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1 **Application of Independent Component Analysis to multi-temporal InSAR data with**  
2 **volcanic case studies**

3  
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7

8 **Key points**

- 9
- 10 1. Independent Component Analysis is appropriate for exploratory analysis of InSAR data
  - 11 2. Deformation can be identified automatically by cluster analysis of independent  
12 components
  - 13 3. Application of ICA demonstrated on Sentinel-1A imagery using contrasting volcanic  
14 examples
- 15

16 **Abstract**

17 A challenge in the analysis of multi-temporal Interferometric Synthetic Aperture Radar (InSAR)  
18 data is distinguishing and separating volcanic, tectonic and anthropogenic displacements from  
19 each other and from atmospheric or orbital noise. Independent Component Analysis (ICA) is a  
20 method for decomposing a mixed signal based on the assumption that the component sources are  
21 non-Gaussian and statistically independent. ICA has potential as a tool for exploratory analysis  
22 of InSAR data, and in particular for testing whether geophysical signals are related or  
23 independent. This article presents tests of the applicability of ICA to InSAR using synthetic data  
24 and application to Sentinel-1A archive images from two contrasting examples of volcano  
25 deformation. Co-eruptive subsidence associated with the April 2015 eruption of Calbuco (Chile)  
26 was identified in spatial patterns found by maximising both spatial and temporal independence.

27 Spatial patterns and rates of lava subsidence were retrieved using ICA analysis of interferograms  
28 from Parícutin lava fields (Mexico), and found to be consistent with previous observations.

29 I demonstrate that ICA is an appropriate method for the analysis of volcanic signals in the  
30 presence of atmospheric noise, and propose a strategy for the automatic identification of  
31 geophysical displacements using cluster analysis of the spatial patterns of independent  
32 components. This approach allows the detection of geophysical processes on a range of scales  
33 and provides a test of signal independence where multiple displacement sources are active.

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## 37 **1.0 Introduction**

38 Interferometric Synthetic Aperture Radar (InSAR) allows centrimetric to millimetric movement  
39 of the ground to be measured on the scale of 10-100s of kilometres at a spatial resolution of <10s  
40 metres and temporal resolution of days to months (e.g., Bürgmann et al., 2000; Simons & Rosen,  
41 2007). InSAR measurements have been used to measure deformation during all stages of the  
42 earthquake cycle (Massonet et al., 1993; Elliott et al., 2016), and to observe a broad range of  
43 processes that cause deformation at volcanoes (Pinel et al., 2014; Biggs et al., 2014).

44 Here, I present an application of a blind source separation method, Independent Component  
45 Analysis (ICA), for identifying and analysing displacement signals in InSAR data. I describe the  
46 potential of the method, already widely used in other branches of remote sensing, medical  
47 physics and geophysics, for application to multi-temporal InSAR data (Section 2). I  
48 demonstrate its application using sets of synthetic interferograms (Section 3.1) and analyze two  
49 contrasting styles of volcanic deformation using Sentinel-1 imagery acquired since the  
50 instrument's launch in 2014 (Sections 3.2-3.3).

## 51 **1.2 Mixed signals: atmospheric and geophysical signals**

52 A major challenge for using InSAR for the measurement of geophysical signals is the separation  
53 of true surface displacements from atmospheric noise (e.g., Zebker et al., 1997; Beauducel et al.,  
54 2000). Atmospheric signals in interferograms are the consequence of differences in the

55 refractivity of the atmosphere between satellite acquisitions caused by variations in  
56 concentrations of water vapour ('wet delay') and hydrostatic pressure ('dry delay') (e.g., Hansen,  
57 2001). Where the atmosphere is stratified, changes to water vapour concentration are correlated  
58 with topography and may mask deformation signals with similar or lower magnitude at high  
59 relief faults and at volcanoes (e.g., Doin et al., 2009; Poland & Lu, 2004; Ebmeier et al., 2013).  
60 Where turbulent mixing is dominant, atmospheric signals are spatially correlated on the scale of  
61 tens of kilometres (e.g., Lohman & Simons, 2005).

62 Atmospheric signals can be mitigated in sets of interferograms by using approaches that increase  
63 the signal to noise ratio. For example, stacking a set of  $m$  independent interferograms reduces  
64 the standard deviation of signals uncorrelated in time by a factor of  $\sqrt{m}$  (Emardson et al., 2003).  
65 This approach is very effective for estimating constant rates of deformation in the presence of  
66 turbulent atmospheric signals, but does not mitigate the effect of stratified water vapour signals,  
67 which are not random in space and may not be sampled evenly across the seasons (Doin et al.,  
68 2009). Atmospheric signals are spatially but not temporally correlated, so can be estimated by  
69 high-pass filtering in time and low-pass filtering in space (Ferretti et al., 2001; Hooper et al.,  
70 2007). Both stacking of repeat acquisitions and spatiotemporal filtering are most effective where  
71 deformation is of much longer duration than the measurement interval (satellite repeat time), but  
72 less effective for deformation captured by only a few interferograms, such as some landslides or  
73 co-eruptive volcanic deformation.

74 Atmospheric signals can be corrected in individual interferograms either empirically (e.g., Wicks  
75 et al., 2002) or using independent predictions or measurements of water vapour and hydrostatic  
76 pressure, and therefore atmospheric phase delays (e.g., Jolivet et al., 2011). Empirical correction  
77 removes the part of the phase caused by stratified water vapour variation by characterising the  
78 relationship between phase delay and topographic height. This may assume a linear (e.g., Elliott  
79 et al., 2008) or non-linear (e.g., Remy et al., 2003) relationship between phase and topography,  
80 which it may be necessary to characterize on different spatial scales across an interferogram  
81 (e.g., Bekaert et al., 2015). Model predictions of atmospheric delay may be derived from  
82 regional atmospheric models (e.g., Parker et al., 2015) or nested models that allow higher  
83 resolution predictions at the site of interest (e.g., over Big Island, Hawai'i, Foster et al., 2006).  
84 Interpolated measurements of atmospheric parameters from GPS networks or multi-spectral

85 satellite data can be used to reduce the contribution of atmospheric delays by themselves or in  
86 combination with model predictions (e.g., Walters et al., 2013). The success of such data and  
87 model-based correction depends on (1) the availability and relative spatial density of atmospheric  
88 data or model prediction grid spacing, (2) the relative timing of InSAR and atmospheric data  
89 acquisitions and (3) model initialisation conditions (Foster et al., 2013; Jolivet et al., 2014;  
90 Parker et al., 2015).

91 The correction of atmospheric phase contributions is particularly difficult over rapidly changing  
92 topography, for example, in measuring the slip rate of major faults (e.g., Elliott et al., 2008; Doin  
93 et al., 2009). Volcanic settings introduce additional challenges for both empirical and predictive  
94 atmospheric mitigation, as high topography can induce turbulence on the scale of kilometres, and  
95 volcanic plumes may also contain water vapour (e.g., Wadge et al., 2016).

96 In some settings, it is common for multiple deformation processes to be superimposed in  
97 interferograms. For example, interferograms spanning the period after a large earthquake are  
98 likely to capture displacements associated with large aftershocks, postseismic processes and  
99 landsliding. Variations in hydrological loading, fault creep and anthropogenic deformation may  
100 occur in the same area over longer timescales and mask the presence of lower magnitude  
101 processes. At an active volcano, multiple related or independent processes often result in  
102 simultaneous surface displacements, including magma movement, magma phase changes, small  
103 earthquakes, and the post-emplacment adjustment of erupted pyroclastic flows, lahars and lavas  
104 (e.g., Jay et al., 2014; Caricchi et al, 2014, Ebmeier et al., 2014). Where a deformation source  
105 has been well characterized, it can be subtracted before modelling (e.g., González et al, 2012). If  
106 temporal and spatial characteristics of any of a set of superimposed sources are known, it may  
107 also be possible to separate signals empirically, in a similar manner to the methods for mitigating  
108 spatially correlated atmospheric noise.

109 ICA provides a tool for exploratory analysis of mixed signals in interferograms and a robust test  
110 for signal independence. It is complementary to mitigating atmospheric or deformation signals  
111 using modelling or empirical correction, and requires very limited a priori assumptions about  
112 signal characteristics.

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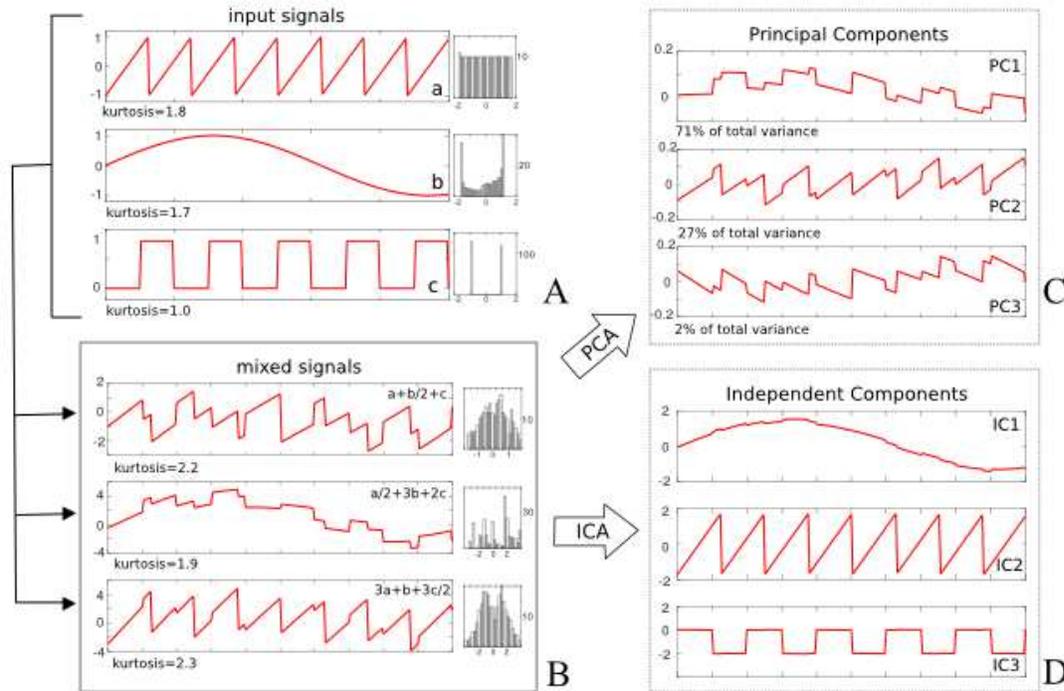
## 114 1.2 Independent Component Analysis

115 Independent Component Analysis (ICA) is a computational signal processing method that aims  
116 to describe random variables as a linear combination of statistically independent components  
117 (e.g, Comon, 1994; Hyvärinen & Oja., 1997; Stone, 2004). This is achieved by the  
118 decomposition of a mixed signal using the assumption that each constituent component has a  
119 non-Gaussian probability distribution. This assumption is based on the premise that the sum of a  
120 sufficient number of non-Gaussian probability distributions tends towards a Gaussian  
121 distribution (the central limit theorem), so that a strongly non-Gaussian component is unlikely to  
122 be produced by a combination of different sources.

123 The assumption of statistical independence employed by ICA makes it possible to find a unique  
124 solution to the decomposition of a mixed signal, in a similar way that the assumption that sources  
125 are uncorrelated is the basis of Principal Component Analysis (PCA). Because ICA retrieves  
126 sources by maximising statistical independence (rather than signal variance, as in PCA) it is  
127 appropriate for the extraction of low magnitude signals, even where noise is high, without a  
128 priori assumptions beyond the independence of the components (Hyvärinen et al., 2004).  
129 Statistical independence is assessed by non-Gaussianity. This can be quantified using different  
130 properties of the random variables, of which kurtosis and negentropy are widely used. Kurtosis  
131 describes the relative contribution of extreme deviations to a probability distribution  
132 ('tailedness') and is normally measured as the absolute value of the fourth standardized moment  
133 of the data, with a Gaussian distribution taking a value of 3. The calculation of kurtosis is  
134 simple, but in practise it is more sensitive to outliers than negentropy, which is more widely used  
135 for ICA. Negentropy is a concept from information theory that describes the difference in  
136 entropy - a measure of the unpredictability of information content - relative to the Gaussian  
137 distribution of the same mean and variance. This is based on the result that a Gaussian  
138 distribution has the highest value of entropy of all the possible random variables with the same  
139 variance. To avoid the challenging estimation of the probability density function, most  
140 algorithms use an approximation of negentropy to assess Gaussianity (e.g., Hyvärinen & Oja,  
141 2000).

142 Figure 1 illustrates the application of ICA and PCA to a simple one-dimensional example. Three  
143 simple independent signals (Figure 1A) are combined in different ratios to produce signal  
144 mixtures (Figure 1B) that are more Gaussian than each of the individual input signals (and  
145 therefore have higher values of kurtosis). The mixed signals are decomposed to find three  
146 Principal Components (PCs, Figure 1C), identified so that they account for as much of the  
147 variability of the mixed signals as possible, and three Independent Components (ICs, Figure 1D),  
148 that maximize the statistical independence of the components. Although the PCs capture major  
149 features of the input signals (e.g., compare input ‘a’ to PC2), each PC contains contributions  
150 from all three input signals. The ICs are successful in retrieving the structure of the original  
151 inputs, although they are not identical (e.g., compare IC1 to input ‘b’), and their signs and  
152 magnitudes are ambiguous (e.g., the sign of IC3 is the opposite of input ‘c’).

153 ICA allows the decomposition of a mixed signal into a set of linear, additive components. For a  
154 set of  $m$  scalar mixed signals (rows of data matrix,  $\mathbf{X}$ ), with  $n$  ( $\leq m$ ), unknown statistically  
155 independent components (rows of source matrix,  $\mathbf{S}$ ), the linear relationship between the two can  
156 be described as  $\mathbf{X} = \mathbf{A} \mathbf{S}$  (1), where the rows of the unknown mixing matrix,  $\mathbf{A}$  ( $m \times n$ ) are  
157 coefficients that describe the relative contribution of each source to a particular mixed signal  
158 (Figure 2). Each independent component is then estimated by choosing unmixing vectors that  
159 maximize the non-Gaussianity of its product with the data, assessed using a property such as  
160 kurtosis or negentropy (the specific approach taken by the FastICA algorithm used in this study  
161 is described further in Section 2.1). Because both  $\mathbf{A}$  and  $\mathbf{S}$  are unknown, a scaling factor in one  
162 of the components could always be cancelled out by its inverse factor in the mixing matrix, so  
163 the sign and the variance (and therefore the true magnitude) of independent components are  
164 ambiguous (Hyvärinen & Oja, 2000). However, the part of the signal that is of interest (or the  
165 original mixed signal itself) can be reconstructed as the outer product of the relevant rows of  $\mathbf{A}$   
166 and  $\mathbf{S}$ .



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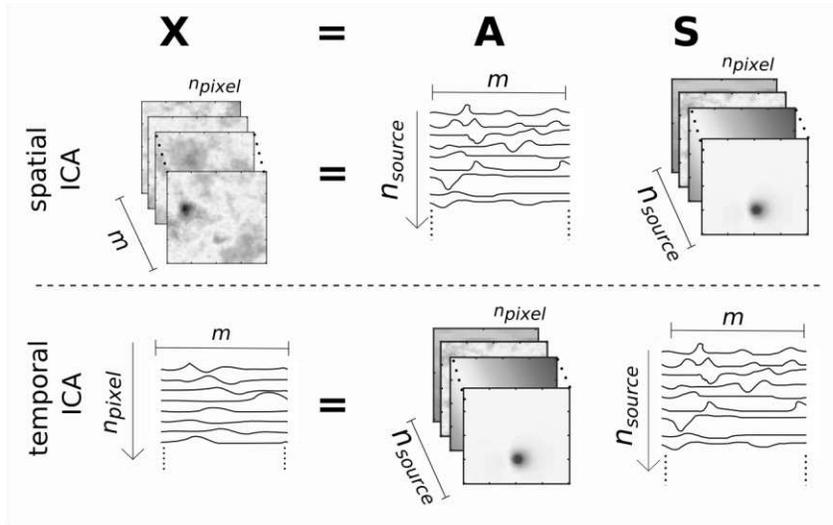
169 **Figure 1:** One dimensional illustration of the application of PCA and ICA to mixed signals.  
170 Three simple input signals (A: a,b,c) are combined in different ratios to produce three mixed  
171 signals (B). Histograms show the distribution of values for the whitened (zero mean,  
172 variance=1) inputs or signal mixtures. The mixed signals are decomposed into Principal  
173 Components (C) and Independent Components (D).

174

175

176 ICA has been applied in medical physics, e.g. to blood oxygen level dependent signals in  
177 functional Magnetic Resonance Imaging (fMRI) used to identify connectivity in brain structures  
178 (Beckmann et al., 2004; Calhoun et al., 2006). For this application many specialized ICA tools  
179 have been developed. Satellite remote sensing applications include hyperspectral unmixing  
180 (Bayliss et al., 1998), cloud masking (Amato et al., 2008) and thermal hotspot detection (Barnie  
181 & Oppenheimer, 2015). ICA has also been used to analyze various geophysical and geochemical  
182 datasets including Global Positioning System time series (Liu et al., 2004), seismic data (De

183 Lauro et al., 2009) and isotopic data (Iwamori et al., 2008).



184

185

186 **Figure 2:** Cartoon illustrating the geometry of decomposition for a multi-temporal InSAR  
 187 dataset,  $\mathbf{X}$ , with  $m$  interferograms, each made up of  $n_{\text{pixel}}$  pixels. For sICA, rows of the mixing  
 188 matrix,  $\mathbf{A}$ , capture the relative contribution of each independent spatial component (rows of  $\mathbf{S}$ ).  
 189 For tICA, spatial patterns are retrieved in the rows of  $\mathbf{A}$ , while independent temporal components  
 190 are retrieved in rows of  $\mathbf{S}$ .

## 191 2.0 Method

### 192 2.1 Application of ICA to InSAR

193 ICA can be used to decompose mixed signals that are a linear combination of statistically  
 194 independent components. As each pixel in an interferogram can be thought of as the sum of  
 195 particular points in time series of various noise and deformation sources, the assumption of linear  
 196 mixing is appropriate for InSAR data. Interferograms are formed by multiplying a first SAR  
 197 radar image ('master') point wise by the complex conjugate of a second image ('slave') to produce  
 198 a map of phase change. If the phase backscattered from the Earth's surface is constant, then the  
 199 interferogram phase ( $\emptyset$ ) between two time-separated radar images consists of the linear  
 200 combination of all of the differences in propagation phase from various temporally and spatially  
 201 varying sources:  $\emptyset = \emptyset_{\text{def}} + \emptyset_{\text{atm}} + \emptyset_{\text{noise}} + \Delta\emptyset_{\text{orbit}}$ , where  $\emptyset_{\text{def}}$  is the phase change due to the  
 202 displacement of the Earth's surface in the direction of the satellite's line of sight, and other  
 203 sources of phase change are normally treated as nuisance factors. A geometric contribution to

204 phase change from the satellite's change in position is corrected from imperfect knowledge of  
205 satellite position and the Earth's topography, leaving just residual phase contributions from errors  
206 in knowledge of satellite position and look angle ( $\Delta\theta_{\text{orbit}}$ ). Thermal noise ( $\theta_{\text{noise}}$ ) is generally  
207 expected to be low magnitude and is neglected, while differences in atmospheric path delay  
208 between the two images ( $\theta_{\text{atm}}$ ) may be of similar or equal magnitude to geophysical signals. For  
209 much InSAR data these noise and deformation sources are expected to be statistically  
210 independent in space and/or time, although correlations between deformation and atmospheric  
211 signals may occur in some circumstances (Section 1.1).

212 For a spatio-temporal dataset, ICA requires that sources are statistically independent in either  
213 space or in time (Figure 2). For spatial ICA (sICA), spatial independence is maximized, and the  
214 number of mixed signals is the same as the number of interferograms ( $m$ ), each sampled at many  
215 thousands of points ( $n_{\text{pixel}}$ ). Phase contributions from errors in the estimation of orbital  
216 contributions, instrument noise, turbulent atmospheric variation and displacement are all  
217 expected to be spatially independent. Deformation caused by different stages of the earthquake  
218 cycle, anthropogenic, hydrological and various volcanic processes all have distinctive spatial  
219 distributions (e.g., Gonzalez et al., 2012, Pinel et al., 2014; Elliott et al., 2016). However, both  
220 variations in a stratified atmosphere and deformation at volcanoes and major faults are often  
221 correlated with topography (e.g., Remy et al., 2003; Doin et al., 2009) and therefore each other.  
222 When tropospheric phase delay is limited to the part of an interferogram where deformation is  
223 occurring, the assumption that sources are spatially independent may be incorrect.

224 Alternatively, one can assume that signal sources are statistically independent in time, so that  
225 each mixed signal is the time-series for one pixel ( $n_{\text{pixel}}$  mixed signals, sampled in each  
226 interferogram). Temporal ICA (tICA) is intuitively appealing, because we expect the time series  
227 of atmospheric variation and deformation caused by different processes to be independent.  
228 However, for whole interferograms (e.g., 10-100 km footprint, pixel size  $\sim 10$ 's m) it is  
229 computationally much more challenging than sICA, because conditioning the mixed signals for  
230 analysis requires the computation of a covariance matrix of the order of  $n_{\text{pixel}}^2$ , where  $n_{\text{pixel}}$  may  
231 be 1000-10,000.

232 If a set of interferograms is used to estimate phase on  $m$  epochs, the matrix of observations,  $\mathbf{X}$ ,  
 233 will have dimensions  $n_{\text{pixel}} \times m$ , where  $n_{\text{pixel}}$  is the number of pixels with phase data for every  
 234 epoch (**Figure 2**). ICA decomposes the mixed signals into a set of  $n_s$  statistically independent  
 235 sources in the rows of source matrix,  $\mathbf{S}$  (sICA:  $n_s \times n_{\text{pixel}}$ ; tICA:  $n_s \times m$ ) and mixing vectors in  
 236 the rows of mixing matrix  $\mathbf{A}$  (sICA:  $n_s \times m$ ; tICA:  $n_s \times n_{\text{pixel}}$ ). Here, this is achieved using a fast  
 237 fixed-point algorithm for ICA (FastICA, Hyvärinen & Oja, 1997; Hyvärinen & Oja, 2000). The  
 238 first steps of this algorithm are the centring and whitening of observations before processing so  
 239 that the mixing matrix is orthogonal, reducing the number of free parameters. This is achieved  
 240 by subtracting the mean from mixed signal matrix,  $\mathbf{X}$ , so that the observations are zero mean  
 241 variables. The mixed signals are then transformed linearly to be expressed in terms of  
 242 uncorrelated variables of variance equal to 1 (whitening or sphering). The FastICA algorithm  
 243 achieves this by preconditioning the centred observations using PCA, which can additionally be  
 244 used to reduce noise in the data. The number of principal components retained for the ICA  
 245 analysis should be lower than the data dimensionality (which is unknown for most real data), so I  
 246 use a trial and error approach to select an appropriate number (e.g., Barnie & Oppenheimer,  
 247 2015). A reasonable starting point can be found by making a rough estimation of the number of  
 248 independent spatial or temporal sources expected for a particular number of interferograms. For  
 249 spatial ICA, a good starting point is one less than the dimension of the data (number of  
 250 interferograms), since the spatially correlated atmosphere that appears in every interferogram is  
 251 independent in time. As orbital and turbulent atmospheric contributions are uncorrelated in time,  
 252 these contribute only Gaussian noise in time and will not be extracted as independent  
 253 components in temporal ICA (e.g., Hyvärinen & Oja, 2000). The number of independent  
 254 temporal sources is therefore likely to be much lower than the dimension of the data (number of  
 255 pixels), and should be reduced to an estimation of the number of temporally correlated processes  
 256 occurring in the area being analyzed. This initial estimation can be iteratively increased so that  
 257 as many PCs as possible are retained without introducing overfitting (identified by sources that  
 258 are isolated peaks in the ICs retrieved, e.g., Hyvärinen, Särelä & Vigário, 1999).

259 The whitened, (potentially reduced dimension) data matrix ( $\mathbf{Z}$ ), is found by multiplying  $\mathbf{X}$  by a  
 260 whitening matrix,  $\mathbf{V}$ , so that  $\mathbf{Z}=\mathbf{VX}=\mathbf{VAS}=\tilde{\mathbf{A}}\mathbf{S}$ , where  $\tilde{\mathbf{A}}$  is an adjusted orthogonal mixing  
 261 matrix. The problem is thus reframed in terms of the whitened data  $\mathbf{Z}=\tilde{\mathbf{A}}\mathbf{S}$ , so that

262 approximation of  $\tilde{\mathbf{A}}^{-1}$ , is an unmixing matrix,  $\mathbf{W}$ , which can be used to estimate the source  
 263 matrix,  $\mathbf{S}$ , from the whitened data,  $\mathbf{Z}$ .

264 The FastICA algorithm estimates unmixing matrix,  $\mathbf{W}$ , using a fixed-point iteration - where each  
 265 point in a converging sequence is a function of the previous one. Each row of  $\mathbf{W}$  is an unmixing  
 266 vector,  $\mathbf{w}$ , that represents a projection of the centred and whitened data ( $\mathbf{Z}$ ) to maximize non-  
 267 Gaussianity as measured using an approximation of negentropy (Hyvärinen & Oja, 2000). For  
 268 each unmixing vector, the iteration is initiated from a random value for  $\mathbf{w}$ , and repeated until  
 269 estimations converge (that is,  $\mathbf{w}_{\text{new}} \cdot \mathbf{w}_{\text{old}} \sim 1$ ). Independent components are extracted one by  
 270 one, with the projections of previously identified mixing vectors ( $\mathbf{w}_1 \dots \mathbf{w}_n$ ) subtracted from the  
 271 next mixing vector ( $\mathbf{w}_{n+1}$ ), which is orthogonalized relative to all the mixing vectors identified so  
 272 far. If the fixed-point iteration failed to converge, then the number of independent components  
 273 extracted were reduced to be one less than the number of principal components.

274 The source matrix,  $\mathbf{S}$ , is then estimated from  $\mathbf{WZ}$ , and the relative contributions of the source in  
 275  $\mathbf{S}$  to each pixel (tICA) or time point (sICA) is then  $\mathbf{V}^{\text{inv}} \mathbf{W}^{-1} (\sim = \mathbf{A})$ , where  $\mathbf{V}^{\text{inv}}$  is an approximate  
 276 inverse of the whitening matrix. Detailed explanations of the FastICA algorithm are provided by  
 277 Hyvärinen & Oja, (1997) and Hyvärinen & Oja, (2000).

278

## 279 **2.2 Identifying and testing the significance of deformation signals**

280 If the spatial or temporal characteristics of a deformation sign are known, then the source can be  
 281 identified by visual inspection of the independent components or mixing matrix. However,  
 282 because FastICA uses random starting points in the estimation of each row of the unmixing  
 283 matrix,  $\mathbf{w}$ , independent components are retrieved in different orders on different runs of the  
 284 algorithm, so that it is difficult to extract the component of interest automatically. This requires  
 285 either a priori information about the location or timing of the target deformation signal, or a test  
 286 of the statistical significance of the retrieved independent sources. Testing the statistical  
 287 significance of sources is important for exploratory analysis of InSAR data, and also provides  
 288 greater flexibility for identifying undescribed or poorly constrained deformation signals.

289 Testing whether independent components capture real aspects of the data can be achieved by  
290 randomising input data in some way (e.g., bootstrapping) and repeating the retrieval of  
291 independent components from different starting points (e.g., FastICA's initial guesses for each  
292 row of  $\mathbf{W}$ ). Independent components that are retrieved by multiple runs are likely to represent a  
293 true property of the data (Hyvärinen, 2013). A better alternative is to compare the spatial  
294 patterns in the independent components or mixing matrices retrieved from ICA of independent  
295 groups of data (e.g., Esposito et al., 2005). In this study, I used the ISCTEST algorithm  
296 (Hyvärinen and Ramkumar, 2013), developed to examine inter-subject or inter-session  
297 consistency in a neuroimaging context. ISCTEST uses an empirical model of the null  
298 distribution of independent components, that is, for the case where components of different  
299 groups of data are no more similar than would be expected by chance. Although the ISCTEST  
300 algorithm was developed for neuroimaging applications, the empirical model of the null  
301 distribution is based only on the assumption that independent components from the same datasets  
302 can be described as part of the same multivariate distribution that captures the spatial patterns of  
303 both signal and noise in the data, with parameters estimated from observations (the algorithm is  
304 explained in detail by Hyvärinen and Ramkumar, 2013). The empirical estimation of the null  
305 distribution is used to estimate the probability that the inter-group similarity of two sources arises  
306 at random. P-values for inter-group similarity can then be used to identify clusters of similar  
307 components.

308 The division of InSAR datasets into independent groups can be conducted systematically or at  
309 random, depending on the characteristics of the source(s) of interest. For example, if  
310 deformation is thought to persist throughout the whole period of observation, then the data set  
311 can be divided into two different blocks of interferograms spanning separate, sequential periods  
312 of time. For short-lived deformation, it may be preferable to randomly divide all acquisition  
313 dates into two separate groups and construct two independent sets of interferograms spanning  
314 similar total time periods.

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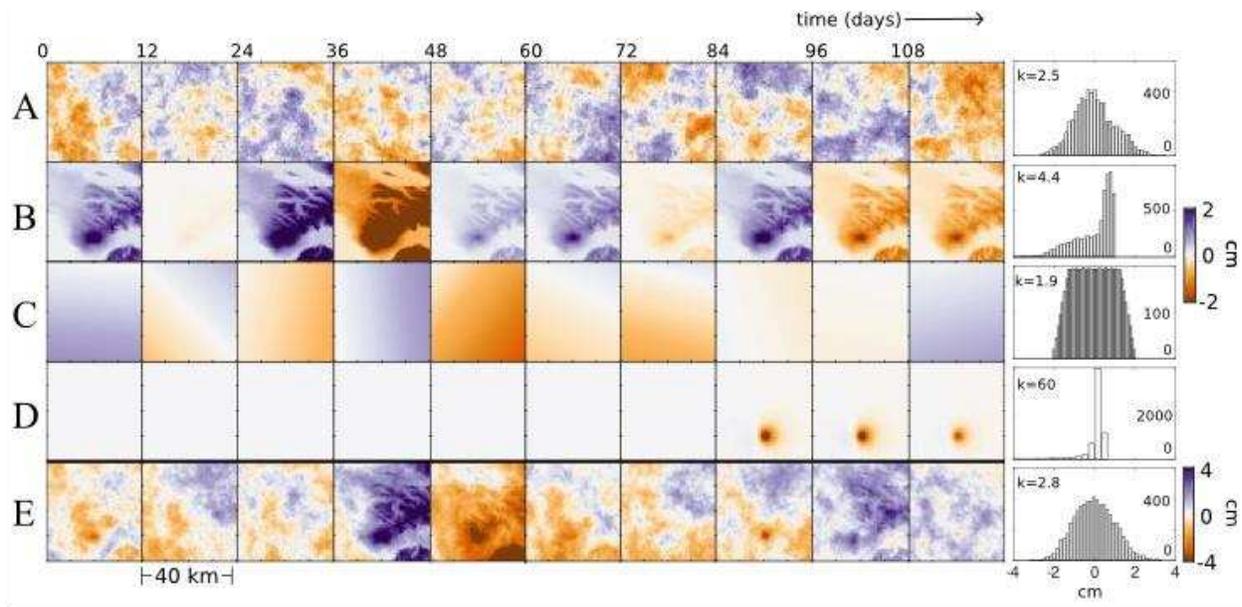
## 316 **3.0 Results**

### 317 **3.1 Tests with synthetic data**

318 I constructed sets of simple synthetic interferograms with similar average properties to those  
319 derived from Sentinel-1 SAR data (Figure 3). These included an emulation of spatially  
320 correlated atmosphere (e.g., Hanssen, 2001; Lohman & Simons, 2005), troposphericly  
321 correlated atmospheric variations (e.g., Remy et al., 2003) and linear ramps (of the form  $ax + by$   
322  $+ c$ , where  $a \sim b \sim 0.01 \text{ km}^{-1}$ ) representing errors in the estimation of orbits). I used central values  
323 of maximum variance =  $20 \text{ mm}^2$  and characteristic length scale exponent = 0.5, after Emardson  
324 et al., (2003), and assumed a normal distribution to randomly generate spatially correlated  
325 atmosphere for each synthetic image. Sample SRTM topography of footprint  $1600 \text{ km}^2$ ,  
326 encompassing Osorno volcano (2652 m, Southern Chile), was used to generate stratified  
327 atmospheric signals with an average phase delay gradient of  $1 \text{ cm/km}$  (e.g., Bekaert et al., 2015).  
328 Interferogram phase screens were then estimated by adding together the spatially and  
329 topographically correlated atmospheric phase for each image and differencing sequential images.  
330 Orbital contributions and a synthetic line-of-sight deformation signal were then added to each  
331 interferogram.

332 Synthetic deformation patterns were constructed by evaluating a Mogi model at 5 km depth in an  
333 elastic half-space for (a) a linear increase in source volume over time, (b) sinusoidal variations in  
334 source volume (c) a 'pulsed' episode of source deflation spanning just a few interferograms ( $< 1$   
335 month), and (d) a 'step' in deformation captured in just one interferogram. A Mogi source  
336 (Mogi, 1958) was selected for simplicity, and because it provides a reasonable first order  
337 approximation of a variety of time-varying deformation sources including  
338 magmatic/hydrothermal reservoirs or the withdrawal of groundwater. The deformation source  
339 was located beneath the topography for Osorno volcano, with a second deformation source  
340 located northwest of the volcano for some tests.

341 The final synthetic data therefore consists of a set of 'daisy chain' interferograms of  $40 \times 40 \text{ km}$   
342 dimensions,  $\sim 500 \text{ m}$  pixel size (to limit computation time) and 12-day separation, referenced to  
343 the first image acquisition time (Figure 3). These synthetic data are simpler than real  
344 interferograms and do not include, for example, non-linear phase-topography gradients,  
345 quadratic orbital ramps or any loss in image coherence. However, they do capture the primary  
346 features of an InSAR dataset sufficiently well to test the applicability of ICA for source  
347 separation.



348

349 **Figure 3:** The signals used to construct a set of synthetic interferograms. (A) Spatially  
 350 correlated atmospheric phase contribution, (B) Topographically correlated atmospheric delay (C)  
 351 Linear orbital ramps of the form  $\varnothing = ax + by + c$ , where  $a$  and  $b$  are normally distributed randomly  
 352 generated numbers with central values of  $\sim 0.01$ . (D) Synthetic deformation – in this case a Mogi  
 353 source at 5km depth, on short-lived episode of inflation starting on day 75. (E) Synthetic  
 354 interferograms, from the sum of signals A to D. Histograms show the distribution of values for  
 355 the last interferogram in the sequence (days 108-120).

356 I applied the ICA methodology described above to examine the impact of varying (1) the number  
 357 of synthetic interferograms used as input data (2) signal to noise ratio of the deformation source  
 358 and (3) temporal characteristics of the deformation source. Tests using temporal rather than  
 359 spatial ICA were conducted on downsampled versions of the same synthetic data of 20 by 20  
 360 pixels (size 2km), to reduce the size of the covariance matrix it was necessary to estimate. To  
 361 test the significance of the independent components retrieved using the clustering method  
 362 described above (Section 2.2), synthetic datasets with the same deformation sources, but  
 363 different random noise, were produced in pairs.

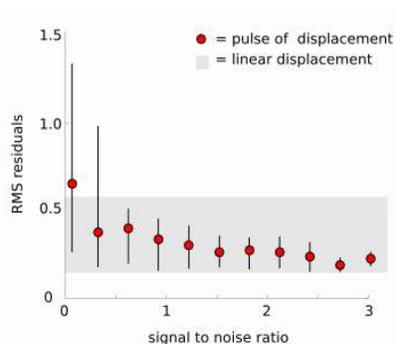
364 The success of ICA in analysing the synthetic InSAR data can be assessed for two different aims.  
 365 First, the ICs should capture the spatial and temporal characteristics of the input signals  
 366 sufficiently well for them to be useful in exploring the development of and relationships between  
 367 different deformation signals. I use the clustering method for identifying real sources (described  
 368 in Section 2.2) as a test for whether ICs contain useful information. A second aim is the accurate

369 reconstruction of the original input deformation signal in a form suitable for modelling. Such  
 370 reconstruction will be most successful when input sources are very non-Gaussian. The presence  
 371 of Gaussian noise and correlations between input signals in space (sICA) or time (tICA) result in  
 372 signals caused by different processes being captured in the same independent components and  
 373 introduce noise to any reconstructed interferograms.

374 Clusters containing the ICs that captured the spatial pattern of input deformation were identified  
 375 from sICA for even very small synthetic datasets (<5 interferograms). For tICA, clusters  
 376 capturing input deformation patterns were most reliably identified for larger datasets (>20  
 377 interferograms). For small sample sizes (i.e., 10s of interferograms, relative to 10,000s of pixels)  
 378 ICA algorithms are less stable, and if too many principal components are retained, also prone to  
 379 overfitting.

380 For all the different input deformation styles, clusters of ICs were identified for signal to noise  
 381 ratio (SNR)  $> 0.1$ . For lower signal to noise ratios, deformation was sometimes removed during  
 382 dimension reduction before performing the ICA. Deformation was only lost at very low SNR  
 383 for sICA, where usually only the smallest eigenvector had been removed. As dimension  
 384 reduction is a more important prerequisite to tICA, the successful identification of clusters was  
 385 more sensitive to SNR, and for the examples examined here, was more successful at  $\text{SNR} > 0.5$ .

386 The residuals between interferograms reconstructed from the clustered component and the  
 387 original input deformation are also sensitive to SNR for some types of deformation. Figure 4  
 388 illustrates the variation of root mean square (RMS) residuals in relation to the SNR of the  
 389 synthetic data for sICA (SNR is approximated as the ratio of maximum deformation to maximum  
 390 noise). For a pulse of deformation, RMS residuals level out to a value of  $\sim 0.2$  cm at  $\text{SNR} > 1$ , but  
 391 are three times higher where  $\text{SNR} < 1$ . For linear displacements, RMS residuals vary across a  
 392 range of almost  $\sim 0.5$  cm without obvious dependence on input SNR.



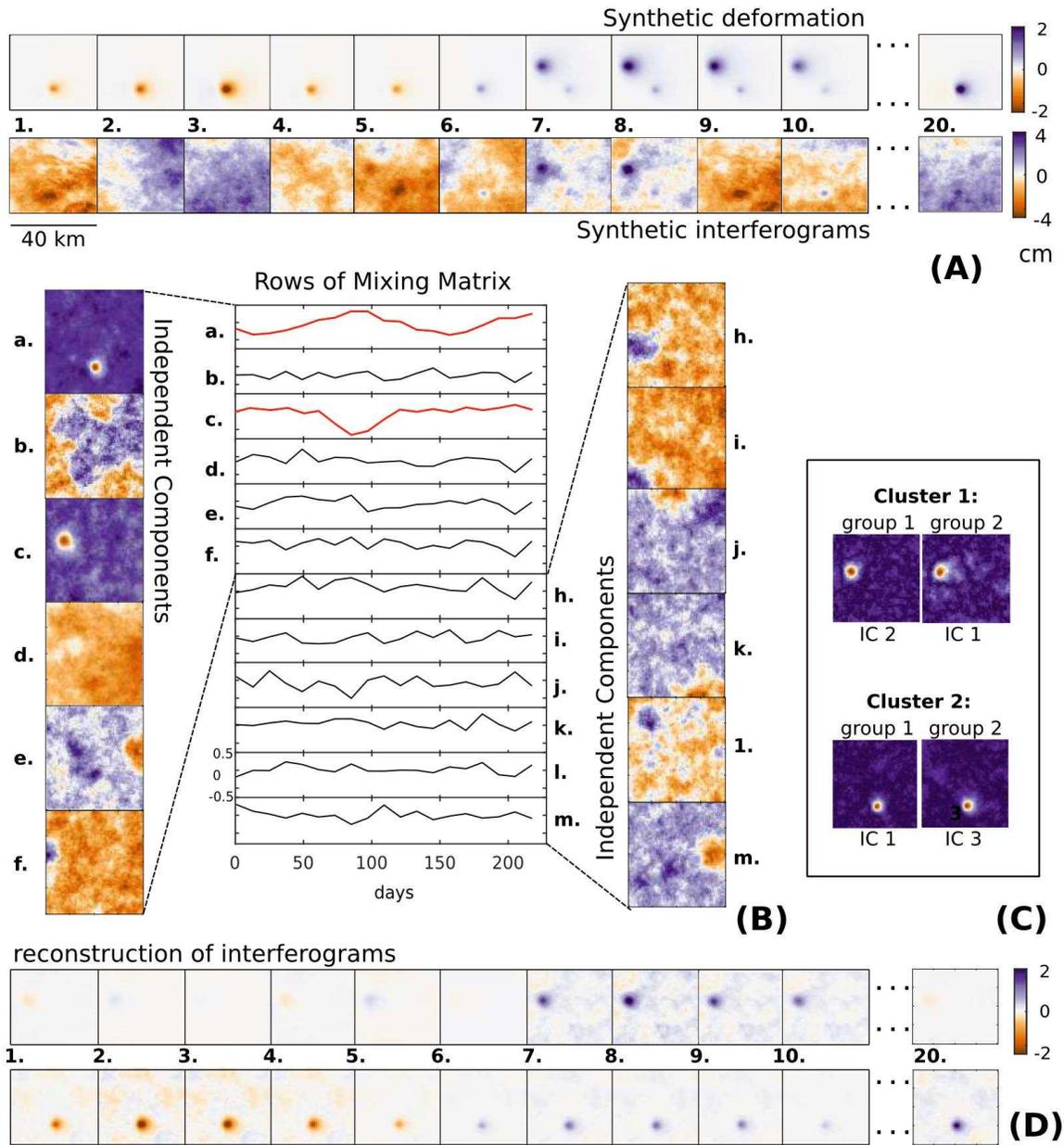
**Figure 4:** Variation of root mean square (RMS) residuals (cm) in relation to the SNR of the input synthetic data for interferograms reconstructed from a single IC identified by sICA.

398

399

400 Identical deformation sources or those where the volume change of one source was a function of  
401 the other in time (i.e. coupled sources), were retrieved in the same independent component,  
402 provided episodes of deformation were sufficiently long relative to the satellite repeat time (e.g.,  
403 appeared in >2 interferograms). Deformation events limited to just one interferogram always  
404 appear to be independent of other sources. Independent deformation sources, such as the  
405 example shown in Figure 5A, were retrieved as separate components (Figure 5B), making it  
406 possible to separate them into different sets of reconstructed interferograms (Figure 5D).

407 For paired groups of synthetic interferograms (same deformation source characteristics with  
408 randomly generated atmospheric and orbital sources) inter-group clusters of components  
409 consistently retrieve the input deformation (e.g., clusters shown in Figure 5C). However, when  
410 the look angle is changed for the two different groups to represent a comparison of ascending  
411 and descending data, then statistically significant inter-group clusters are only found for near  
412 vertical deformation, as the horizontal components of displacement seen by the satellite are more  
413 sensitive to look angle. For the synthetic data used here, independent components containing  
414 atmospheric features were also assigned to clusters in about 10% of cases, normally where  
415 synthetic interferograms were dominated by topographically correlated atmospheric delay.  
416 These false positives present a challenge for automation, but were easily identified by eye and  
417 may be the result of the simple representation of atmospheric signals in the synthetic data.



418

419 **Figure 5:** Illustration of workflow for analysis of a synthetic set of interferograms capturing two  
 420 independent deformation sources. (A) Synthetic deformation for a Mogi-type source at 5km  
 421 depth with sinusoidal variations in volume (lower source) and a second source at 7 km depth  
 422 inflating for ~ one month (upper source in time steps 7-10). Synthetic interferograms include  
 423 atmospheric and orbital contributions as well as deformation, and are expressed in terms of  
 424 satellite line-of-sight displacement. (B) Independent spatial components of the set of  
 425 interferograms, shown with letters to match the corresponding rows of the mixing matrix, which  
 426 show the contribution of each spatial component to each interferogram in the synthetic data set.  
 427 (C) Clusters of independent components from the analysis shown in (B) and a similar set of  
 428 randomly generated interferograms. The p-values for the components being parts of the same

429 cluster are 0.8 and 0.7 for sources 1 and 2, respectively. (D) Reconstruction of interferograms  
430 showing the two independent synthetic deformation sources identified from cluster analysis,  
431 calculated as the outer product of the relevant rows of the mixing and sources matrices.

432

## 433 **3.2 Application to Volcanic displacements with Sentinel-1 SAR data**

434 I used interferograms spanning two recent periods of contrasting volcanic deformation from the  
435 archive of Sentinel-1a imagery to investigate the applicability of ICA. Given that Sentinel-1 will  
436 provide the largest, freely available SAR dataset over the coming decades, it provides the most  
437 useful test for the applicability of ICA to real data. Volcanic deformation is a reasonable ‘proof-  
438 of-concept’ test, because deformation rates were in both cases high enough to be detectable in  
439 the 18 months of imagery acquired since Sentinel-1A’s launch in 2014. The two examples  
440 investigated represent end-members for temporal characteristics of volcano deformation  
441 detectable using InSAR. The only deformation to have been detected at Calbuco volcano, Chile,  
442 was during an eruption in April 2015, while lava flows at Parícutin, Mexico have been subsiding  
443 steadily for decades. Subsidence at Calbuco was high in magnitude (~12 cm), clearly  
444 identifiable in a single interferogram, and therefore provides a clear illustration of how ICs  
445 representing deformation can be identified. In contrast, deformation is not immediately obvious  
446 in any one individual interferograms from Parícutin, but can be identified from the products of  
447 ICA.

448

### 449 **3.2.1 Data processing and preparation**

450 SAR images from the European Commission's Sentinel-1A satellite were used to construct a set  
451 of interferograms over two volcanoes (Parícutin, Mexico and Calbuco, Chile) and processed  
452 using GAMMA software ([www.gamma-rs.ch](http://www.gamma-rs.ch)). Images were acquired in Terrain Observation by  
453 Progressive Scans (TOPS) mode and co-registration of master and slave single-look complex  
454 images was achieved by iterative estimation of constant range and azimuth offsets from cross-  
455 correlation and then from Doppler variation in burst overlap regions (e.g., González et al., 2015).  
456 Topographic phase contributions were corrected using Shuttle Radar Topography (SRTM)  
457 mission 30 m data (Farr et al., 2007). Interferograms were unwrapped using a minimum cost

458 flow method and were processed at 12 and 2 looks in range and azimuth respectively to give a  
459 pixel size of approximately 30 m.

### 460 **3.2.2 Co-eruptive subsidence at Calbuco, Chile**

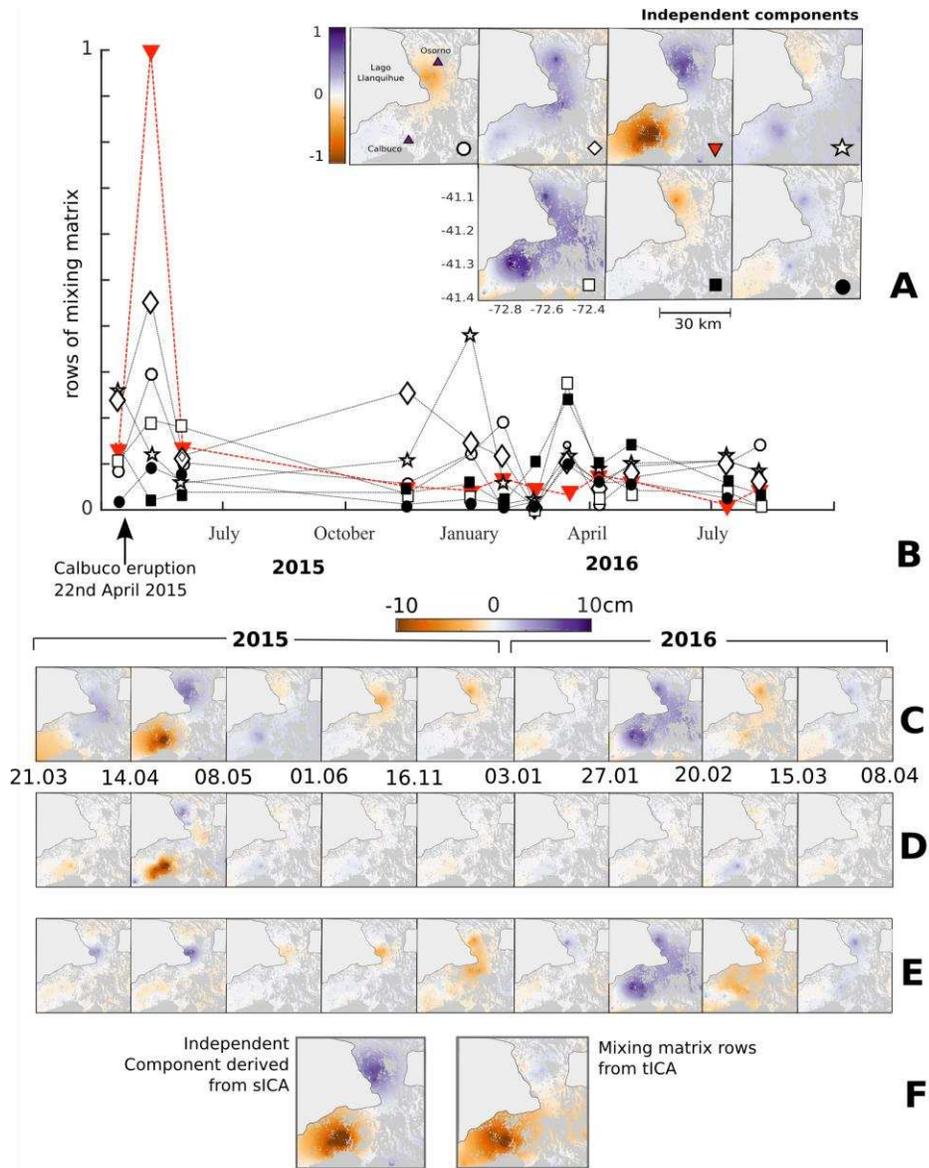
461 Calbuco volcano in Southern Chile erupted on 22<sup>nd</sup> April 2015, 54 years after its last major  
462 eruption. The ash plume reached heights of up to 18 km and ejected  $\sim 4.5 \pm 2.3 \times 10^{11}$  kg tephra  
463 (Romero et al., 2016; Van Eaton et al., 2016). No deformation was detected in the weeks before  
464 the onset of the eruption in Sentinel-1A InSAR data, or during regional InSAR surveys that  
465 covered the Southern Andes between 2006 and 2010 (Fournier et al., 2010; Pritchard et al.,  
466 2013). Interferograms from three separate tracks do capture co-eruptive subsidence of  $\sim 12$  cm,  
467 which appears to have occurred only during the first two phases of the eruption on the 22<sup>nd</sup> - 23<sup>rd</sup>  
468 April. Here, I use daisy-chain Sentinel-1 interferograms from a single track (164) that spans the  
469 Calbuco eruption. The timespan of most interferograms is 24 days, but there was a significant  
470 gap in acquisitions between June and November 2015 that resulted in one interferogram  
471 spanning 168 days.

472 Spatial ICA was performed on a subset of the Sentinel-1A interferograms of dimensions  $\sim 50 \times$   
473 50 km. Twelve interferograms (Supplementary Table 1) were used in the analysis and the data  
474 dimensions were reduced to ten during preparation and whitening. No atmospheric corrections  
475 or temporal filtering was performed on the dataset before application of ICA. To use tICA on  
476 the same data, I downsampled the same subset by a factor of ten to ease computation time and  
477 similarly reduced the dimension of the data to ten during whitening.

478 A selection of independent spatial components and mixing matrix rows from the sICA analysis  
479 are shown in Figure 6, with the one associated with co-eruptive deformation marked by a red  
480 triangle. Note that this IC also captures an atmospheric feature at Osorno volcano. Other  
481 components are consistent with topographically correlated atmospheric signals, for example, the  
482 black circle or the white square on Figures 6 A and B, which show signals associated with both  
483 Osorno and Calbuco volcanoes and contribute to the phase observed in many of the  
484 interferograms. The mixing matrix rows (Figure 6B) show the relative contributions of the  
485 spatial components to each interferogram in the analysis.

486 As deformation only appears in one of the sequential daisy-chain interferograms, the  
487 interferograms were reconstructed to create two independent groups without any acquisition  
488 dates in common, so that each group included one interferogram that spanned the eruption  
489 (group 1: 20150321-20150508 and group 2: 20150414-20150601). The ICs containing the  
490 deformation from the two groups were identified as a cluster ( $p$ -value=0.76).

491 Interferograms containing just the components associated with deformation were reconstructed  
492 by taking the outer product of the relevant mixing and source matrix rows. These reconstructed  
493 interferograms (Figure 6D), are dominated by the co-eruptive subsidence in the interferogram  
494 that spanned the 22<sup>nd</sup> - 23<sup>rd</sup> April eruption, although there is also some residual noise spread  
495 through the other reconstructed interferograms. This noise gives an indication of the expected  
496 level of uncertainty in the reconstruction of the co-eruptive deformation field (<2 cm), and is  
497 much lower than the variance of the interferograms reconstructed from the remaining  
498 components (Figure 6E, ~ 5.5cm). The spatial patterns associated with co-eruptive deformation  
499 derived from sICA and tICA are compared in Figure 6F. They are similar (but not identical)  
500 over Calbuco, but quite different over Osorno volcano.



501

502 **Figure 6:** (A) Selection of independent components from ICA of a set of twelve interferograms  
 503 spanning the time between 21st March 2015 and 6th August 2016 (505 days) over Calbuco  
 504 volcano, Chile. Colors are scaled between -1 and 1 for presentation. (B) Mixing matrix rows for  
 505 the components shown in part A, plotted against the 'slave' date of each interferogram, and scaled  
 506 between 0 and 1. Each point shows the relative contribution of the corresponding spatial pattern  
 507 shown in A to a single interferogram in the data set. (C) Interferograms used for the analysis  
 508 (first nine of the full set of twelve). Numbers below show the date of the master image for the  
 509 reconstructed interferogram to the right (dd.mm) (D) Interferograms reconstructed from the  
 510 independent spatial components and mixing matrix rows identified as deformation. (E)  
 511 Interferograms reconstructed from the independent spatial components and mixing matrix rows  
 512 not associated with deformation, and instead considered to be dominated by atmospheric  
 513 features. (F) Comparison of spatial patterns of the independent spatial component (from sICA)  
 514 and the mixing matrix row (from tICA).

### 515 3.2.3 Lava subsidence of the Parícutin lava fields

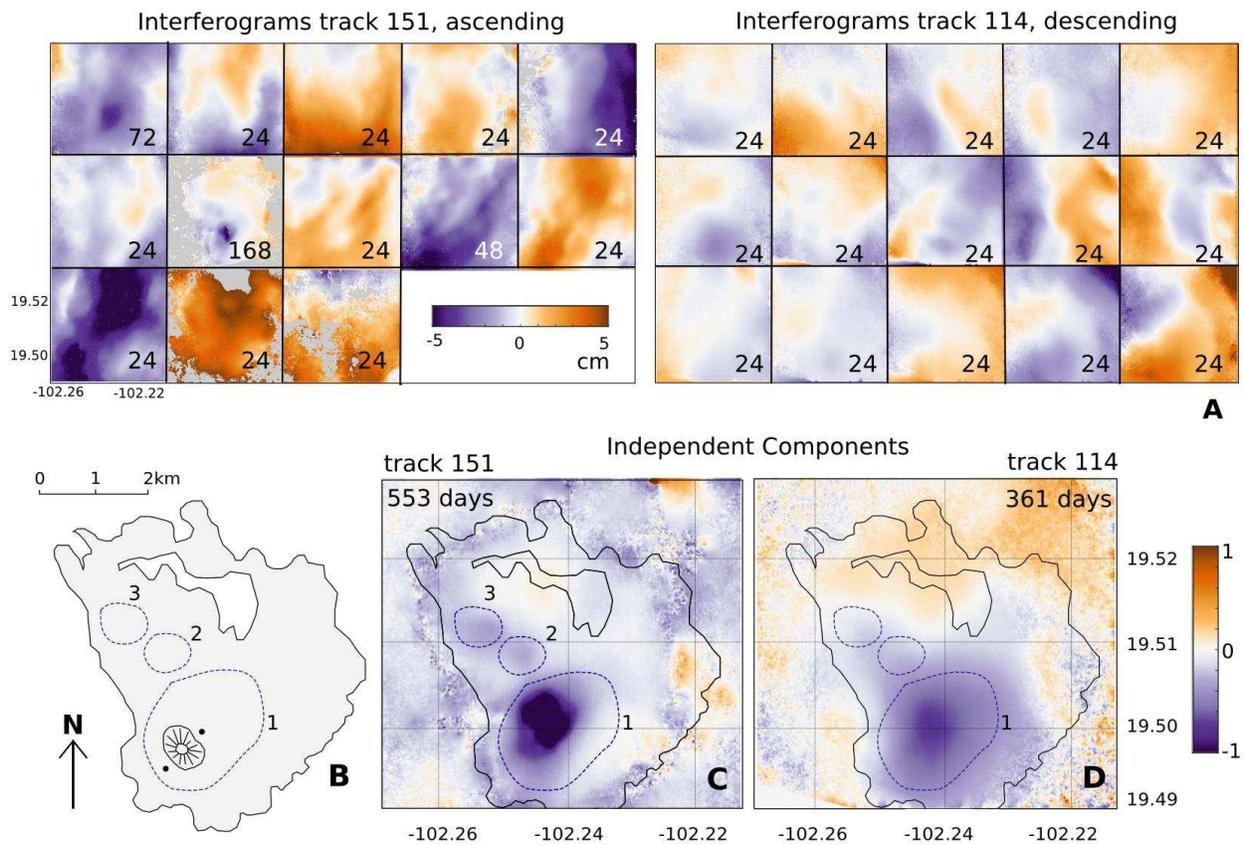
516 In 1943 a new monogenetic cone, Parícutin, appeared in a cornfield in the Michoacán-  
517 Guanajuato volcanic field in central Mexico. Over the next 9 years 1.9 km<sup>3</sup> (Fries, 1953) of  
518 basaltic-andesitic lavas and pyroclastic products were deposited over an area of ~ 25 km<sup>2</sup> in  
519 around 40 separate lava flows with a total thickness exceeding 200 m. The Parícutin lava flows  
520 have now been subsiding for over 60 years and past InSAR observations up to 2011 detected  
521 linear subsidence at a rate of up to ~5 cm/yr (Fournier et al., 2010; Chaussard et al., 2016). Lavas  
522 were erupted from a cinder cone onto what had previously been gently sloping farmland, so in  
523 this case deformation signals are not expected to be strongly correlated with topography.

524 I performed sICA on interferograms from both ascending and descending tracks of Sentinel-1A  
525 imagery (Supplementary Table 1) to test whether the already well-characterized spatial patterns  
526 of deformation are captured as an independent component. For both data sets the number of  
527 dimensions were reduced during preconditioning to one less than the number of interferograms,  
528 and the same number of independent components were retrieved. The usefulness of ICA was  
529 tested at two scales, first for a subset of the interferogram 40 x 40 km, and second for a smaller  
530 subset (~5 km x 5km) over the lavas themselves. Although lava subsidence can be identified in  
531 one of the independent components estimated from the 40 x 40 km subset, their spatial patterns  
532 are seen more clearly in the 5 x 5 km extract shown in Figure 7. Although lava subsidence is  
533 not clearly visible in many of the input interferograms due to the relatively low signal to noise  
534 ratio in any single time period (Figure 7A), both tracks of data are decomposed to produce an  
535 independent component with a spatial pattern that closely matches patterns of lava subsidence  
536 described by other authors (Figure 7B). Specifically, the signal maximum appears in the same  
537 location (~-102.242°, 19.499°) in components from both ascending and descending datasets  
538 (Figure 7 C and D), and in the same location as where Chaussard (2016) measured maximum  
539 subsidence over the thickest part of the 1943-52 lava flow. Furthermore, three distinct patches of  
540 subsidence are captured in the same independent component from the ascending (151) track of  
541 data, and are associated with a less distinct patch in the descending (114) data. The three signal  
542 patches are caused by the same physical process (the cooling and compaction of lavas emplaced  
543 >60 years ago), which is consistent with them being retrieved within the same independent  
544 component. The differences in the deformation retrieved from the two tracks are primarily due

545 to the differences in their total temporal coverage (i.e. lower magnitude deformation is detected  
546 only over a longer period).

547 By separating the Paricutin data for each track into two independent groups, I tested whether the  
548 component containing the deformation could be identified automatically. As we can expect lava  
549 subsidence so long after emplacement to have a constant rate over the 1.5 years over which  
550 Sentinel-1A acquired data, I divided the interferograms into two sequential groups, removing the  
551 midpoint interferogram so that the groups did not hold any acquisition dates in common. The  
552 central long-period 168-day interferogram was also removed from the analysis of track 151 so  
553 that it did not dominate the independent components retrieved. Although no clusters between the  
554 two independent groups were identified with the desired confidence (false positive rate for the  
555 existence of a cluster, and false discovery rate of an independent component belonging to a  
556 cluster set to  $<5\%$ , after Hyvärinen & Ramkumar, 2013), the pair of components with the  
557 greatest probability ( $p=0.5$ ) of capturing the same feature were those with the same spatial  
558 pattern as the lava subsidence (the two independent components identified as a cluster for track  
559 151 are shown in Supplementary Figure 1). Although the lava flow subsidence is not clear in any  
560 of the interferograms spanning  $<100$  days, ICA is able to retrieve the largest displacement signal  
561 from both tracks of images, and even the smaller, lower magnitude lobes of subsidence in the  
562 ascending track, which spanned a longer time period.

563 I reconstructed interferograms from the ascending track IC that captures the lava subsidence field  
564 and estimated a linear subsidence rate from the total cumulative displacement over the whole  
565 time period. Region 1 (Figure 7B) is subsiding at  $5.3\text{ cm/yr} \pm 0.5$  (in line-of-sight), with the  
566 uncertainty taken as the variance of the reconstructed interferograms in areas away from the lava  
567 fields. This is close to the value of  $5.5\text{ cm/yr}$  found by Chaussard et al., (2016) between 2007  
568 and 2011. Estimations of the rate of subsidence for the two smaller patches are, however, slower  
569 than previous measurements, being  $1.5\pm 0.5\text{ cm/yr}$  2014-2016 relative to  $3.3\text{ cm/yr}$  2007-2011.



570

571 **Figure 7:** (A) Interferograms used in ICA analysis of InSAR signals over Parícutin lava fields  
 572 from ascending and descending tracks of Sentinel-1A data (numbers in corners refer to number  
 573 of days spanned by the interferogram). (B) Spatial extent of Parícutin lava fields (in grey, after  
 574 Chaussard, 2016) with the location of deformation measured in ALOS interferograms (2007-  
 575 2011) indicated by blue dashed outlines. The location of the cinder cone built up between 1943  
 576 and 1952 is marked along with two secondary eruptive vents (black circles). (C) Spatial pattern  
 577 of an independent component capturing lava subsidence found from spatial ICA of 13 Sentinel  
 578 interferograms (track 151, ascending) spanning the period between 27th December 2014 and 1st  
 579 July 2016. (D) Spatial pattern of an independent component capturing lava subsidence found  
 580 from spatial ICA of 15 interferograms (track 114, descending) spanning the period between 29th  
 581 May 2015 and 23rd May 2016. As the magnitudes of independent components are arbitrary  
 582 (e.g., Hyvärinen & Oja, 2000), they are scaled here between 1 and -1 for presentation purposes.

583

584

585

**586 Discussion**

587 ICA has potential as a tool for exploratory analysis of InSAR datasets, automatically identifying  
588 displacements, assessing the relationships between deformation signals, and in some  
589 circumstances, for separating displacements from atmospheric noise. It is likely to be  
590 particularly useful for interrogating the large volumes of satellite radar imagery now available  
591 for monitoring geophysical signals.

592 As an analysis tool, ICA will be particularly useful, where a priori information about  
593 deformation location or temporal characteristics is limited. Deformation sources that do not  
594 share a causal mechanism are likely to result in independent displacement patterns, and as such  
595 will be decomposed into separate ICs. In contrast, deformation related to the same physical  
596 process will be captured by the same IC, as seen at the Parícutin lavas, where three separate  
597 patches of subsidence appear in the same independent component (Figure 7 C-D).

598 Exploratory analysis requires a reliable method for assessing the statistical significance of the  
599 ICs. I found that cluster analysis of ICs from different groups was reliable for automatically  
600 extracting the IC related to input deformation from tests with synthetic data at  $\text{SNR} > 0.1$ . The  
601 ICs associated with lava subsidence at Parícutin had the highest probability ( $p=0.5$ ) of being an  
602 inter-group cluster for two groups of 6-7 interferograms, as did the ICs that capture co-eruptive  
603 deformation at Calbuco ( $p=0.76$ ). Although the examples presented here are both volcanic, a  
604 very similar approach could be used to analyze deformation associated with tectonic or  
605 anthropogenic processes, landsliding or for searching for transient events, such as small  
606 earthquakes, or seasonal hydrological loading. Separating otherwise similar interferograms into  
607 independent groups requires redundancy in the number of satellite acquisitions and will be most  
608 successful where either deformation is constant and long-lived relative to satellite repeat time (of  
609 days), or coherence is sufficiently good to allow multiple (probably longer time-span)  
610 interferograms to be formed over the period of interest. An alternative method may be to look  
611 for correlations between independent components retrieved from recent interferograms and either  
612 past deformation signals or the a priori expected location of deformation. Qualitative  
613 comparison of ICs retrieved from sICA and tICA of the same datasets may also be useful,

614 although the properties of ICs that are independent in space versus independent in time may be  
615 different (e.g., as at Calbuco, Figure 6F).

616 For the mitigation of atmospheric artefacts, predictive methods are theoretically preferable to  
617 empirical approaches, such as ICA. However, as their efficacy depends on the density and  
618 quality of independent atmospheric data available, or the resolution and initial conditions of an  
619 atmospheric model, there are some situations where an empirical approach is likely to provide  
620 better results. ICA may also be suitable for initial ‘quick-look’ analyzes of large datasets before  
621 atmospheric data or higher resolution models can be prepared. At Calbuco, for example, it was  
622 possible to remove much of the atmospheric signal from the time series with sICA without the  
623 use of any independent atmospheric data, although the discrepancy between spatial patterns  
624 extracted with sICA and tICA suggests that some contribution from topographically correlated  
625 atmosphere is likely to remain. An additional application of sICA could be the identification and  
626 removal of quasi-systematic features in phase, not directly correlated with topography, but  
627 associated with regular meteorological patterns (e.g., as observed at Medicine Lake, Parker et al.,  
628 2015). ICA is a complementary approach to temporal filtering, which can be done as a  
629 preparatory step (e.g., Hyrärinen & Oja, 2000). It is also more flexible than spatiotemporal  
630 filtering for the identification (and potentially extraction) of short-lived deformation signals  
631 captured in just a few interferograms (e.g., Section 3.2.2).

632 Deformation that is spatially correlated with atmospheric signals, for example at steep, isolated  
633 volcanoes, could potentially result in both features being encompassed in the same spatial IC.  
634 However, stratified water vapour signals are normally spread throughout an interferogram rather  
635 than limited specifically to the location of deformation, and as such are part of a broad (if  
636 discontinuous) spatial pattern. For example, atmospheric signals at Calbuco are commonly  
637 accompanied by similar signals at neighbouring Osorno, and are decomposed into the same IC  
638 (Figure 6). However, deformation captured by only a single interferogram in a time series (as at  
639 Calbuco) is particularly challenging to separate from tropospheric atmospheric features based on  
640 either spatial or temporal independence, and ICs from both approaches contain contributions  
641 from atmospheric signals (Figure 6F).

642 ICA generally requires the assumption that no more than one of the independent components can  
643 be Gaussian, because any orthogonal transformation of independent Gaussian variables will have  
644 the same multivariate distribution (e.g., Hyvärinen & Oja, 2000). Where atmospheric signals are  
645 likely to have a Gaussian distribution in space or more likely in time, adaptations to the  
646 methodology presented here (e.g., Beckmann & Smith, 2004) could improve the quality of the  
647 results. Further advances in ICA methodology that can be applied to InSAR data include the  
648 simultaneous maximization of spatial and temporal independence and the use of skewed rather  
649 than symmetrical probability density functions (e.g., Stone et al., 2002).

650

## 651 **Conclusions**

652 ICA is an appropriate and useful method for the analysis of multi-temporal InSAR data, and  
653 especially for the exploratory analysis of geophysical signals.

654 Tests with synthetic interferograms indicate that the characteristics of input deformation sources  
655 can be retrieved by maximising either the spatial or temporal independence of source  
656 components, and that independent deformation sources are extracted into separate components.  
657 By splitting input data into two independent groups, the source component containing  
658 deformation can be identified automatically using cluster analysis. This allows for the automatic  
659 identification, and potentially also reconstruction, of deformation.

660 Co-eruptive deformation over Calbuco (Chile) in April 2015 was identifiable in the spatial  
661 patterns derived from both spatial and temporal ICA of twelve Sentinel interferograms, although  
662 there were differences between the two approaches. Atmospheric contributions were reduced in  
663 interferograms reconstructed from the spatial component containing deformation, but were not  
664 removed entirely. In particular, the spatial component describing deformation probably  
665 encompassed some signals associated with topographically correlated atmosphere.

666 Analysis of 29 Sentinel-1A interferograms over Parícutin lava flows (Mexico) using sICA  
667 captures the shape of three distinct patches of lava subsidence as part of the same spatial  
668 component, consistent with deformation caused by a common process. Lava subsidence rates

669 estimated from the reconstructed signal are consistent with previous InSAR measurements of  
670 deformation.

671 These prototype examples demonstrate that the combination of ICA and cluster analysis is  
672 appropriate for the analysis of InSAR data and that it has potential for (1) identifying  
673 geophysical signals caused by tectonic, volcanic or anthropogenic processes and (2) testing the  
674 independence of geophysical signals.

675

## 676 **References**

677 Amato, U., Antoniadis, A., Cuomo, V., Cutillo, L., Franzese, M., Murino, L., & Serio, C. (2008).  
678 Statistical cloud detection from SEVIRI multispectral images. *Remote Sensing of Environment*,  
679 112(3), 750-766. doi:10.1016/j.rse.2007.06.004

680 Barnie, T., & Oppenheimer, C. (2015). Extracting High Temperature Event radiance from  
681 satellite images and correcting for saturation using Independent Component Analysis. *Remote*  
682 *Sensing of Environment*, 158, 56-68. doi:10.1016/j.rse.2014.10.023

683 Bayliss, J. D., Gualtieri, J. A., & Crompton, R. F. (1998, March). Analyzing hyperspectral data with  
684 independent component analysis. In *26th AIPR Workshop: Exploiting New Image Sources and*  
685 *Sensors* (pp. 133-143). International Society for Optics and Photonics. doi:10.1117/12.300050

686 Beckmann, C. F., & Smith, S. M. (2004). Probabilistic independent component analysis for  
687 functional magnetic resonance imaging. *IEEE transactions on medical imaging*, 23(2), 137-152.  
688 doi:10.1109/TMI.2003.822821

689 Bekaert, D. P. S., Hooper, A., & Wright, T. J. (2015). A spatially variable power law  
690 tropospheric correction technique for InSAR data. *Journal of Geophysical Research: Solid Earth*,  
691 120(2), 1345-1356. doi:10.1002/2014JB011558

692 Bell, A. J., & Sejnowski, T. J. (1995). An information-maximization approach to blind  
693 separation and blind deconvolution. *Neural computation*, 7(6), 1129-1159.  
694 doi:10.1162/neco.1995.7.6.1129

- 695 Beauducel, F., Briole, P. and Froger, J.L., (2000). Volcano- wide fringes in ERS synthetic  
696 aperture radar interferograms of Etna (1992–1998): Deformation or tropospheric effect?. *Journal*  
697 *of Geophysical Research: Solid Earth*, 105(B7), pp.16391-16402.
- 698 Biggs, J., Ebmeier, S. K., Aspinall, W. P., Lu, Z., Pritchard, M. E., Sparks, R. S. J., & Mather, T.  
699 A. (2014). Global link between deformation and volcanic eruption quantified by satellite  
700 imagery. *Nature communications*, 5. doi:10.1038/ncomms4471
- 701 Bürgmann, R., Rosen, P. A., & Fielding, E. J. (2000). Synthetic aperture radar interferometry to  
702 measure Earth's surface topography and its deformation. *Annual review of earth and planetary*  
703 *sciences*, 28(1), 169-209. doi:10.1146/annurev.earth.28.1.169
- 704 Calhoun, V. D., & Adali, T. (2006). Unmixing fMRI with independent component analysis.  
705 *IEEE Engineering in Medicine and Biology Magazine*, 25(2), 79-90.  
706 doi:10.1109/MEMB.2006.1607672
- 707 Caricchi, L., J. Biggs, C. Annen, and S. K. Ebmeier (2014), The influence of cooling,  
708 crystallisation and re-melting on the interpretation of geodetic signals, *Earth and Planetary*  
709 *Science Letters* , doi:10.1016/j.epsl.2013.12.002
- 710 Chaussard, E. (2016). Subsidence in the Parícutin lava field: Causes and implications for  
711 interpretation of deformation fields at volcanoes. *Journal of Volcanology and Geothermal*  
712 *Research*, 320, 1-11. doi:10.1016/j.jvolgeores.2016.04.009
- 713 Comon, P. (1994). Independent component analysis, a new concept?. *Signal processing*, 36(3),  
714 287-314.
- 715 De Lauro, E., De Martino, S., Falanga, M., & Palo, M. (2009). Decomposition of high-frequency  
716 seismic wavefield of the Strombolian-like explosions at Erebus volcano by independent  
717 component analysis. *Geophysical Journal International*, 177(3), 1399-1406. doi:10.1111/j.1365-  
718 246X.2009.04157.x

- 719 Doin, M. P., Lasserre, C., Peltzer, G., Cavalié, O., & Doubre, C. (2009). Corrections of stratified  
720 tropospheric delays in SAR interferometry: Validation with global atmospheric models. *Journal*  
721 *of Applied Geophysics*, 69(1), 35-50.
- 722 Ebmeier, S. K., Biggs, J., Mather, T. A., & Amelung, F. (2013). Applicability of InSAR to  
723 tropical volcanoes: insights from Central America. *Geological Society, London, Special*  
724 *Publications*, 380(1), 15-37.
- 725 Ebmeier, S. K., J. Biggs, C. Muller and G. Avaré (2014). Thin-skinned mass-wasting responsible  
726 for edifice-wide deformation at Arenal Volcano, *Frontiers in Earth Science*, 2, 35,  
727 doi:10.3389/feart.2014.00035
- 728 Elliott, J. R., Biggs, J., Parsons, B., & Wright, T. J. (2008). InSAR slip rate determination on the  
729 Altyn Tagh Fault, northern Tibet, in the presence of topographically correlated atmospheric  
730 delays. *Geophysical Research Letters*, 35(12).
- 731 Elliott, J. R., Walters, R. J., and Wright, T. J. (2016) The role of space-based observation in  
732 understanding and responding to active tectonic and earthquakes. *Nature Communications*, Vol  
733 7. doi:10.1038/ncomms13844
- 734 Emardson, T. R., Simons, M., & Webb, F. H. (2003). Neutral atmospheric delay in  
735 interferometric synthetic aperture radar applications: Statistical description and mitigation.  
736 *Journal of Geophysical Research: Solid Earth*, 108(B5). doi:10.1029/2002JB001781
- 737 Esposito, F., Scarabino, T., Hyvarinen, A., Himberg, J., Formisano, E., Comani, S., Tedeschi, G.,  
738 Goebel, R., Seifritz, E. and Di Salle, F., 2005. Independent component analysis of fMRI group  
739 studies by self-organizing clustering. *Neuroimage*, 25(1), pp.193-205.  
740 doi:10.1016/j.neuroimage.2004.10.042
- 741 Farr, T. G., Rosen, P. A., Caro, E., Crippen, R., Duren, R., Hensley, S., ... & Seal, D. (2007). The  
742 shuttle radar topography mission. *Reviews of geophysics*, 45(2). doi:10.1029/2005RG000183
- 743 Ferretti, A., Prati, C. and Rocca, F., (2001). Permanent scatterers in SAR interferometry. *IEEE*  
744 *Transactions on geoscience and remote sensing*, 39(1), pp.8-20. doi: 10.1109/36.898661

- 745 Fournier, T. J., Pritchard, M. E., & Riddick, S. N. (2010). Duration, magnitude, and frequency of  
746 subaerial volcano deformation events: New results from Latin America using InSAR and a  
747 global synthesis. *Geochemistry, Geophysics, Geosystems*, 11(1). doi:10.1029/2009GC002558
- 748 Foster, J., Brooks, B., Cherubini, T., Shacat, C., Businger, S., & Werner, C. L. (2006). Mitigating  
749 atmospheric noise for InSAR using a high resolution weather model. *Geophysical Research*  
750 *Letters*, 33(16).
- 751 Foster, J., Kealy, J., Cherubini, T., Businger, S., Lu, Z., & Murphy, M. (2013). The utility of  
752 atmospheric analyzes for the mitigation of artifacts in InSAR. *Journal of Geophysical Research:*  
753 *Solid Earth*, 118(2), 748-758.
- 754 Fries, C. (1953). Volumes and weights of pyroclastic material, lava, and water erupted by  
755 Paricutin volcano, Michoacan, Mexico. *Eos, Transactions American Geophysical Union*, 34(4),  
756 603-616.
- 757 González, P. J., Tiampo, K. F., Palano, M., Cannavó, F., & Fernández, J. (2012). The 2011 Lorca  
758 earthquake slip distribution controlled by groundwater crustal unloading. *Nature Geoscience*,  
759 5(11), 821-825.
- 760 González, P.J., Bagnardi, M., Hooper, A.J., Larsen, Y., Marinkovic, P., Samsonov, S.V. and  
761 Wright, T.J., 2015. The 2014–2015 eruption of Fogo volcano: Geodetic modeling of Sentinel-1  
762 TOPS interferometry. *Geophysical Research Letters*, 42, 9239-9246.
- 763 Hanssen, R. F. (2001). *Radar interferometry: data interpretation and error analysis (Vol. 2)*.  
764 Springer Science & Business Media.
- 765 Henderson, S. T., & Pritchard, M. E. (2013). Decadal volcanic deformation in the Central Andes  
766 Volcanic Zone revealed by InSAR time series. *Geochemistry, Geophysics, Geosystems*, 14(5),  
767 1358-1374. doi:10.1002/ggge.20074
- 768 Hooper, A., Segall, P. and Zebker, H., (2007). Persistent scatterer interferometric synthetic  
769 aperture radar for crustal deformation analysis, with application to Volcán Alcedo, Galápagos.  
770 *Journal of Geophysical Research: Solid Earth*, 112(B7).

- 771 Hyvärinen, A., & Oja, E. (1997). A fast fixed-point algorithm for ICA. *Neural computation*, 9,  
772 1483-1492.
- 773 Hyvärinen, A., & Oja, E. (2000). Independent component analysis: algorithms and applications.  
774 *Neural networks*, 13(4), 411-430.
- 775 Hyvärinen, A., Karhunen, J., & Oja, E. (2004). Independent component analysis (Vol. 46). John  
776 Wiley & Sons.
- 777 Hyvärinen, A., J. Sarela, and Ricardo Vigário. "Spikes and bumps: Artefacts generated by  
778 independent component analysis with insufficient sample size." In First International Workshop  
779 on Independent Component Analysis and Signal Separation. 1999.
- 780 Hyvärinen, A. (2013). Independent component analysis: recent advances. *Phil. Trans. R. Soc. A*,  
781 371(1984), 20110534. doi:10.1098/rsta.2011.0534
- 782 Hyvärinen, A., & Ramkumar, P. (2013). Testing independent component patterns by inter-  
783 subject or inter-session consistency. *Frontiers in human neuroscience*, 7, 94.  
784 doi:10.3389/fnhum.2013.00094
- 785 Iwamori, H., & Albarède, F. (2008). Decoupled isotopic record of ridge and subduction zone  
786 processes in oceanic basalts by independent component analysis. *Geochemistry, Geophysics,*  
787 *Geosystems*, 9(4).doi:10.1029/2007GC001753
- 788 Jay, J., Costa, F., Pritchard, M., Lara, L., Singer, B., & Herrin, J. (2014). Locating magma  
789 reservoirs using InSAR and petrology before and during the 2011–2012 Cordón Caulle silicic  
790 eruption. *Earth and Planetary Science Letters*, 395, 254-266. doi:10.1016/j.epsl.2014.03.046
- 791 Jolivet, R., Agram, P. S., Lin, N. Y., Simons, M., Doin, M. P., Peltzer, G., & Li, Z. (2014).  
792 Improving InSAR geodesy using global atmospheric models. *Journal of Geophysical Research:*  
793 *Solid Earth*, 119(3), 2324-2341.
- 794 Jolivet, R., Grandin, R., Lasserre, C., Doin, M. P., & Peltzer, G. (2011). Systematic InSAR  
795 tropospheric phase delay corrections from global meteorological reanalysis data. *Geophysical*  
796 *Research Letters*, 38(17). doi:10.1029/2011GL048757

- 797 Mogi, K. (1958). Relations between the eruptions of various volcanoes and the deformations of  
798 the ground surfaces around them.
- 799 Parker, A. L., Biggs, J., Walters, R. J., Ebmeier, S. K., Wright, T. J., Teanby, N. A., & Lu, Z.  
800 (2015). Systematic assessment of atmospheric uncertainties for InSAR data at volcanic arcs  
801 using large-scale atmospheric models: Application to the Cascade volcanoes, United States.  
802 *Remote Sensing of Environment*, 170, 102-114.
- 803 Pinel, V., Poland, M. P., & Hooper, A. (2014). Volcanology: Lessons learned from synthetic  
804 aperture radar imagery. *Journal of Volcanology and Geothermal Research*, 289, 81-  
805 113.doi:10.1016/j.jvolgeores.2014.10.010
- 806 Pritchard, M.E., Jay, J.A., Aron, F., Henderson, S.T., Lara, L.E., 2013, Subsidence at southern  
807 Andes volcanoes induced by the 2010 Maule, Chile earthquake. *Nature Geoscience*, 6, 632-636.  
808 doi:10.1038/ngeo1855
- 809 Liu, B., Dai, W., Peng, W., & Meng, X. (2015). Spatiotemporal analysis of GPS time series in  
810 vertical direction using independent component analysis. *Earth, Planets and Space*, 67(1),  
811 1.doi:10.1186/s40623-015-0357-1
- 812 Lu, Z., & Dzurisin, D. (2014). InSAR Imaging of Aleutian Volcanoes. In *InSAR Imaging of*  
813 *Aleutian Volcanoes* (pp. 87-345). Springer Berlin Heidelberg. doi:10.1007/978-3-642-00348-6\_6
- 814 Massonnet, D., Rossi, M., Carmona, C., Adragna, F., Peltzer, G., Feigl, K., & Rabaute, T.  
815 (1993). The displacement field of the Landers earthquake mapped by radar interferometry.  
816 *Nature*, 364(6433), 138-142.
- 817 Poland, M. P., & Lu, Z. (2004). Radar interferometry observations of surface displacements  
818 during pre-and co-eruptive periods at Mount St. Helens, Washington, 1992–2005. A volcano  
819 rekindled: the renewed eruption of Mount St. Helens, 2006.
- 820 Remy, D., Bonvalot, S., Briole, P., & Murakami, M. (2003). Accurate measurements of  
821 tropospheric effects in volcanic areas from SAR interferometry data: Application to Sakurajima  
822 volcano (Japan). *Earth and Planetary Science Letters*, 213(3), 299-310.

- 823 Romero, J.E., Morgavi, D., Arzilli, F., Daga, R., Caselli, A., Reckziegel, F., Viramonte, J., Díaz-  
824 Alvarado, J., Polacci, M., Burton, M., Perugini, D., Eruption dynamics of the 22–23 April 2015  
825 Calbuco volcano (Southern Chile): Analyzes of tephra fall deposits, *Journal of Volcanology and*  
826 *Geothermal Research* (2016), doi:10.1016/j.jvolgeores.2016.02.027
- 827 Sigmundsson, F., Hooper, A., Hreinsdóttir, S., Vogfjörd, K. S., Ófeigsson, B. G., Heimisson, E.  
828 R. et al., (2015). Segmented lateral dyke growth in a rifting event at Bardarbunga volcanic  
829 system, Iceland. *Nature*, 517(7533), 191-195. doi:10.1038/nature14111
- 830 Stone, J. V., Porrill, J., Porter, N. R., & Wilkinson, I. D. (2002). Spatiotemporal independent  
831 component analysis of event-related fMRI data using skewed probability density functions.  
832 *NeuroImage*, 15(2), 407-421.
- 833 Stone, J. V. (2004). *Independent component analysis*. John Wiley & Sons, Ltd.
- 834 Van Eaton, A.R., Amigo, A., Bertín, D., Mastin, L.G., Giacosa, R., González, J., Valderrama, O.,  
835 Fontijn, K., Behnke, S.A. (2016). Volcanic lightning and plume behavior reveal evolving  
836 hazards during the April 2015 eruption of Calbuco Volcano, Chile. *Geophysical Research Letters*  
837 43, 3563-3571, doi: 10.1002/2016GL068076
- 838 Walters, R. J., Elliott, J. R., Li, Z., & Parsons, B. (2013). Rapid strain accumulation on the  
839 Ashkabad fault (Turkmenistan) from atmosphere- corrected InSAR. *Journal of Geophysical*  
840 *Research: Solid Earth*, 118(7), 3674-3690.
- 841 Wadge, G., Costa, A., Pascal, K., Werner, C., & Webb, T. (2016). The Variability of Refractivity  
842 in the Atmospheric Boundary Layer of a Tropical Island Volcano Measured by Ground-Based  
843 Interferometric Radar. *Boundary-Layer Meteorology*, 1-25. doi:10.1007/s10546-016-0168-3
- 844 Wicks, C. W., Dzurisin, D., Ingebritsen, S., Thatcher, W., Lu, Z., & Iverson, J. (2002). Magmatic  
845 activity beneath the quiescent Three Sisters volcanic center, central Oregon Cascade Range,  
846 USA. *Geophysical Research Letters*, 29(7).doi:10.1029/2001GL014205

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