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1 Understanding the ash deposition formation in Zhundong
2 lignite combustion through dynamic CFD modelling analysis

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10 **Abstract:**

11 A dynamic CFD model, which is based on the inertia impaction, the thermophoresis and the direct
12 alkali vapour condensation incorporating the influence of the heat transfer to the tube, has been developed
13 for predicting the ash deposition formation in Zhundong lignite combustion in a pilot-scale furnace. The
14 results show that particle deposition from the inertia impaction and the thermophoresis dictates the ash
15 deposition formation under high furnace temperatures. The deposition caused by the direct alkali vapour
16 condensation is less significant. As deposition time increases, particle impaction efficiency decreases and
17 sticking efficiency increases due to the thermophoresis and the local temperature conditions, which result
18 in the time-dependent behaviour of the deposition growth. In addition, the ash deposition characteristics
19 are influenced under different furnace temperatures, due to the change in the particle impaction and
20 sticking behaviours. Qualitative agreement is obtained between the predicted results and the measurements
21 for the heat flux to the tube and the ash deposition growth.

22 **Keywords:** CFD, ash deposition, Zhundong lignite, deposition mechanisms, particle behaviours.

23 **1 Introduction**

24 Zhundong (ZD) lignite, with a huge forecast reserve of 390 billion tons, could provide China with
25 coal consumption for many decades [1-3]. However, due to the ZD lignite having a high content of Alkali
26 and Alkaline Earth Metal (AAEM) elements [1-3], severe problems of ash slagging, fouling and corrosion
27 are induced in the radiation and convection sections of the boilers [3, 4]. This can raise significant practical
28 issues, such as reducing the efficiency and lifetime of boilers. In recent years, many efforts have been paid
29 to experimentally study the ash deposition behaviour of Zhundong lignite combustion in lab-scale [1,
30 2]/pilot-scale test facilities [5-8] as well as for full scale boilers [3, 4]. The main reasons for the ash
31 deposition problems of ZD lignite are concluded as: (i) high amount of basic components in the ZD lignite
32 can increase the melting potential in the radiation and convection sections which cause the slagging
33 formation [2, 5, 7, 8], and (ii) both the thermophoretic deposition of small particles and the condensation
34 induced by the sodium related alkali vapours are responsible for the severe fouling phenomenon in the
35 convection section of the boilers [1, 3, 8]. Although the main reasons that caused the severe ash deposition
36 characteristics have been investigated widely, the deep understanding and prediction of the particle
37 impaction and sticking behaviour, and the importance of the individual ash deposition mechanism on the
38 ash deposition formation/growth is still insufficient.

39 CFD methods have been widely used for understanding and predicting ash deposition behaviours in
40 combustors with different scales (lab-scale, pilot scale, and full-scale boilers) using either the ‘steady state’
41 assumptions or the dynamic simulations. Up to date, most of the publications employ the ‘steady state’
42 assumptions of the deposition rates to develop the sub-models in CFD methods (for better describing the
43 ash deposition behaviours [9-15], for new fuels [16-20], for the oxy-combustion condition [21], etc.). This
44 kind of assumption is suitable for the ash deposit growth on the uncooled deposition tube where the
45 deposition surface temperature is close to the furnace temperature, which results in the stable particle
46 impaction and sticking behaviours. In addition, the inertial impaction may be the main ash deposition
47 mechanism under this condition [18]. However, for a real heat exchanger tube (which is cooled in boilers),
48 the deposition surface temperature could increase with the growth of the deposit on the tube. This affects
49 the particle impaction and sticking behaviours and the contribution of the major deposition mechanisms
50 (inertia impaction, the thermophoretic force and the condensation) on the overall ash deposition growth.
51 Therefore, only a dynamic consideration of the ash deposition growth is suitable for a cooled tube, rather

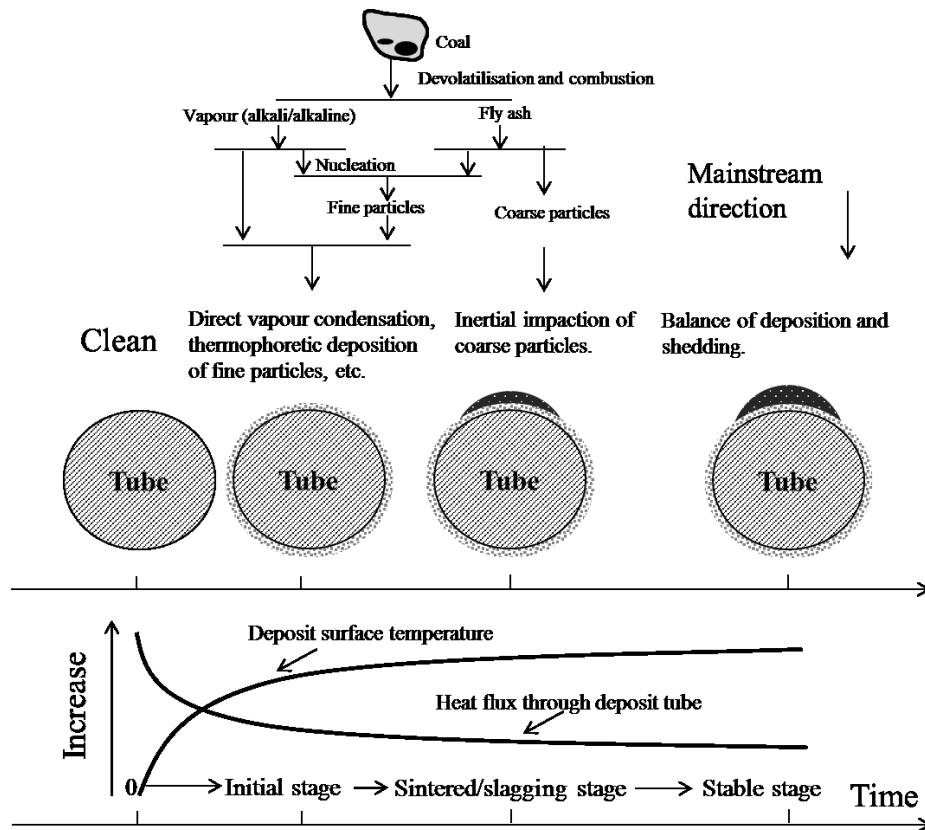
52 than a ‘steady state’ assumption. Recently, only a limited number of studies have investigated the ash
53 deposition growth through a dynamic CFD simulation. Kaer et al. [36] developed a dynamic CFD model to
54 predict the ash deposition formation and heat transfer rates and the paper focused on straw combustion and
55 investigated the ash deposition rate caused by different deposition mechanisms. Wang et al. [22], Li et al.
56 [23-25], and Balakrishnan et al. [26] developed CFD models to predict the ash deposition growth and heat
57 transfer rate for boilers. Their models mainly considered the slag layer growth where the inertial impaction
58 mechanisms are the main contribution. Waclawiak et al. [27, 28] modelled the ash deposit growth in the
59 convection section based on the inertial impaction mechanism. García Pérez et al. [29] modelled the
60 deposit growth of fume particles based on the thermophoretic force, Brownian motion and inertial
61 impaction. In both the Waclawiak and García Pérez’s model, they focused on predicting the deposit shape
62 and weight. The energy conservation principles were neglected in their models, which cannot consider the
63 influence of the increase of the deposition surface temperature on the deposition behaviour. In addition, the
64 details of particle impaction and sticking behaviours during the deposition growth process are still not clear
65 from these previous publications [22-25, 27-31].

66 Therefore, this paper aims to develop a dynamic CFD model to predict the ash deposit growth process
67 for ZD lignite combustion in a pilot-scale furnace. Understanding the initial ash deposition behaviour on
68 cooled tubes is significant to predict the deposition propensity. Therefore, we focus on predicting the
69 influence of the main ash deposition mechanisms, namely the inertial impaction, the thermophoretic force
70 and the direct vapour condensation, on the deposit rate and understanding of how the deposit growth will
71 influence the heat transfer rate through the deposit to the cooled deposition probe. In addition to the effect
72 of furnace temperatures on the deposit growth, the particle impaction and sticking behaviours with the
73 deposit growth are studied in-depth and the importance of the main ash deposition mechanisms on
74 controlling the deposit growth is investigated. The model developed has been tested using the experimental
75 data (including the deposit growth rate and the heat flux) from the Zhejiang University’s pilot-scale
76 furnace [5].

77 **2 Source of experimental data**

78 Ash deposition experiments were conducted in a 300 KW pulverized fuel combustion furnace located
79 at Zhejiang University, with an inner diameter of 0.35 m and a length of about 3.95 m. The swirl burner

80 consists of a primary inlet through which the pulverized coal and the primary air are fed, and a secondary
 81 inlet for the heated air to maintain a stable flame [5]. The cooled ash deposition probe, made of stainless
 82 steel, is placed in the central region of furnace, which has furnace temperatures of approximately from
 83 1373 K to 1593 K, respectively. The probes are cooled by heat conducting oil with a temperature 503 K. In
 84 the meantime, the deposit growth is monitored online by an image sampling system. More details of the
 85 furnace and the deposition sampling system can be found in [5].



86 **Figure 1.** Schematic diagram of the main formation of the ash deposits on a cooled heat exchanger tube.

87 Figure 1 shows a schematic diagram of ash deposition typically formed on a cooled heat exchanger
 88 tube. Ash deposits are mainly generated by fly ash particles and the alkali/alkaline vapour after coal
 89 combustion [32]. Due to the low tube surface temperature, the deposition due to the thermophoretic force
 90 and the vapour condensation may play an important role in the ash deposit formation in the initial stage of
 91 the ash deposition formation [33-35]. The deposition surface temperature could rapidly increase due to the
 92 deposit growth and due to the rapid decrease in the heat flux to the deposition tube in the initial stage [18].
 93 With the increase in the deposition surface temperature, the melting potential of the deposition surface is
 94 enhanced, which causes the sintering and slagging formation, the vapour condensation disappears and the
 95 contribution of the thermophoretic deposition on the arrival rate of ash particles declines [36]. At this stage,

96 the deposition caused by the inertial impaction of coarse particles is the main deposition mechanism. Due
 97 to the higher thermal conductivity and lower heat flux through the tube than those in the initial stage, the
 98 deposition surface temperature increases slowly and this results in the slow decrease in the heat flux
 99 through the deposition tube [18]. With the deposit growth, the shedding of the deposit is enhanced by the
 100 erosion, liquid flow at the deposit surface, gravity shedding, etc. [37]. When the shedding rate is similar to
 101 the deposition rate, the deposit growth could stop or fluctuated and then the deposit height becomes stable
 102 [38]. From the deposition test of Zhundong lignite in Zhejiang University [5], obvious shedding appears
 103 after almost two hours of deposition time. The prediction of the ash deposition behaviour is focused on the
 104 first two hours in this study, where the shedding is less important. A robust shedding model is required to
 105 capture the physics of shedding, which is considered to be a future work.

Table 1. Fuel properties of the ZD lignite [5].

<i>Ash composition (wt.%)</i>		<i>Proximate analysis (wt.%)</i>	
SiO ₂	35.08	Volatiles (<i>db</i>)	32.79
Al ₂ O ₃	14.04	Fixed carbon (<i>db</i>)	52.91
Fe ₂ O ₃	6.07	Ash (<i>db</i>)	12.3
CaO	27.78	HHV(MJ/kg)	54.01
MgO	4.73	<i>Ultimate analysis (wt.%) (db)</i>	
K ₂ O	0.48	C	64.07
Na ₂ O	8.31	H	3.58
TiO ₂	0.71	O	19.22
SO ₂	2.8	N	0.65

Table 2. Mineral compositions of low temperature ash by XRD (*wt%*) [5].

Quartz (SiO ₂)	Calcite (CaCO ₃)	Halite (NaCl)	Hematite (Fe ₂ O ₃)	Anhydrite (CaSO ₄)
28.0	27.6	24.7	13.4	6.2

106 Table 1 shows the properties of the ZD lignite, including the proximate and ultimate analysis, as well
 107 as the major ash composition of the ZD lignite [5]. Table 2 shows the mineral compositions of the low
 108 temperature ZD lignite ash [5]. As expected, the ZD lignite has a high volatile content and low-medium
 109 ash yield. The ash analysis is dominated by silicon (Si), calcium (Ca), sodium (Na), aluminium (Al), iron
 110 (Fe) and magnesium (Mg) oxides, accounting for almost 96% of the total ash. In particular, the low

111 temperature ash is rich in sodium (Halite) and calcium (Calcite and Anhydrite). Additionally, quartz and
 112 hematite are present in the ash sample. The ZD lignite rich in AAEM has shown a high tendency to cause
 113 ash slagging, fouling and corrosion in the radiation and convection sections of the boilers [1-3].

114 **3 Mathematical models**

115 In order to describe the dynamic deposition growth of the ZD lignite, efforts have been made on
 116 producing an accurate numerical description of the ash deposition mechanisms in controlling the deposit
 117 growth and its interactions with the thermal boundary at the deposit surface. To achieve this, several
 118 submodels have been developed and applied in the CFD framework. In this section, the momentum
 119 equation to solve the particle trajectories is introduced, followed by a description on the submodels for the
 120 thermophoresis and the sticking model of the particles and the deposition surface, as well as the direct
 121 alkali vapour condensation and the deposit properties. The solving strategy of the deposition growth model
 122 with the CFD framework is discussed at the end of this section.

123 *3.1 Particle trajectories*

124 The arrival rate of the ash particles on the deposition surface is dictated by the particle trajectories. The
 125 particle trajectories are solved in a combined Eulerian-Lagrangian frame of reference where the gas phase
 126 is modelled in the Eulerian frame of reference and the ash particles are tracked in a Lagrangian frame of
 127 reference [39]. The velocity of the particles are governed by the particle momentum equation, which is a
 128 balance of the drag, gravity, and other forces as formulated in the following equation [39]:

$$\frac{d\vec{v}_p}{dt} = \frac{18\mu_g C_D Re_p}{\rho_p d_p^2} (\vec{v}_g - \vec{v}_p) + \frac{\vec{g}(\rho_p - \rho_g)}{\rho_p} + \vec{F} \quad (1)$$

129 where \vec{v} , ρ , μ and d are the velocity, density, viscosity and diameter of the particles, respectively; the
 130 subscripts p and g refer to the particle and gas, respectively, C_D is the drag coefficient, and \vec{F} is the other
 131 forces, such as the thermophoretic force, the virtual mass force, the pressure gradient force, the Saffman's
 132 lift force, etc.

133 In this paper, both the gravitational force and the thermophoretic force are considered. The
 134 thermophoretic force, which is caused by the temperature gradient in the gas stream close to a cold
 135 deposition surface, needs to be considered when modelling the ash deposition on a cooled surface. In this
 136 paper, the thermophoretic force, \vec{F}_{th} , is considered by the correlations employed by Tablot et al. [39, 40]:

$$\vec{F}_{th} = -\phi \frac{d_p \mu_g^2}{2\rho_g T_g m_p} \nabla T \quad (2)$$

$$\phi = \frac{12\pi C_s (k/k_p + C_t Kn)}{(1 + 3C_m Kn)(1 + 2k/k_p + 2C_t Kn)} \quad (3)$$

137 where ϕ is the thermophoretic coefficient, T_g is the gas temperature, m_p is the particle mass, ∇T is the
 138 temperature gradient in the gas phase, $C_s = 1.17$, $C_t = 2.18$, $C_m = 1.14$, k is the fluid thermal
 139 conductivity, k_p is the particle thermal conductivity, and Kn is the Knudsen number. The virtual mass and
 140 pressure gradient forces, which are due to the acceleration of the fluid around the particle and the pressure
 141 gradient in the fluid, can be ignored when the density of the particle is much greater than the density of the
 142 fluid.

143 The accuracy of predicting the arrival rate of the particles is determined not only by an accurate
 144 mathematical description of the physical mechanism, but also by an accurate numerical method. Previous
 145 studies have shown that an improper grid around the deposition surface can lead to an inaccurate
 146 prediction of the particle arrival rate due to the inaccurate resolving of the flow-field within the boundary
 147 layer near the deposition surface [15, 18, 41, 42]. The accurate resolving of the flow boundary layer
 148 requires an extremely fine computational mesh close to the deposition surface. A revised particle
 149 impaction model has been developed from our previous studies [18]. It can be employed to better predict
 150 the arrival rate of the particles by resolving the particle impaction efficiency for both the drop tube
 151 furnaces and utility boilers without excessive meshing [18].

152 The energy balance equation for the particles, which are solved along the trajectories of the particles in
 153 order to obtain the corresponding particle temperatures, is given as follows [39, 43]:

$$m_p c_p \frac{dT_p}{dt} = h A_p (T_\infty - T_p) + \varepsilon_p A_p \sigma (\theta_R^4 - T_p^4) \quad (4)$$

154 where m_p , c_p , T_p , A_p , and ε_p are the mass, specific heat, temperature, surface area and emissivity of the
 155 particles, T_∞ is the gas temperature, σ is the Stefan–Boltzmann constant, and θ_R is the radiation
 156 temperature.

157 *3.2 Sticking efficiency*

158 In addition to the particle impaction caused by the inertia impaction and the thermophoretic force, the
 159 stickiness of the ash particles is critical to determine the fate of the particles, whether they stick on the

160 surface or rebounds from the surface [11, 30, 44]. Typically, the models to predict the sticking efficiency
 161 are based on such as the ash viscosity, the kinetic energy and the degree of molten of fly ash particles. The
 162 viscosity based sticking model is strongly dictated by the value of a reference viscosity. However, this
 163 value ranges within $8\text{-}10^8$ Pa.s and this may contribute to an inaccurate stickiness prediction [19, 45]. The
 164 kinetic energy thresholding sticking model requires a fitting process to develop the effective Young's
 165 modulus versus the particle temperature and the particle diameter by matching the experimental data with
 166 the simulation results [13]. In addition, the ZD lignite ash has a high content of sodium and calcium,
 167 which increases the difficulty to predict the ash viscosity and the effective Young's modulus from the
 168 present modelling methodology. Further, the molten fraction-based sticking model has been developed
 169 using slag calculations based on the chemical equilibrium of the ash composition and it was found that
 170 deposition models based on the molten fraction of ash particles calculated from chemical equilibrium are
 171 promising [45]. In addition, this model is widely used for predicting the sticking efficiency of biomass ash
 172 which also contains high concentration of the alkali species [30]. Therefore, the molten fraction-based
 173 sticking model is employed to determine the sticking efficiency, η_{stick} , and it can be determined by the
 174 melt fraction of the particles and the melt fraction of the deposit on the probe surface [14, 30]:

$$\eta_{stick} = \eta_p(T_p) + (1 - \eta_p(T_p))\eta_s(T_s) \quad (5)$$

175 where $\eta_p(T_p)$ is the melt fraction of the particles at the particle temperature (T_p), and $\eta_s(T_s)$ is the melt
 176 fraction of the deposit on the probe at the deposition surface temperature (T_s). The melt fraction is
 177 determined by the thermodynamic equilibrium calculations based on the minimization of the Gibbs free
 178 energy from the system subject to the mass balance constraints [46, 47]. In this paper, the thermodynamic
 179 software package FactSage 7.0 is employed to perform the thermodynamic equilibrium calculations.

180 The calculations were performed for a temperature range between 500 K and 1750 K at a temperature
 181 interval of 20 K and at atmospheric pressure. The ash composition determined by the mineral quantity
 182 analysis of the low temperature ash and the air composition were used as the reactants. Their amounts are
 183 dictated by the inlet air/fuel ratio. It should be noticed that, in order to calculate the melt fraction of the
 184 deposit, its ash composition may be different from that of the ash particles due to the direct condensation
 185 of the alkali phases. Therefore, the local ash composition of the deposit is determined by the deposit mass
 186 of the particle deposition and the direct alkali vapour condensation calculated from the CFD results. The
 187 possible products selected are the entire compound species (ideal gases and pure solids) from the ELEM,

188 FToxid, FTsalt and FACTPS databases. The melt phases chosen in the calculations were the ‘SLAGB’
 189 (covers liquid oxide solutions of SiO₂, Fe₂O₃, Fe₂(SO₄)₃ and, Na₂O, Na₂SO₄, CaO, and CaSO₄) and
 190 ‘SALTB’ (covers liquid salt solutions of NaCl, NaOH, CaCl₂, Ca(OH)₂, FeCl₃, Fe(OH)₃, etc.) with
 191 possible 2-phase immiscibility.

192 3.3 Deposit growth and update of deposit properties

193 In this paper, the deposition rate is calculated by the deposition caused by the inertia impaction, the
 194 thermophoretic force and the direct alkali vapour condensation. Therefore, the deposition rate is the
 195 summation of the deposition of these deposition mechanisms [15, 20]:

$$\frac{dR_{dep}}{dt} = A_{arrival}\eta_{stick} + I_v \quad (6)$$

196 where $A_{arrival}$ is the flow flux of the arrival ash particles due to the inertial impaction and thermophoretic
 197 force, η_{stick} is the sticking efficiency and I_v is the vapour condensation mass flux. Based on the
 198 assumption that the alkali phase reactions are chemical equilibrium reactions because the furnace
 199 temperature is high enough for equilibrium to be reached quickly [20]. The vapour condensation mass flux,
 200 I_v , can be determined by the following equations [20, 48]:

$$I_v = Sh(T_g) \frac{(D_v(T_g)D_v(T_s))^{1/2}}{D_h R_g} \left[\frac{p_v(T_g)}{T_g} - \frac{p_{v,s}(T_s)}{T_s} \right] \quad (7)$$

$$Sh(T_g) = 0.023Re^{0.8}Sc(T_g)^{0.4} \quad (8)$$

$$Sc(T_g) = \mu_g / (\rho_g D_v(T_g)) \quad (9)$$

201 where $Sh(T_g)$ is the Sherwood number, $Sc(T_g)$ is the Schmidt number, Re is the Reynold number, $D_v(T)$
 202 is the vapour diffusivity at flue gas temperature, T_g , or deposition surface temperature, T_s , $p_v(T_g)$ is the
 203 partial pressure of the alkali vapour, $p_{v,s}(T_s)$ is the saturation vapour pressure, D_h is the hydraulic diameter
 204 of the flow channel, and R_g is the specific gas constant. In this study, only the alkali vapour of sodium
 205 chloride (NaCl) is considered since NaCl is the major alkali vapour phase of ZD lignite studied according
 206 to the chemical equilibrium calculation. For fuels with high content of potassium (K), the major K related
 207 alkali vapour phases should be considered as well.

208 The deposit properties (porosity, thermal conductivity, deposition surface temperature, etc.) may
 209 change with the deposit growth. Previous research indicates that these changes may have the following
 210 characteristics: (i) the deposition surface temperature can increase and the heat flux through the deposit can

211 decrease; (ii) the physical structure of the deposit can change from a loose and porous structure to a dense
 212 and molten structure; (iii) hence, the porosity can reduce at the sintered/slag slayer and the thermal
 213 conductivity can increase. For the initial layer, the thermal conductivity is given a value of 0.14 W/m·k [49,
 214 50] and then the measured thermal conductivity from [5] is employed in this study, which shows the
 215 thermal conductivity will increase with the deposit growth.

216 A correlation based on the temperature and deposit composition is employed to calculate the deposit
 217 porosity as follows [22, 30, 31]:

$$\varepsilon_{deposit} = 1 - \left[(1 - \varepsilon_0) + \frac{V_{liq}}{V_{solid}} (1 - \varepsilon_0) \right] \quad (10)$$

218 where $\varepsilon_{deposit}$ is the deposit porosity, ε_0 is the initial deposit porosity, V_{liq} is the volume of the liquid
 219 phase, and V_{solid} is the volume of the solid phase. Calculation of the volume fraction of the liquid phase
 220 and solid phase is performed by using chemical equilibrium methods and then estimating the density of the
 221 liquid phase as a function of the chemistry using the method described by Mills et al. [51]. The deposit
 222 thickness, $L_{deposit}$, can be described as follows:

$$\frac{dL_{deposit}}{dt} = \frac{A_{arrival}\eta_{stick} + I_v}{\rho_p(1 - \varepsilon_{deposit})} \quad (11)$$

223 The deposition surface temperature, T_{ds} , can be calculated based on the total heat flux to the probe (q_{total})
 224 predicted from the CFD calculations, the deposit thickness ($L_{deposit}$) and the total thermal resistance (R)
 225 are as follows [23, 30]:

$$T_{ds} = q_{total}R + T_{oil} \quad (12)$$

$$R = \frac{L_{deposit}}{k_{deposit}} + \frac{L_{steel}}{k_{steel}} + \frac{1}{h_{oil}} \quad (13)$$

226 where T_{oil} is the temperature of the cooling oil, $k_{deposit}$ is the thermal conductivity of the deposit, L_{steel}
 227 and k_{steel} are the thickness and the thermal conductivity of the stainless steel probe, respectively, and h_{oil}
 228 is the heat transfer coefficient of the cooling oil.

229 *3.4 Integration of the ash deposition model with the CFD framework*

230 In this paper, the commercially available CFD software package ANSYS Fluent version 16.0 has
 231 been employed to perform the basic calculations, incorporating the in-house developed User Defined
 232 Functions and Memories in order to model the ash deposition growth process. Mathematical submodels,

233 such as the SST $k-\omega$ model, Discrete Ordinate model and Discrete Phase Model (DPM), were used for
 234 modelling the turbulence, radiation heat transfer and particle trajectories. In addition, the in-house
 235 developed FSCK based radiation model [52, 53] has been tested in this study, which shows similar heat
 236 transfer predictions compared to the standard WSGGM based radiation model. The present CFD model
 237 focuses on the deposition probes being placed in the central region of the furnace. A 2D geometry with a
 238 tube of diameter 40mm placed in the central region is considered as the computational domain. A fine
 239 mesh is generated around the deposition probe in order to resolve the flow-field within the boundary layer
 240 and minimize numerical inaccuracies in predicting the particle impaction efficiency. Figure 2 shows a
 241 schematic diagram of the computational domain and the meshing scheme around the deposition probe. The
 242 size of the first cell around the tube is approximately 0.3mm, which is suggested by [42, 54, 55], in order
 243 to accurately predict both the particle impaction efficiency and the particle temperature. In this paper, three
 244 cases with different furnace temperature have been investigated, namely, 1373 K, 1543 K and 1593 K. It is
 245 assumed that the discrete parcels of particles are uniformly distributed and the particles are injected
 246 through the inlet boundary condition [27-29]. The flow rate of the ash particles of $1.153 \text{ g}\cdot\text{s}^{-1}$ and the
 247 velocity of the flue gas (N_2 -0.758, CO_2 -0.166, O_2 -0.05, H_2O -0.026, mole fraction) and particles of $2.8 \text{ m}\cdot\text{s}^{-1}$
 248 ¹ have been used from the experiments [5]. The ash particle size ranges between $1 \mu\text{m}$ and $60 \mu\text{m}$ with a
 249 mean diameter of $16 \mu\text{m}$ and a spread parameter of 0.7 based on Rosin-Rammler distribution, which
 250 indirectly results from the original coal particle size distribution and the ash content [5, 56]. It should be
 251 noted that aerosols generated from nucleation of the alkali vapour is neglected due to the high furnace
 252 temperature [1].

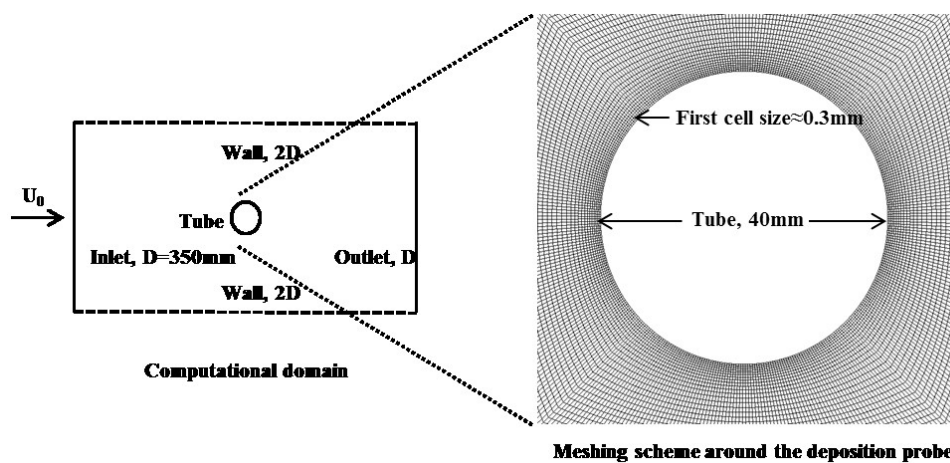
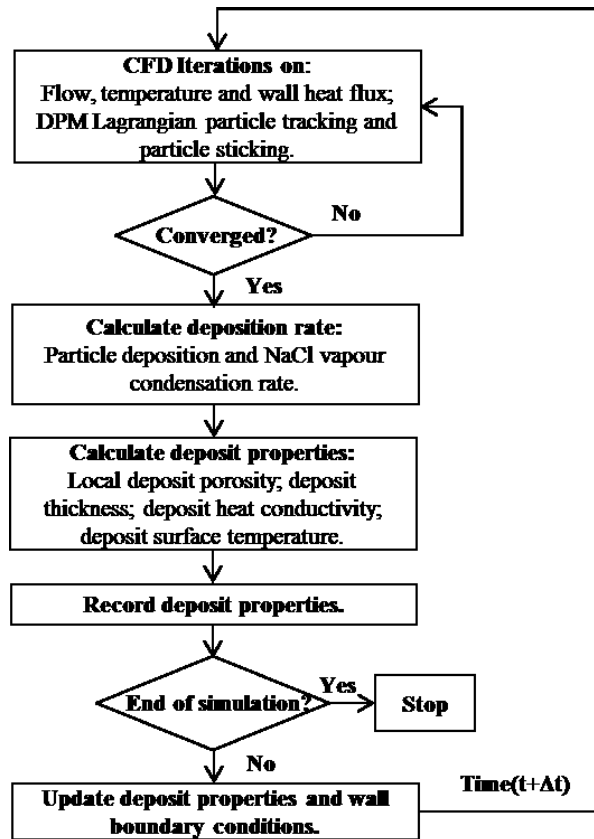


Figure 2. Schematic diagram of computational domain and meshing scheme around the deposition tube.



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Figure 3. The algorithm of the ash deposition growth model integration in the CFD framework.

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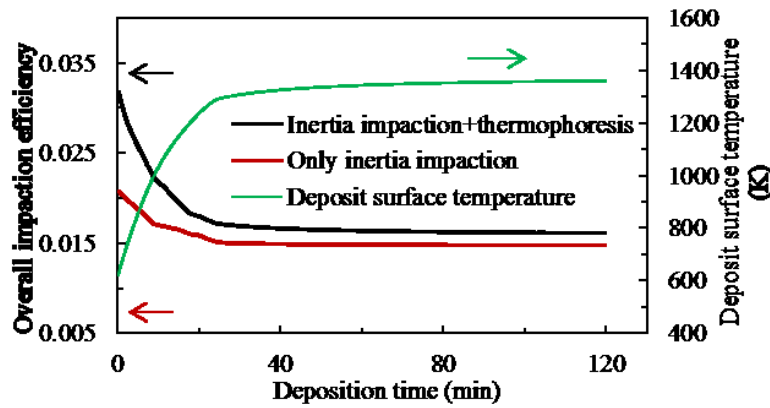
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Figure 3 shows a brief flow chart of the algorithm used to carry out the simulation of the ash deposition growth process. A similar quasi-transient calculation concept has also been used to integrate the deposition model with the CFD framework [23, 26, 30]. In a time step, CFD iterations are carried out to solve the gas flow, temperature and wall heat flux. Then the Lagrangian particle tracking and particle sticking procedures are performed to determine the particle deposition. The total deposition rate can be determined by the particle deposition and the direct alkali vapour condensation rate. Then the new deposit properties (porosity, thickness, thermal conductivity, total heat resistance, etc.) are calculated, updated and stored in the User Defined Memories. In addition, a new deposition surface temperature is calculated based on the total heat flux and the total heat resistance from the updated deposit properties; the new deposition surface temperature is given to the wall boundary surface conditions by the User Defined Functions for the CFD calculation in the next time step and this process is continued until the end of the simulation. It should be noted that the simulation process starts with a clean deposition tube (deposition time=0) placed in the furnace and the initial surface temperature is predicted based on the total thermal resistance contributed from the probe itself and the cooling oil [23], as shown in Equation (12) and (13). In addition,

271 the calculation ends within two hours of the deposition time, where the shedding is less important [5]. The
 272 time step size is dynamically determined by limiting the increase in the deposition surface temperature in a
 273 time step to be less than 1K in order to achieve a balance between the accuracy of the simulations and the
 274 expenses of the computation time. Therefore, a time step size of 1 s was employed at the initial stage
 275 because the surface temperature increased at a high rate at this stage. The time step size gradually
 276 increased to 30s at the later stages because the increase of deposition surface temperature became very
 277 small.



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 279 **Figure 4.** The overall particle impaction efficiency and deposition surface temperature as a function of the
 280 deposition time.

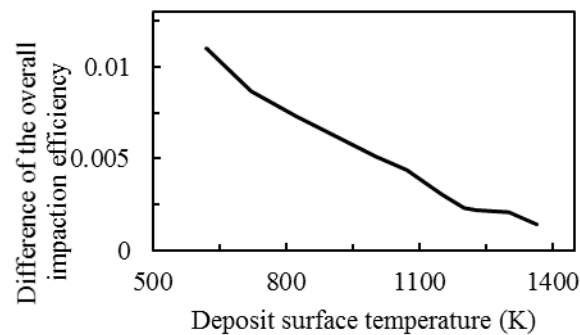
281 4 Results and discussions

282 4.1 Predicted results of the baseline case (furnace temperature under 1543 K)

283 4.1.1 Particle impaction efficiency and sticking efficiency

284 The prediction of the particle impaction and sticking is critical for modelling the ash deposition
 285 formation because particle impaction and sticking determine the amount of the arrival particles which may
 286 stick on the deposition probe surface. Figure 4 shows the predicted overall particle impaction efficiency
 287 (defined as the overall mass flow rate of the particles impacting on the probe to the overall mass flow rate
 288 of particles in the projected surface area) and the deposition surface temperature as a function of the
 289 deposition time. It can be found that, under the conditions without thermophoretic force and with only the
 290 inertia impaction, the overall particle impaction efficiency ($\eta_{i_inertia}$), which has a value ranged from
 291 0.021 to 0.015, decreases with an increase in the first 30 minutes and then it remains essentially unchanged.
 292 This is because the local condition near the deposition surface (velocity, gas viscosity, etc.) changes with

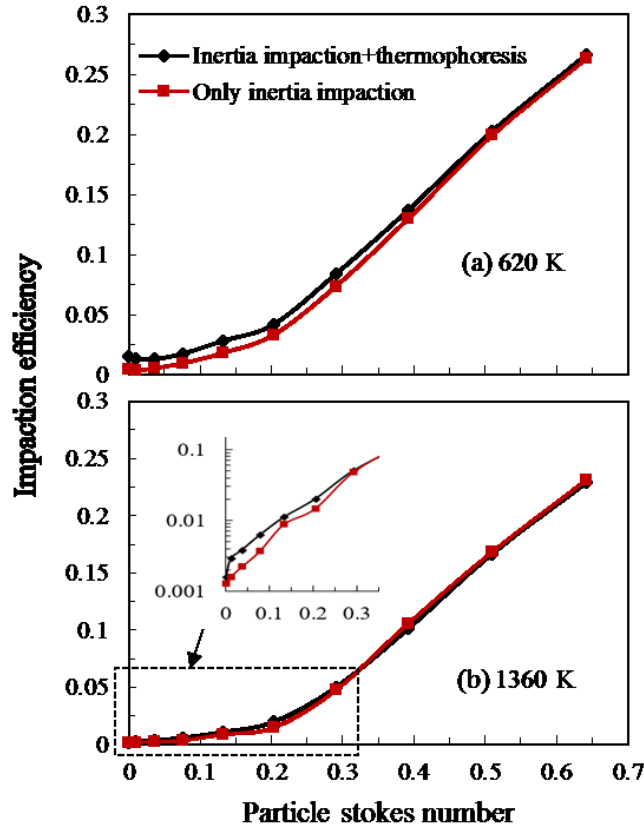
293 the deposition growth. Under the condition with both the inertia impaction and thermophoretic force, the
 294 overall particle impaction efficiency ($\eta_{i_inertia+tp}$) shows a similar variance trend compared to $\eta_{i_inertia}$.
 295 In addition, $\eta_{i_inertia+tp}$ is larger than $\eta_{i_inertia}$, ranging from 0.032 to 0.016. Also, Figure 5 shows that
 296 the difference of overall particle impaction efficiency between $\eta_{i_inertia+tp}$ and $\eta_{i_inertia}$ gradually
 297 reduces with the increase in the deposition surface temperature. This is because the influence of the
 298 thermophoretic force on the particles, which is dictated by the thermal gradient near the deposit surface, is
 299 decreased as a result of the increase in the deposition surface temperature. Therefore, the thermophoretic
 300 force contributes to the overall particle impaction efficiency by as much as 50% in the initial stage and
 301 nearly 10% at the later stage. Beckmann et al. [15] also found that the thermophoresis could increase the
 302 arrival rate of the particles by as much as 7%-50% onto the cooled deposition tube. The amount of the
 303 increased overall particle impaction efficiency (or the arrival rate) by the thermophoresis is determined by
 304 the particle size distribution and the thermal gradient in the vicinity of the deposition surface.



305
 306 **Figure 5.** The difference of overall particle impaction efficiency between $\eta_{i_inertia+tp}$ and $\eta_{i_inertia}$ as a
 307 function of the deposition surface temperature.

308 In order to further investigate the influence of the thermophoresis on the individual particle impaction
 309 behaviour, the impaction efficiency of the particles as a function of the particle Stokes number is shown in
 310 Figure 6. It can be seen that, under the condition without thermophoretic force and with only the inertia
 311 impaction, the particle impaction efficiency ($\eta_{pi_inertia}$) is very small and close to zero (smaller than 0.01)
 312 when the particle Stokes number is less than 0.1 and then the particle impaction efficiency sharply
 313 increases with an increase in Stokes number. This is because the particles with a larger Stokes number are
 314 less likely to be affected by the gas flow and more likely to impact on the deposition surface. However,
 315 particles with smaller Stokes number follow more closely to the fluid streamlines and they are less likely to
 316 impact on the surface [57]. Similar variations of the particle impaction efficiency by the inertia impaction

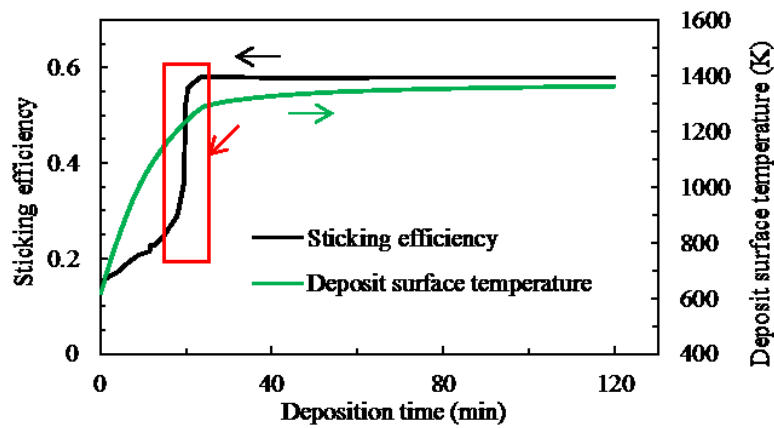
317 is also predicted in the references [18, 36, 42, 55] using the RANS, LES and DNS based CFD methods.
 318 However, under the condition with both the inertia impaction and thermophoretic force, the particle
 319 impaction efficiency ($\eta_{pi_inertia+tp}$) is larger than $\eta_{pi_inertia}$, as shown in Figure 6. In addition, the
 320 influence of the thermophoresis on the increase in the efficiency is enhanced with a decrease in the
 321 deposition surface temperature, as shown in Figure 6. This results in a higher increase of overall impaction
 322 efficiency with a lower deposition surface temperature as shown in Figure 4 and Figure 5.



323
 324 **Figure 6.** The particle impaction efficiency ($\eta_{pi_inertia}$, only inertia impaction; $\eta_{pi_inertia+tp}$, inertia
 325 impaction and thermophoresis) as a function of particle Stokes number under a low deposition surface
 326 temperature (620 K) and a high deposition surface temperature (1360 K).

327 Figure 7 shows the predicted overall particle sticking efficiency (defined as the ratio of the overall
 328 mass flow rate of the deposited particles to the overall mass flow rate of the impacting particles) and the
 329 deposition surface temperature as a function of the deposition time. It can be observed that the overall
 330 particle sticking efficiency gradually increases with an increase in the deposition time and then it remains
 331 essentially unchanged, ranging from 0.15 to 0.58, and a corresponding increase in the deposition surface
 332 temperature, then a nearly flat variance of the temperature. It is noticed that there is a transition of a sharp

333 increase in the sticking efficiency and this occurs at nearly 25 mins deposition time, which corresponds to
 334 a deposition surface temperature of approximately 1230 K, as shown by the red rectangle and the red
 335 arrow in Figure 7. This is because the deposit surface starts to melt at this temperature and becomes sticky
 336 according to the chemical equilibrium calculations. It is also noted that the sticking efficiencies for the
 337 particles increase with an increase in the Stokes number. This is because the ash particles were at the
 338 cooling stage when moving towards the cold deposition surface, the small particles cool earlier and more
 339 quickly and thus have a lower temperature [13, 18].



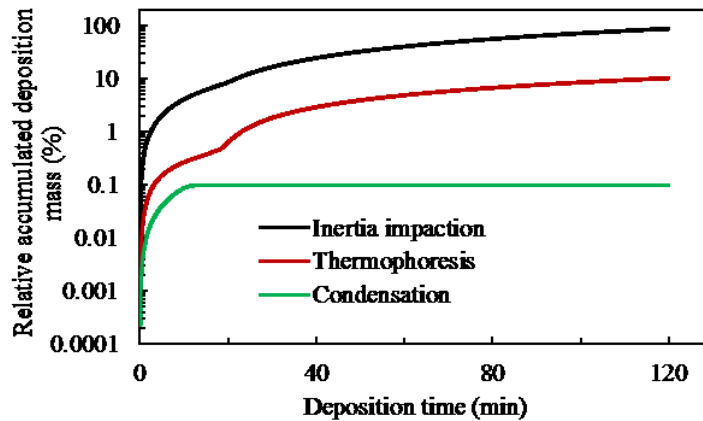
340

341 **Figure 7.** The overall particle sticking efficiency and deposition surface temperature as a function of the
 342 deposition time.

343 4.1.2 Deposition properties

344 In order to understand the contribution of the deposition mechanisms (the inertia impaction and the
 345 thermophoresis, and the direct vapour condensation) on the deposition formation, the relative accumulated
 346 deposition mass (defined as the ratio of the accumulated deposition mass to the total deposition mass after
 347 two hours' deposition time) by the three deposition mechanisms as a function of the deposition time as
 348 shown in Figure 8. It is found that the relative accumulated deposition mass caused by both the inertia
 349 impaction and the thermophoresis gradually increases with an increase in the deposition time. The
 350 deposition caused by the direct alkali vapour condensation is only accumulated in the initial stage for
 351 approximately thirteen mins by the deposition model. This is because the saturation vapour pressure of the
 352 alkali phase (NaCl) increases with an increase in the deposition surface temperature. When the saturation
 353 vapour pressure is high enough, the partial pressure of the alkali vapour (NaCl) cannot support the direct
 354 vapour condensation according to the direct alkali vapour condensation model [20, 48]. In addition, it can

355 be seen that the relative accumulated deposition mass caused by the inertia impaction is almost eight times
 356 as large as that by thermophoresis. The relative accumulated deposition mass caused by the direct
 357 condensation is the smallest, which is hundred times smaller than that caused by the inertia impaction. In
 358 addition, the contribution of the direct condensation (defined as the ratio of the accumulated deposition
 359 mass by the direct condensation to the total accumulated deposition mass) only accounts for approximately
 360 2% in the initial stage and 0.1% in the final stage.

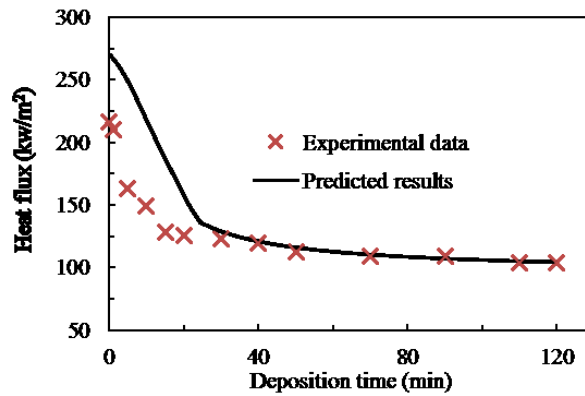


361
 362 **Figure 8.** The relative accumulated ash deposition mass by different deposition mechanisms as a function
 363 of the deposition time.

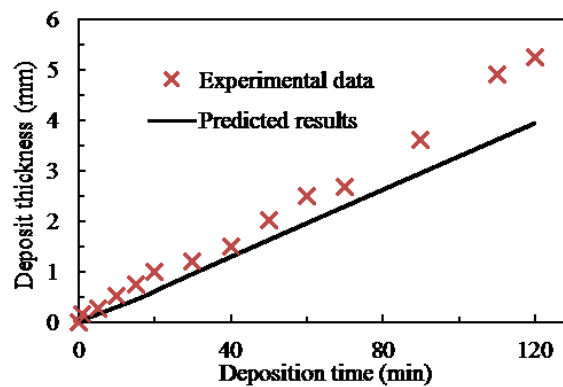
364 Therefore, the predicted results suggest that the main deposition mechanisms are the inertia impaction
 365 and the thermophoresis and the contribution by the direct vapour condensation is less significant. In
 366 addition, the experimental observations of the ash composition in the different layers of the deposit show
 367 that the sodium content among all the deposit layers is less than that in the original ash and the sodium
 368 content in the inner layer is larger than that in the outer layers for the studied furnace temperature [5],
 369 which is consistent with the predicted results related to the contribution of the alkali vapour condensation.
 370 Wu et al. [8] found that the particle depositions, rather than the vapour condensation, are the main ash
 371 deposition mechanisms in the radiation section for Zhundong lignite combustion in a pilot-scale
 372 combustion test. Leppänen et al. [20] also found that the contribution of the direct alkali vapor
 373 condensation, which only contributes up to 0.01% of the total deposited mass, is insignificant. A similar
 374 direct vapour condensation model to that employed in this study [20].

375 However, it should be noticed that the vapour condensation may become significant for ash deposition
 376 formation in the convection section which has a much lower furnace temperature than that in the radiation

377 section. Under a lower furnace temperature, alkali vapour may behave under the following modes [10, 20,
 378 58]: (i) nucleation to generate fume particles; (ii) condensation onto already existing particles; (iii) direct
 379 condensation onto the deposition surfaces. Fume particles can enhance the initial ash deposition formation
 380 on the cooled superheater surfaces by the thermophoretic force [1, 20]; the particle surfaces coated with
 381 condensed alkali phases could have a higher sticking possibility [10]. Li et al. [1] investigated the ash
 382 deposition formation of Zhundong lignite combustion in a down-fired furnace and they found that the fume
 383 particles generated by indirect alkali vapour condensation could initiate the ash deposition formation under
 384 a furnace temperature of almost 1073 K and the bulk fly ash particles with a sticky surface possibly coated
 385 by the condensed alkali vapour phases further enhance the ash deposition formation.



386
 387 **Figure 9.** Comparison of the heat flux through the deposit between the predicted results and the
 388 experimental data as a function of the deposition time.

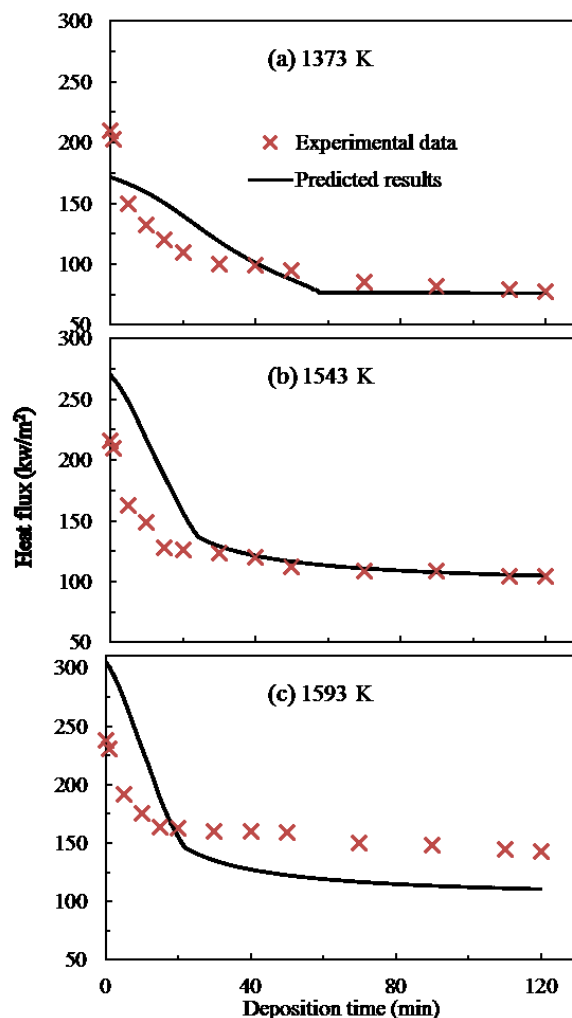


389
 390 **Figure 10.** Comparison of the average deposit thickness between the predicted results and the
 391 experimental data as a function of the deposition time.

392 *4.1.3 Heat transfer properties and deposition growth*

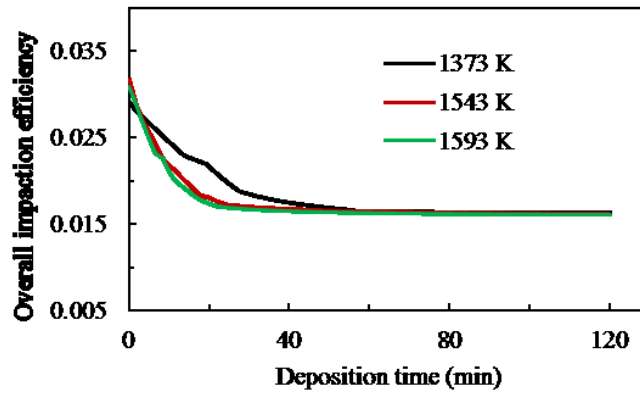
393 In order to understand the heat transfer abatement with the ash deposition formation and growth, the
 394 heat flux (including both the predicted results and the experimental results) through the deposit as a

395 function of the deposition time is shown in Figure 9. Generally, it can be observed that the predictions are
 396 in reasonable agreement with the experimental data. The heat flux significantly decreases in the first half
 397 an hour and then slowly decreases in the later stages, which is consistent with the fact that the initial stage
 398 of the ash deposition is significant in the heat transfer abatement [22]. This is because the heat conductivity
 399 of the deposit is quite low in the initial stage due to its high porosity and low degree of sintering [5, 49, 50],
 400 even though the accumulated deposit at this stage is not huge compared to that in the later stage, as shown
 401 in Figure 8. **The average deposit thickness (including both the predicted results and the experimental
 402 results) as a function of the deposition time is shown in Figure 10.** It can be seen that the predicted deposit
 403 thickness shows a lower growth rate compared to the experimental data. This may be a result of the
 404 underestimation of the deposition rate. Up to date, it is still a challenge to quantitatively predict the particle
 405 sticking efficiency, which needs a robust sticking model to take into consideration the particle melting
 406 behaviour (ash chemistry), particle kinetic energy (particle diameter and velocity) and material properties
 407 of the particle and deposit surface, which will be considered as a future work.

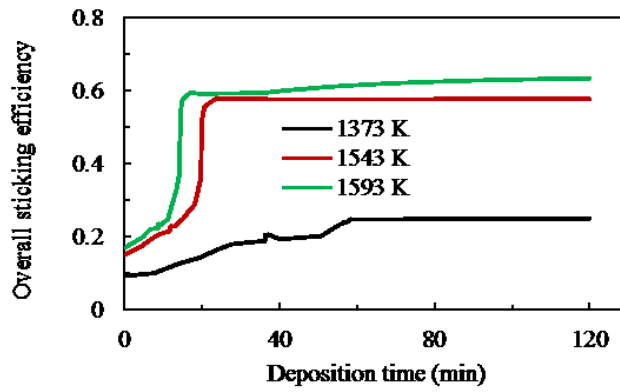


408

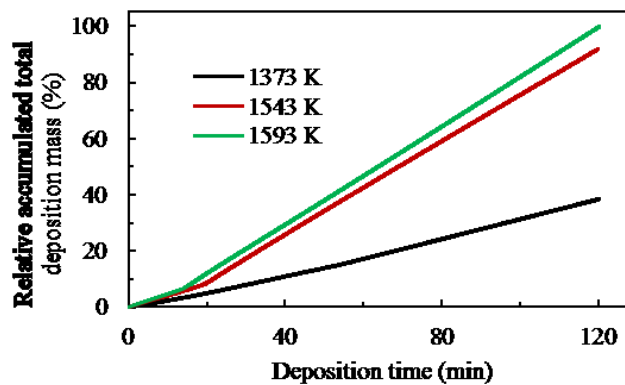
409 **Figure 11.** Comparison of the heat flux between the predicted results and the experimental data as a
410 function of the deposition time for the three cases.



411
412 **Figure 12.** Overall particle impactation efficiency as a function of the deposition time under different
413 furnace temperatures.



414
415 **Figure 13.** Overall particle sticking efficiency as a function of the deposition time under different furnace
416 temperatures.



417
418 **Figure 14.** Accumulated total deposition mass as a function of the deposition time under different furnace
419 temperatures.

420 *4.2 Ash deposition formation under different furnace temperatures*

421 The furnace temperature, which can influence the local temperature condition (the impacting particle
422 temperature and the thermal boundary near the deposition surface), is a significant factor that controls the
423 ash deposition formation. Therefore, it is important to investigate the ash deposition behaviour under
424 different furnace temperatures by using the present deposition model. Figure 11 shows a comparison of the
425 heat flux between the predicted results and the experimental data among the three different furnace
426 temperatures as a function of the deposition time. It can be seen that the three curves show similar variance
427 trends. Generally, it can be seen that the predictions are in reasonable agreement with the experimental
428 data for the three cases. Also, it is noticed that higher furnace temperatures result in a higher heat flux.
429 Figure 12 shows a comparison of the overall particle impaction efficiency for the three different furnace
430 temperatures as a function of the deposition time. It is noticed that the 1543 K case has a similar overall
431 impaction efficiency compared to that of the 1593 K case. At the initial stage of deposition formation, the
432 1373 K case has a much higher overall impaction efficiency than both the 1543 K and 1593 K cases at the
433 same deposition time. This is because the deposition surface temperature under a lower furnace
434 temperature is much lower than that under a higher furnace temperature at the same deposition time, which
435 can result in a larger thermal gradient near the deposit surface and a higher thermophoresis increase in the
436 particle impaction efficiency. Figure 13 shows a comparison of the overall particle sticking efficiency for
437 the three different furnace temperatures as a function of the deposition time. It can be observed that the
438 sticking efficiency increases with an increase in the furnace temperature based on the present sticking
439 model. The efficiency reaches the highest value in the later deposition stage, 0.25, 0.58 and 0.63 for 1373
440 K, 1543 K and 1593 K cases, respectively. Figure 14 shows a comparison of the accumulated deposition
441 mass (normalized by the total accumulated deposition mass after two hours' deposition time for the 1593
442 K case) for the three different furnace temperatures as a function of deposition time. It is found that there is
443 much more deposit mass accumulated under a higher furnace temperature. This is mainly because there is
444 a much higher particle sticking efficiency under a higher furnace temperature as shown in Figure 13.

445 Therefore, the predicted results suggest that the heat flux through the deposit increases with increasing
446 the furnace temperature and this is confirmed by the experimental data. In addition, both the deposit mass
447 and the deposit thickness are larger under a higher furnace temperature than those under a lower furnace
448 temperature. This is because the particle sticking efficiency increases with an increase in the furnace

449 temperature. Wu et al. [8] also observed a higher deposition rate under a higher furnace temperature in the
450 radiation section for the Zhundong lignite combustion in a pilot-scale combustion test. However, Zhou et
451 al. [5] found that the stable deposit thickness (when the shedding rate is balanced with the deposition rate)
452 under a lower furnace temperature is higher than that under a higher furnace temperature. This may be
453 attributed to the combined effect of the deposition rate, shedding rate, and the deposit microstructure.

454 **5 Conclusions**

455 A dynamic ash deposition model based on inertia impaction, thermophoresis and direct alkali vapour
456 condensation has been developed for the modelling of the ash deposition formation on a cooled deposition
457 probe under high furnace temperatures in a pilot-scale furnace. The ash deposition model incorporates the
458 energy conservation principles to include the effect of the heat transfer on the deposition growth. In
459 addition to the growth of the deposition on the probe, the particle impaction and sticking behaviours have
460 been investigated. Also, the ash deposition behaviour under different furnace temperatures is studied
461 through the developed deposition model.

462 The predicted results for the ash deposition behaviour and the heat flux through the deposition probe
463 have been compared with the experimental data obtained from ZD lignite combustion in the pilot-scale
464 furnace and qualitative agreement is obtained. The results suggest that the ash deposition formation is
465 mainly dictated by the particle deposition from the inertia impaction and the thermophoresis under high
466 furnace temperatures. The deposition caused by the direct alkali vapour condensation is less significant.
467 The overall particle impaction efficiency decreases with the deposit growth at the initial stage and
468 stabilised at higher deposition surface temperature. This is mainly due to the decrease in the effect of
469 thermophoresis. The overall particle sticking efficiency increases with the deposit growth due to the
470 increase in the local temperature conditions (particle temperature and the deposition surface temperature).
471 The heat flux through the deposition probe significantly decreases at first and then slowly decreases as the
472 deposit builds up. Also, it is noticed that both the particle impaction and stickiness control the ash
473 deposition formation. Much higher sticking efficiency can result in a larger deposition rate under a higher
474 furnace temperature, while the calculated overall particle impaction efficiency decreases at the initial stage.
475 This is because the deposition surface temperature increases to a much higher level under higher furnace
476 temperature and this results in a lower thermophoresis influence of the particle impaction.

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