected Reward	Standard Error
None	0.72	0.0073	4.01	0.031
A	0.9	0.0012	2.85	0.0029
B	0.81	0.0019	3.62	0.0037
C	0.78	0.0012	4.5	0.0041

cling redundant abstract policies where possible, thus significantly reducing the verification effort required to update the Pareto front of safe abstract policies. Since it is often the case that there are only minor differences between the initial, incorrect AMDP model and the corrected model, we envisage that the abstract policies for the two models will be similar. Therefore, it is intuitively not necessary to generate an entirely different abstract policy. Since it is time consuming to generate policies as well as to verify them, we aim to reuse those elements of the initial abstract policy that still match the abstract model.

To evaluate the algorithm, a series of experiments will be conducted using extension of the two case studies described in the previous section. For each case study we will produce a series of RL environments where the environment is uniquely different from that of the initial AMDP. We will then determine if on average the knowledge revision algorithm is faster at finding a new safe abstract policy than if an AI engineer were to manually inspect the initial RL model, reconstruct the high-level model, and generate safe abstract policies from scratch.

6.3 Future Work

Future work will involve more in depth analysis of the framework's performance. This includes evaluation of how long it takes for a safe solution to be learned and the processing overheads incurred. Additionally, further experiments will be conducted by expanding the existing case studies to establish how well the framework will scale, also, new case studies will be developed for different domains to determine the range of scenarios which the technique can be applied to.

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