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Thermodynamic interpolation for the simulation of two-phase flow of complex mixtures


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Abstract

This paper describes the development and application of a technique for the rapid interpolation of thermodynamic properties of mixtures for the purposes of simulating two-phase flow. The technique is based on adaptive inverse interpolation and can be applied to any Equation of State and multicomponent mixture. Following analysis of its accuracy, the method is coupled with a two-phase flow model, based on the homogeneous equilibrium mixture assumption, and applied to the simulation of flows of carbon dioxide (CO2) rich mixtures. This coupled flow model is used to simulate the experimental decompression of binary and quinternary mixtures. It is found that the predictions are in good agreement with the experimental data and that the interpolation approach provides a flexible, robust means of obtaining thermodynamic properties for use in flow models.

Keywords: Carbon dioxide transport, Two-phase flow, Equations of state, Pipeline safety

1. Introduction

The modelling of compressible two-phase or flashing flows is common place in a wide range of areas in engineering. For example, cavitation in automotive fuel injection systems (Martynov et al., 2006), flash boiling of water during loss-of-coolant accidents in nuclear reactors (Blinkov et al., 1993) and liquid boiling and expansion in refrigeration systems and heat pumps (Simões-Moreira and Bullard, 2003). Whilst various approaches are available to model the dynamics of two-phase flow, the accuracy of simulations for flashing two-phase flows to a large extent depends on the accuracy of

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the physical properties data in use. This particularly applies to multi-component mixtures, which are commonly found as working fluids in the above systems.

In practice, complex mathematical formulas known as Equations of State (EoS), are used to provide the thermodynamic properties for both vapour and liquid phases. As a result, a practical problem arises when pressure explicit EoS are coupled with flow models. In these EoS, the thermodynamic properties are predicted as a function of pressure, temperature and composition while phase equilibria, at a given system pressure and temperature (P-T), is determined using a variety of isothermal ‘flash’ algorithms (M. Michelsen, 1982; M. L. Michelsen, 1982). This formulation contrasts with the fluid-dynamics models, where the conservation laws governing are naturally posed in terms of density and internal energy (p-U). To overcome this problem, one possible solution is to use the so-called isochoric-isoenergetic flash (Castier, 2009; Michelsen, 1999). However, existing isochoric-isoenergetic flash algorithms are neither robust nor computationally efficient in the context of flow simulation because they either rely on an internal iterative loop over the P-T variables (Michelsen, 1999; Saha and Carroll, 1997) or on the direct minimisation of total entropy (Castier, 2009; Munkejord and Hammer, 2015).

The problem of computational inefficiency is exacerbated by the complexity of modern EoS. For example, for the case of CO$_2$ and its mixtures, high accuracy is provided by SAFT EoS (Diamantonis and Economou, 2011) or by the “reference” EoS (Span and Wagner, 1996) and both EoS have a large number of relatively complex terms. As a result, application of these EoS to flow simulations not only increases the computational cost, but also the susceptibility to numerical instabilities in the underlying isothermal flash algorithms. This is a particular problem in the simulation of flows associated with Carbon Capture and Storage (CCS), where the CO$_2$ stream may contain a number of impurities and vary in composition (Porter et al., 2015). Indeed, it is well established that the presence of these impurities has important impacts on many aspects where the modelling of two-phase flow is relevant, including ductile fracture (Mahgerefteh et al., 2012a) and the release rate in the case of loss of containment (Brown et al., 2013).

Previous work to address this issue has focused on producing tables of thermodynamic properties from isenthalpic or isentropic flash calculations (Mahgerefteh et al., 2006), which are facilitated by changing the variables with which the flow is resolved, or using isothermal tables for use in the iterative loop (Andresen, 2009). The former of these means that alternative numerical techniques must be applied and that conservation of mass, momentum and energy is not ensured. Dumbser et al. (2013) presented a method of building an interpolating function using adaptive mesh refinement for a single component fluid; however this relied on the ability to calculate isochoric-isoenergetic flashes which cannot be done efficiently for mixtures.

In this work a robust technique for efficiently performing isochoric-isoenergetic flashes, for the purposes of two-phase flow calculations, is presented. The technique is based on adaptive inverse interpolation and can be applied independently of the EoS and the specific mixture under consideration. The technique is intended for the application of the complex, computationally heavy EoS that are required for the accurate prediction of the thermodynamic properties and phase equilibria of CO$_2$ mixtures. This is then coupled with a two-phase flow model based on the homogeneous equilibrium mixture assumption (Brown et al., 2015a; Mahgerefteh et al., 2012b) and applied to the simulation of CCS relevant two-phase flows.
This paper is structured as follows: Section 2 firstly presents the fluid flow model applied in this study (Section 2.1) followed by a description of the interpolation technique developed (Section 2.2). The section ends with an overview of the EoS used in this work.

Section 3 provides an analysis of the interpolation technique's consistency with the EoS (Section 3.1). Next, the method is coupled with the two-phase flow model and a number of tests are performed to establish the robustness and computational efficiency of the method in the presence of rapid transients (Section 3.2). This coupled flow model is then used to predict the decompression of several mixtures and the results are compared against available experimental data (Section 3.3). Conclusions and suggestions for future work are discussed in Section 4.

2. Methodology

2.1. The Homogeneous Equilibrium Model (HEM) flow model

The model applied in this study is based on the assumptions of one-dimensional, unsteady flow and, in the case of two-phase flow, thermodynamic and mechanical equilibrium, i.e. a single temperature, pressure and velocity, between the saturated vapour and liquid phases. In this case the respective continuity, momentum, and energy conservation equations are given by (see for example Zucrow and Hoffman, 1975):

\[
\frac{\partial \rho}{\partial t} + \frac{\partial \rho u}{\partial z} = 0
\]

\[
\frac{\partial \rho u}{\partial t} + \frac{\partial \rho u^2 + P}{\partial z} = -\frac{f_w \rho u^2}{D_p}
\]

\[
\frac{\partial E}{\partial t} + \frac{\partial u(E + P)}{\partial z} = -u \frac{f_w \rho u^2}{D_p}.
\]

where \( \rho, u, P \) are respectively the mixture density, velocity and pressure, which are functions of time, \( t \), and spatial coordinate, \( z \); \( D_p \) and \( f_w \) are the pipeline diameter and Fanning friction factor, calculated using Chen's correlation (Chen, 1979), and \( E \) is the total mixture energy defined as:

\[
E = \rho \left( e + \frac{1}{2} u^2 \right)
\]

where \( e \) is the mixture specific internal energy:

\[
e = x_{eq} e_v + (1 - x_{eq}) e_l
\]

\( x_{eq} \) is the equilibrium vapour quality, and \( \rho \) is the mixture density defined as:

\[
\frac{1}{\rho} = \frac{x_{eq}}{\rho_v} + \frac{(1 - x_{eq})}{\rho_l}.
\]

In equations 5 and 6, the subscripts \( v \) and \( l \) refer to the vapour and liquid phases respectively.
To solve equations (1) to (3) numerically, a finite volume method is used (Leveque, 2002), where, following Brown et al. (2015b), the conservative left-hand-side of equations (1) to (3) are solved using the AUSM+ flux vector splitting scheme (Liou, 2006).

2.2. Interpolation technique

As described previously, the coupling of the EoS described in Section 2.3 with the flow equations (1) to (3) where the fluid is two-phase is complicated by the fact that the free variables are the density, \( \rho \), and internal energy, \( e \), with which we must compute the system \( P \) and \( T \), while the computation of the phase equilibria using an EoS (in this case PC-SAFT as described in section 2.3) is most commonly performed using the \( P \) and \( T \) of a mixture at a given composition. To overcome this, we introduce the construction of two interpolant grids, one of which is constructed using the \( P \) and \( T \) as free variables, denoted \{\( P, T \)\}, and the other using \( \rho \) and \( e \), denoted \{\( \rho, e \)\}. These grids provide the means for rapidly computing the thermodynamic properties and phase equilibria during flow simulations.

The construction begins by defining the bounds of the \{\( P, T \)\} grid using the fluid conditions required for the simulation (i.e. the intervals \([T_{\text{min}}, T_{\text{max}}]\) and \([P_{\text{min}}, P_{\text{max}}]\)). Grid points are sampled along isotherms which are uniformly distributed within the temperature range. Typically, for the pressure ranges of interest for \( \text{CO}_2 \) pipeline decompression, the isotherms will intersect the dew and bubble point and hence pass through the phase envelope. As a result, an interpolant has to be developed which can resolve the abrupt changes of the fluid properties with pressure and temperature within the phase coexistence regions, and in particular near the equilibrium lines. In practice this means that the points selected for building the interpolant cannot be uniformly distributed along the isotherm, but must be chosen so as to resolve the region around, and within, the phase envelope of the mixture, which is known a priori given the composition of the fluid.

In order to address this problem and improve the mapping, we adopt a non-uniform sampling along each isotherm, resulting in an increased density of points close to the dew and bubble point pressures (\( P_d \) and \( P_b \) respectively) and within the phase envelope itself. The set of \( N \) points along each isotherm are selected as follows:

a. if \( P_{\text{max}} \leq P_d \) or \( P_b \leq P_{\text{min}} \), i.e. a permanently single-phase fluid, the points are uniformly distributed in \([P_{\text{max}}, P_{\text{min}}]\):

\[
P_i = P_{\text{min}} + (i - 1) \frac{P_{\text{max}} - P_{\text{min}}}{N - 1}, \quad i = 1, \ldots, N
\]

b. if \( P_{\text{min}} \leq P_d \leq P_b \leq P_{\text{max}} \), i.e. the interval \([P_{\text{min}}, P_{\text{max}}]\) encompasses the two-phase region, \( N_d \) points are distributed in \([P_{\text{min}}, P_d - \Delta]\) to increase the point density close to the dew point using:

\[
P_i = P_{\text{min}} + (P_d - \Delta - P_{\text{min}}) g \left( \frac{i - 1}{N_d} \right), \quad i = 1, \ldots, N_d
\]

\( N_d \) points are distributed uniform in \([P_b + \Delta, P_{\text{max}}]\) to increase the point density close to the bubble point using:

\[
P_i = (P_b + \Delta - P_{\text{min}}) + (P_{\text{max}} - P_b - \Delta) g \left( \frac{i - 1}{N_b} \right), \quad i = 1, \ldots, N_b
\]
while the remaining $N_{VLE}$ points are distributed using the mapping function which increases the points density near the dew and the bubble line:

$$P_i = (P_d - \Delta) + (P_b - P_d + 2\Delta) g \left( \frac{i - 1}{N_{VLE}} \right), \quad i = 1, \ldots, N_{VLE}$$

with:

$$g(x) = \frac{1 + erf(Ax - B)}{2}$$

2.3. Equations of State

In the present study in order to predict the properties of CO$_2$ and its mixtures, the Perturbed Chain-Statistical Associating Fluid Theory (PC-SAFT) EoS presented by Diamantonis et al. (2013a) is applied, a brief description is given next. The PC-SAFT EoS is expressed as the summation of residual Helmholtz free energy terms that occur due to different types of intermolecular interactions between the various components in the system under study. The residual Helmholtz free energy, $A_{\text{res}}$, is equal to the Helmholtz free energy minus the Helmholtz free energy of the ideal gas at given temperature and density. For a system that consists of associating chains (for example aqueous mixtures), PC-SAFT can be expressed as:

$$\frac{A_{\text{res}}(\rho, T)}{NRT} = \frac{a_{hs}}{RT} + \frac{a_{\text{chain}}}{RT} + \frac{a_{\text{disp}}}{RT} + \frac{a_{\text{assoc}}}{RT},$$
where $\gamma$ is the Helmholtz free energy per mole, $R$ is the universal gas constant and the superscripts “res”, “hs”, “chain”, “disp”, and “assoc” refer to residual, hard sphere, chain (hard chain reference fluid), dispersion, and association, respectively. The mathematical expressions for the individual terms may be found in Diamantonis et al. (2013b). More details on the SAFT EoS and its variants for pure components and their mixtures are given in Kontogeorgis and Folas (2010).

3. Results and discussion

3.1. Interpolation consistency analysis

Prior to its application to flow simulations the consistency of the interpolation method with the underlying thermodynamic model must be assessed. For the subsequent analysis, two mixtures are chosen; a simple binary mixture of CO$_2$ and nitrogen (N$_2$) and a more complex quaternary mixture of hydrogen (H$_2$), oxygen (O$_2$), N$_2$, methane (CH$_4$) and CO$_2$ (Tests 26 and 31 respectively presented by Cosham et al., 2012). The composition of each mixture is shown in Table 1. The construction of the tables uses a total of 100 isotherms along which $N$ was taken to be 200, while $\Delta$ is set to zero. It should be noted that, due to the extended P and T conditions of the experimental data, and hence lower pressures and temperatures, produced for the binary mixture presented in Section 3.3 it is necessary to produce a table which extends to far lower temperatures. Figures 1 (a) and (b) respectively show the points sampled for the $\{P,T\}$ constructed for the binary mixture using a uniform $\{P,T\}$ grid and using the methodology developed above. The $\{P,T\}$ grid developed for this latter is shown in Figure 2. As can clearly be seen in Figure 1 (a) the “uniform sampling strategy” produces in a much sparser weighting of the points through the phase envelope compared to the one achieved in (b) where the re-distribution of the points results in a much greater number of samples between the dew and bubble point lines.

In order to quantify the deviations of the predictions obtained from the interpolation grids and the actual values calculated from the underlying EoS, 10,000 random samples are taken in the relevant $P$-$T$ domain. From these samples, the $\varepsilon(P,T)$ and $f(P,T)$ functions are evaluated using the EoS and the application of the interpolation grids using these values compared with the original point. Table 2 presents the percentage average absolute deviations (% AAD) of the predictions obtained from this analysis for both the binary and quaternary mixtures. It should be noted that the grid produced from the uniform $\{P,T\}$ sampling failed to provide predictions for all of the points used in this comparison and so is omitted. As may be observed, with the exception of the binary pressure predictions for which a value of 0.44 % was found, the results show an AAD% of less than 0.1%.

Figures 3 (a) and (b) show the %AAD contours of the predicted temperature and pressure respectively, for the binary mixture. Figures 4 (a) and (b) shows the same data for the quaternary mixture. As can be seen from both Figures 3 and 4 the error observed in the prediction of the pressure is substantially higher in places, reaching up to 10 %, than for the temperature, which is less than 0.5 % throughout; nevertheless, the regions of high error are restricted to low temperatures above the bubble point line which has limited physical interest. It should further be noted that this region also corresponds to conditions where solid formation may be expected, which however is not accounted for in the current thermophysical model.

3.2. Shock tube tests

In order to assess the efficacy of the interpolation technique developed in this work as a means of providing thermodynamic properties to flow simulations, two shock tube tests conducted are

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simulated. For the first simulation, the states are chosen such that the fluid remains in the single-phase region. For the second simulation the states are chosen to induce phase change in an initially single-phase state. The conditions for the single and two-phase shock tube tests can be found in Tables 3 and 4 respectively. In both cases, simulations are performed for both the binary and quaternary mixtures using a CFL number of 0.2 and 200 computational cells.

3.2.1. Single phase

Figures 5 (a) to (c) show the profiles of the density, pressure and temperature respectively for both the binary and quinternary mixture. As may be observed from Figure 5 (a) for the density of the binary mixture, an expansion wave is observed at ca. 0.3 to 0.4 separating two constant states; this is followed by a jump in the density across the discontinuity at ca. 0.6 before a smooth drop beginning at ca 0.8 and ending at ca. 0.9. It is clear that the features of the results for the quinternary mixture are the same as in the binary case, with the exception that they are at a lower density level.

For the pressure (Figures 5 (b)) the results for both the binary and quinternary mixtures are almost identical; as expected the discontinuity is still present. The slight variations are likely due to the slight differences in the speed of sound and hence wave speeds. The temperature results show the same similarities between the two mixtures (Figure 5 (c)). Importantly, the interpolated results remain stable despite the presence of shock and rarefaction waves as well as contact discontinuities.

3.2.2. Two-phase

Figures 6 (a) to (d) shows the profiles of the density, vapour fraction, pressure and temperature respectively, for the binary and quinternary mixtures. While the left hand states are the same and the fluid is in the single-phase region, the state on the right is selected within the mixture’s phase envelope. Thus, relative to the dew line, the states are different for both of the two mixtures simulated.

As Figure 6 (a) shows, for the binary mixture the density falls across the expansion wave which begins at ca. 0.3 m and ends at ca. 0.4 m. The density drops sharply at 0.58 m, where the initial boundary between the states was placed; this is followed by a slight distortion of the discontinuity at ca. 0.62 m, representing an additional wave, and a slower drop across the shock between 0.64 m and 0.68 m. Similar trends are observed for the quinternary mixture. However, the density throughout is lower and the shock wave from 0.64 m is smeared over a larger distance.

The profiles of the vapour fraction (Figure 6 (b)) show that no vapour is produced across the expansion wave. The vapour fraction is seen to increase through the series of waves between 0.58 m and 0.64 m. Interestingly, across the shock wave, the vapour fraction increases for the binary and decreases for the quinternary mixture, which is due to the different phase equilibria through the respective mixture’s phase envelopes.

Following the expansion wave, the pressures (Figure 6 (c)) obtained prior to the shockwaves is substantially higher for the quinternary mixture, and in both cases relates to the bubble line pressure of the fluids. In the case of the temperature (Figure 6 (d)), a fall is observed through the expansion wave as with the density, after this however a sharp fall is seen at discontinuity before rising and falling again. For this latter behaviour the quinternary mixture exhibits much larger changes.
3.3. Decompression tests

In the following, the robustness of the HEM outflow model coupled with the interpolation technique is evaluated for pipeline releases of CO$_2$ mixtures. The outflow model is validated against two sets of experimental data obtained from Full-Bore Rupture (FBR) releases of CO$_2$ from a 144 m long, 150 mm internal diameter section of pipeline using the two mixtures introduced earlier (Cosham et al., 2012). Table 1 presents the initial conditions and composition of fluid in the pipeline in both cases. Given the very short depressurisation durations considered in both tests, heat transfer between the pipe wall and the pipe surrounding is ignored in the model. The pipeline roughness was found experimentally to be 0.005 mm, while the ambient pressure was 1.01 bara.

3.3.1. Binary mixture

Figure 7 shows comparison of the predicted and measured variation of the pressure at the closed end of the section of pipeline following the initiation of the decompression. As may be observed in the predicted results, the pressure remains initially constant but falls rapidly at ca. 0.2 s when the initial expansion wave, caused by the decompression, reaches the closed end of the pipeline. The experimental pressures shown were sampled with too low frequency to resolve this. Following this, a pressure plateau of ca. 58 bara is predicted, until ca. 2.5 s at which point the pressure begins to fall again towards the ambient. In comparison, after the initial pressure drop, the experimental pressure is observed to fall more slowly to a minimum at ca. 1 s before recovering to a pressure very close to the plateau pressure predicted by the model. This is practically important as this pressure is that which is used in the analysis of the propagation of ductile fractures (Mahgerefteh et al., 2012a). Following this the pressure again drops, but at a slower rate than that predicted. As noted by various authors (Mahgerefteh et al., 2012b; Munkejord et al., 2010) this later behaviour is largely due to frictional and heat transfer effects, the modelling of which is outside of this study.

Figure 8 shows the thermodynamic trajectory at the closed end of the pipeline section during the decompression relative to the dew and bubble lines. As may be observed, as noted above, during the initial decompression the fluid drops almost instantaneously along the isentrope into the phase envelope where it descends towards the dew line at low temperatures.

3.3.2. Quaternary mixture

Figure 9 shows the comparison of the predicted pressures with the experimental data recorded at transducers P14 and P18, 1.84 m and 3.64 m from the open end of the pipeline respectively (Cosham et al., 2012). As may be observed, at both P14 and P18 the time at which the initial pressure drop occurs, 2.75 and 5.5 ms respectively, is well captured. The recorded pressure during the initial decompression is seen to be slower than that predicted; this deviation can partially be explained by a lag in the measurements, given the rapidity in the pressure change.

Following this initial period of transients the simulations predict a steadying of the pressure at ca. 65 bara, at P18 this lasts for the duration of the simulation while for P14 the pressure begins to fall at ca. 36 ms. In contrast, the measured data fall steadily throughout this period, this is likely in part due to the effects of friction and heat transfer which the fluid model applied here does not capture accurately (Mahgerefteh et al., 2012b). Notably the measured pressure at P14 indicates a subsequent acceleration of the pressure drop at the time predicted by the fluid model.
4. Conclusions

This paper presents the development and application of a robust interpolation technique for the prediction of thermodynamic properties and phase equilibria of complex mixtures. The accuracy and computational burden of computing these physical properties greatly affects the overall accuracy and computational cost of multiphase multicomponent simulations. Thus, the adaption of this technique has a tremendous impact on our ability to perform sophisticated computational fluids dynamics (CFD) simulations at reasonable cost without significant loss of accuracy.

The assessment of the technique’s ability to reproduce the results of the EoS showed, for the most part, an error no greater than 0.5 % compared to the actual EoS predictions. Large errors were observed only for the liquid phase at low temperatures, where the physical model represented by the EoS is itself not applicable, as solid formation not predicted by the EoS is expected. The extension of the current interpolation technique to a thermophysical model where the solid phase is accounted for is part of ongoing work.

Following this, the method was coupled with a fluid model and was used for the simulation of CO\textsubscript{2} rich mixtures, which is of particular interest in the development of CCS technology. Analysis of several hypothetical shock tube tests, as well as the comparison of the predictions against experimental decompression data, showed that the interpolation method produced robust and highly reliable results for simple and complex mixtures.

Interestingly, comparison between model predictions and experimental decompression results showed that the implementation of the interpolation technique produced a reasonable prediction of the initial depressurisation period. On-going work by the authors focuses on the development of appropriate models for the heat transfer and frictional effects to improve the accuracy of the predictions beyond this period.

5. Acknowledgements

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Data 25.

Table 1. Initial conditions and fluid composition for decompression experiments Test 26 and 31 (Cosham et al., 2012).

<table>
<thead>
<tr>
<th>Input Parameter</th>
<th>Test 26</th>
<th>Test 31</th>
</tr>
</thead>
<tbody>
<tr>
<td>Feed Inlet Temperature (K)</td>
<td>278.35</td>
<td>283.15</td>
</tr>
<tr>
<td>Feed Inlet Pressure (bar)</td>
<td>141</td>
<td>151.51</td>
</tr>
<tr>
<td>Fluid Composition (% vol./vol)</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>H₂ : 1.15</td>
<td></td>
</tr>
<tr>
<td></td>
<td>N₂ : 4.0</td>
<td></td>
</tr>
<tr>
<td></td>
<td>CO₂ : 95.96</td>
<td></td>
</tr>
<tr>
<td></td>
<td>O₂ : 1.87</td>
<td></td>
</tr>
<tr>
<td></td>
<td>CH₄ : 1.95</td>
<td></td>
</tr>
<tr>
<td></td>
<td>CO₂ : 91.03</td>
<td></td>
</tr>
</tbody>
</table>

Table 2. Average absolute deviations (%) of predictions of the temperature and pressure produced by the interpolation grids.

<table>
<thead>
<tr>
<th>Input Parameter</th>
<th>Binary</th>
<th>Quternary</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature</td>
<td>0.005</td>
<td>0.002</td>
</tr>
<tr>
<td>Pressure</td>
<td>0.44</td>
<td>0.07</td>
</tr>
</tbody>
</table>

Table 3. Initial states for the single-phase shock tube tests

<table>
<thead>
<tr>
<th>Input Parameter</th>
<th>P (bara)</th>
<th>Temperature (K)</th>
<th>Velocity (m s⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Left state</td>
<td>151</td>
<td>283.15</td>
<td>0</td>
</tr>
<tr>
<td>Right state</td>
<td>100</td>
<td>260.00</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 4. Initial states for the two-phase shock tube tests

<table>
<thead>
<tr>
<th>Input Parameter</th>
<th>P (bara)</th>
<th>Temperature (K)</th>
<th>Velocity (m s⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Left state</td>
<td>151</td>
<td>283.15</td>
<td>0</td>
</tr>
<tr>
<td>Right state</td>
<td>P_dew+2</td>
<td>260.00</td>
<td>0</td>
</tr>
</tbody>
</table>

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Figure 1: The $\{\rho, c\}$ interpolation grids in the case of a uniform sampling (a) and with the adaptive sampling method (b) produced for the binary mixture of 95.96% CO$_2$ - 4.04% N$_2$ (vol/vol).

Figure 2: The $\{P,T\}$ interpolation grid produced with the adaptive sampling method for the binary mixture of 95.96% CO$_2$ - 4.04% N$_2$ (vol/vol).
Figure 3: %AAD interpolation errors observed in the pressure (a) and temperature (b) across the relevant region in the P-T phase diagram for the binary mixture.
Figure 4: %AAD interpolation errors observed in the pressure (a) and temperature (b) across the relevant region in the P-T phase diagram for the quaternary mixture.
Figure 5: Comparison of binary and quaternary mixture profiles of density (a), pressure (b) and temperature (c) for the single-phase shock tube test after 0.4 ms.
Figure 6: Comparison of binary and quaternary mixture profiles of density (a), vapour fraction (b), pressure (c) and temperature (d) for the two-phase shock tube test after 0.4 ms.
Figure 7: Comparison of the predicted and measured variation of pressure with time at the closed end of the pipeline following the initiation of decompression.

Figure 8: Thermodynamic trajectory of the decompression relative to the binary mixture phase envelope at the closed end of the pipeline following the initiation of decompression.

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Figure 9: Comparison of the predicted and measured variation of pressure with time 1.84 m (P14) and 3.84 (P18) from the open end of the pipeline following the initiation of decompression for the case of quinternary mixture.