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***Tables***

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**Published paper**

Jumahat, A., Soutis, C., Jones, F.R., Hodzic, A. (2009) *Fracture mechanisms and failure analysis of carbon fibre/toughened epoxy composites subjected to compressive loading*, Composite Structures, 92 (2), pp. 295-305  
<http://dx.doi.org/10.1016/j.compstruct.2009.08.010>

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Table 1

Summary of material properties of the HTS40/977-2 toughened composite system.

Material Properties	Symbol	Data
<i>Properties of the HTS40 carbon fibre</i>		
Density*	$\rho_f$	1.76 g/cm <sup>3</sup>
Average fibre diameter	$d_f$	6.96 $\mu$ m
Elastic modulus*	$E_f$	239 GPa
Tensile strength*	$\sigma_{fu}$	4629 MPa
Failure strain in tension*	$\gamma_{fu}$	1.80 %
<i>Properties of the Cycom<sup>®</sup>977-2 thermoplastic toughened epoxy resin</i>		
Density	$\rho_m$	1.31 g/cm <sup>3</sup>
Elastic modulus	$E_m$	3.5 GPa
Tensile strength	$\sigma_{mu}$	81 MPa
Failure strain in tension	$\gamma_{mu}$	2.50 %
<i>Physical properties of UD HTS40/977-2 composite laminate</i>		
Density	$\rho_c$	1.54 g/cm <sup>3</sup>
Fibre volume fraction	$V_f$	58%
Initial Half Fibre wavelength	$\lambda_o$	10 $d_f$
Initial misalignment angle	$\phi_o$	0.92 <sup>o</sup>
Laminate width	$w$	0.01 m
Overall Laminate thickness	$t_o$	2.16 mm
No. of plies	$n$	8
Ply thickness	$t_p$	270 $\mu$ m
<i>Compressive Properties of UD HTS40/977-2 composite laminate</i>		
Longitudinal compressive modulus	$E_1$	112 GPa
Longitudinal compressive strength	$\sigma_1$	1396 MPa
Compressive failure strain	$\varepsilon_1$	1.5 %
Principal Poisson Ratio	$\nu_{12}$	0.3
<i>Tensile properties of [<math>\pm 45</math>]<sub>2s</sub> HTS40/977-2 composite laminate</i>		
Tensile modulus at 0.2% strain	$E_{[\pm 45]}$	22 GPa
Tensile strength	$\sigma_{[\pm 45]}$	202 MPa
Failure strain	$\varepsilon_{[\pm 45]}$	7.6 %
<i>In-Plane Shear Properties of HTS40/977-2 composite laminate</i>		
Elastic in-plane Shear Modulus	$G_{12}^e$	4.4 GPa
Plastic in-plane Shear Modulus	$G_{12}^p$	0.68 GPa
In-plane shear yield strength	$\tau_y$	52MPa
In-plane shear strain at yield	$\gamma_y$	1.8 %
In-plane shear strength	$\tau_{ult}$	101 MPa
In-plane shear strain at shear strength	$\gamma_{ult}$	17 %

\* [manufacturer datasheet]

Table 2

Input data for the compressive failure predictions of the UD HTS40/977-2 CFRP composite laminate using several types of failure models.

Failure mode	Reference	Eqn.	Input data
Fibre kinking	Budiansky [18]	(1)	$\tau_y = 52$ MPa, $\sigma_{ry} = 40$ MPa, $\gamma_y = 0.018$ , $\phi_o = 0.92^\circ$ , $\beta = 20^\circ$
Fibre microbuckling (non-linear matrix)	Berbinau et al [12] (incorporated a newly developed elastoplastic shear stress-strain behaviour)	(10)	$V_f = 0.58$ , $r_f = 3.5$ $\mu\text{m}$ , $E_f = 239$ GPa, $\phi_o = 0.92^\circ$ , $\tau_y = 52$ MPa, $\tau_{ult} = 101$ MPa, $G_{12}^e = 4.4$ GPa, $G_{12}^p = 0.68$ GPa, $\lambda_o = 10d_f = 70\mu\text{m}$ ,
Combined modes model (fibre microbuckling and plastic kinking models)	(a new developed model based on Berbinau [12] and Budiansky [18])	(12)	$V_f = 0.58$ , $r_f = 3.5$ $\mu\text{m}$ , $E_f = 239$ GPa, $\phi_o = 0.92^\circ$ , $\tau_y = 52$ MPa, $\gamma_y = 0.018$ , $\tau_{ult} = 101$ MPa, $\gamma_{ult} = 0.18$ , $G_{12}^e = 4.4$ GPa, $G_{12}^p = 0.68$ GPa, $\lambda_o = 10d_f = 70\mu\text{m}$ ,

Table 3

Summary of the input data for the study of the effects of non-linear shear stress-strain ( $\tau$ - $\gamma$ ) response, initial fibre misalignment  $\phi_o$ , initial half-wavelength  $\lambda_o$  and fibre volume fraction  $V_f$  on the compressive strength of the UD HTS40/977-2 composite laminate.

Programme name	$\tau_y$ (MPa)	$\tau_{ult}$ (MPa)	$G_{12}^e$ (GPa)	$G_{12}^p$ (GPa)	$\phi_o$	$\gamma_y$ (%)	$\lambda_o$	$V_f$
$\tau_y = 45$ MPa	45	85	3.7	0.58	$1^\circ$	1.8	$10d_f$	0.55
$\tau_y = 52$ MPa	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.55
$\tau_y = 60$ MPa	60	115	5.0	0.80	$1^\circ$	1.8	$10d_f$	0.55
$\tau_y = 68$ MPa	68	130	5.7	0.90	$1^\circ$	1.8	$10d_f$	0.55
$\phi_o = 1^\circ$	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.55
$\phi_o = 2^\circ$	62	101	4.4	0.68	$2^\circ$	2.6	$10d_f$	0.55
$\phi_o = 3^\circ$	65	101	4.4	0.68	$3^\circ$	3.1	$10d_f$	0.55
$\phi_o = 5^\circ$	72	101	4.4	0.68	$5^\circ$	4.5	$10d_f$	0.55
$\lambda_o = 8d_f$	52	101	4.4	0.68	$1^\circ$	1.8	$8d_f$	0.55
$\lambda_o = 10d_f$	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.55
$\lambda_o = 12d_f$	52	101	4.4	0.68	$1^\circ$	1.8	$12d_f$	0.55
$\lambda_o = 15d_f$	52	101	4.4	0.68	$1^\circ$	1.8	$15d_f$	0.55
$V_f = 50\%$	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.50
$V_f = 55\%$	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.55
$V_f = 60\%$	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.60
$V_f = 65\%$	52	101	4.4	0.68	$1^\circ$	1.8	$10d_f$	0.65

