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Proceedings Paper:
Predictive control design on an embedded robust output-feedback compensator for wind turbine blade-pitch preview control

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Abstract—The use of upstream wind measurements has motivated the development of blade-pitch preview controllers to improve rotor speed tracking and structural load reduction beyond that achievable via conventional feedback design. Such preview controllers, typically based upon model predictive control (MPC) for its constraint handling properties, alter the closed-loop dynamics of the existing blade-pitch feedback control system. This can result in the robustness properties of the original closed-loop system being no longer preserved. As a consequence, several authors (e.g. [6]–[8]), employed model predictive control (MPC) for its ability to handle constraints and feed-forward information, and their results demonstrated the efficacy of a preview MPC design in the flap-wise blade load reduction.

The majority of wind turbine preview MPC studies can be divided into two categories. The first branch is to formulate the blade-pitch control problem as one single MPC formulation where the resultant controller handles both feedback and feed-forward measurements (e.g. [7]), whilst the second branch is to construct the MPC layer based on a known state-feedback controller (e.g. [6]). The shortcomings of both methods are that the robustness and closed-loop frequency-domain properties are usually not well considered in a standard MPC design. The loads on turbine blades predominately exist at the harmonics of the blade rotational frequency, thus, it is not straightforward to design robust closed-loop feedback controllers in the time-domain. Furthermore, it is often assumed that the existing controllers use full state-feedback, despite the fact that output-feedback controllers are prevalent in industry.

This work therefore aims to bridge this gap by formulating a MPC layer based on a known robust output-feedback controller, where the MPC layer handles constraints and upcoming wind measurements. A further key focus of this paper stems from existing research often overlooking the conditions that separate the original closed-loop dynamics from the additional control layer design. If the given closed-loop dynamics are changed by the extra layer design, as a consequence, the benefits of utilising real-time measurement of the upstream wind become less transparent. The separate nature of the MPC layer is important from an industry perspective, since it can be implemented without replacing the existing feedback controller. Also, it provides a clear framework to quantify the benefits of feed-forward and predictive control over a baseline feedback strategy.

The remainder of this paper is structured as follows. In Section II, the modelling aspect of the blade pitch control problem, including disturbance modelling, is presented and the detail of the nominal embedded feedback controller is discussed. This is followed in Section III by a formulation of a predictive control layer and the conditions that ensure the original closed-loop dynamics are retained which is the main result of this paper. In Section IV, simulation results on a high-fidelity wind turbine demonstrate the benefits of having the proposed MPC layer on top of the closed-loop
feedback controller. Conclusions are in Section V.

II. WIND TURBINE MODELLING AND NOMINAL ROBUST FEEDBACK COMPENSATOR

This section presents background on the wind turbine model and disturbances. In addition, the details of the embedded nominal robust feedback controller are discussed.

A. Wind turbine modelling

A typical wind turbine blade pitch control system architecture for above-rated conditions is depicted in Figure 1. The CPC regulates the rotor speed \( \omega(t) \) by adjusting the collective pitch angle signal whilst the IPC attenuates perturbations in the flap-wise root bending moments on each blade. Additional inputs to the turbine, such as wind loading and generator torque, are accounted for in the term \( f(t) \)

\[
\begin{bmatrix}
\dot{\theta}_1(t) \\
\dot{\theta}_2(t) \\
\dot{\theta}_3(t)
\end{bmatrix} =
\begin{bmatrix}
\dot{\theta}(t) + \dot{\theta}_1(t) \\
\dot{\theta}(t) + \dot{\theta}_2(t) \\
\dot{\theta}(t) + \dot{\theta}_3(t)
\end{bmatrix},
\begin{bmatrix}
\dot{M}_1(t) \\
\dot{M}_2(t) \\
\dot{M}_3(t)
\end{bmatrix} =
\begin{bmatrix}
\dot{M}(t) + \dot{M}_1(t) \\
\dot{M}(t) + \dot{M}_2(t) \\
\dot{M}(t) + \dot{M}_3(t)
\end{bmatrix}
\]

(1)

For simplicity, it is assumed that there is no coupling between the CPC and IPC loops from the tower dynamics. The relationship between collective pitch input \( \dot{\theta}(t) \) and rotor speed output \( \omega(t) \) can be modelled by a transfer function \( G_{\omega \theta}(s) \) obtained by linearising the turbine dynamics around the operating wind condition of 18 m\( \text{s}^{-1} \), chosen because this value is close to the centre of the range of wind speeds covering the above-rated wind condition. Similarly, the relationship mapping the perturbations in flap-wise blade root bending moment \( M_{1,2,3} \) to additional pitch angle \( \dot{\theta}_{1,2,3} \) of each blade can be modelled by a transfer function \( G_{M \theta}(s) \). These transfer functions are as follows:

\[
\begin{align*}
G_{\omega \theta}(s) & := G_a(s)G_T(s), \\
G_{M \theta}(s) & := G_a(s)G_b(s)G_{\text{bp}}(s),
\end{align*}
\]

(2a)

(2b)

where \( G_T(s), G_b(s) \) and \( G_a(s) \) describe the dynamics of rotor, blade and actuator, respectively, whilst \( G_{\text{bp}}(s) \) is a band-pass filter that is included in order to remove the low and high frequency contents of the blade root bending measurement signals, obtained from strain-gauge sensors. These transfer functions are defined as follows:

\[
\begin{align*}
G_T(s) & := \frac{\partial \omega}{\partial \theta} \frac{1}{\tau_s s + 1}, \\
G_b(s) & := \frac{\partial M_{\text{bp}}}{\partial \theta} \frac{(2\pi f_b)^2}{s^2 + 4\pi f_b D_b s + (2\pi f_b)^2}, \\
G_a(s) & := \frac{1}{\tau_s s + 1}, \\
G_{\text{bp}}(s) & := \frac{2\pi f_b}{s^2 + 2\pi(f_b + f_i)s + 4\pi^2 f_b f_i},
\end{align*}
\]

(3a)

(3b)

(3c)

(3d)

where \( \frac{\partial \omega}{\partial \theta} \) and \( \tau_s \) denote the the variation in rotor speed in time constant of the rotor dynamics, whilst \( \frac{\partial M_{\text{bp}}}{\partial \theta} \). \( D_b \) and \( f_b \) represent change in blade bending moment to pitch angle, blade damping ratio and natural frequency of first blade mode, respectively. The time constant of the pitch actuator is \( \tau \) whilst \( f_i \) and \( f_i \) denote the upper and lower cut-off frequencies of the band-pass filter, respectively. Values are listed in Table II.

B. Disturbance modelling

The rotor and blade are subjected to a temporally varying and spatially distributed wind field. Given the feasibility of estimating the wind-field from a few point measurements taken upstream of the turbine (e.g. [12]), this work assumes the full approaching wind field is known a priori. The disturbance trajectories of rotor speed \( \omega_d \) and flap-wise blade bending moment \( M_{d,i} \), for \( i \in \{1, 2, 3\} \), caused by the approaching wind, are defined as follows:

\[
\begin{align*}
\omega_d(t) & := \sum_{l, \phi} \frac{\partial \omega}{\partial v} (\bar{v}, l) v(l, \phi) \\
M_{d,i}(t) & := \sum_{l, \phi} \frac{\partial M_{\text{bp}}}{\partial v} (\bar{v}, l) v(l, \phi), \quad i = 1, 2, 3
\end{align*}
\]

(4)

(5)

where \( v(l, \phi) \) denote the stream-wise wind speed measurements where \( l \) and \( \phi \) represent the radial and angular coordinates across the rotor disk whilst \( \bar{v} \) denote the averaged wind speed of the measurements. Noted that span-wise and vertical wind speed is assumed negligible because the turbine blades spin fast in span-wise and vertical directions. The variations in rotor speed and blade bending moment with respect to the wind are denoted as \( \frac{\partial \omega_d}{\partial v} \) and \( \frac{\partial M_{d,i}}{\partial v} \). The rotor speed response \( \omega \) to wind-induced disturbance \( \omega_d \) is modelled as a first-order transfer function \( G_{\omega_d}(s) \), whilst the response of flap-wise blade root bending moment \( M_i \) to wind-induced disturbance \( M_{d,i} \), for \( i \in \{1, 2, 3\} \), is modelled as \( G_{M_{d,i}}(s) \):

\[
\begin{align*}
G_{\omega_d}(s) & := \frac{1}{\tau_s s + 1}, \\
G_{M_{d,i}}(s) & := \frac{(2\pi f_b)^2}{s^2 + 4\pi f_b D_b s + (2\pi f_b)^2} G_{\text{bp}}(s),
\end{align*}
\]

(6a)

(6b)
Combining (2) and (6), the overall transfer function models $G(s)$ and $G_d(s)$ can be represented as follows:

\[
\begin{bmatrix}
\omega(s) \\
\dot{M}_1(s) \\
\dot{M}_2(s) \\
\dot{M}_3(s)
\end{bmatrix} =
\begin{bmatrix}
G_{\omega\theta}(s) & 0 & 0 & 0 \\
0 & G_{M\theta}(s) & 0 & 0 \\
0 & 0 & G_{M\theta}(s) & 0 \\
0 & 0 & 0 & G_{M\theta}(s)
\end{bmatrix}
\begin{bmatrix}
\dot{\theta}(s) \\
\dot{\theta}_1(s) \\
\dot{\theta}_2(s) \\
\dot{\theta}_3(s)
\end{bmatrix}
\]

\[
+ \begin{bmatrix}
G_{\omega\omega}(s) & 0 & 0 & 0 \\
0 & G_{M\omega}(s) & 0 & 0 \\
0 & 0 & G_{M\omega}(s) & 0 \\
0 & 0 & 0 & G_{M\omega}(s)
\end{bmatrix}
\begin{bmatrix}
\omega(s) \\
\dot{M}_1(s) \\
\dot{M}_2(s) \\
\dot{M}_3(s)
\end{bmatrix}
\]

Equivalently, a discrete-time state-space model representation can be constructed as follows:

\[
x_{k+1}^p = A^p x_k^p + B^p u_k + B_d^p d_k,
\]

\[
y_k = C^p x_k^p,
\]

\[
u_k = [\dot{\theta}(s), \dot{\theta}_1(s), \dot{\theta}_2(s), \dot{\theta}_3(s)]^T,
\]

\[
y_k = [\dot{\omega}(s), \dot{M}_1(s), \dot{M}_2(s), \dot{M}_3(s)]^T,
\]

\[
d_k = [\dot{\omega}_d, \dot{M}_d, \dot{M}_d, \dot{M}_d]^T,
\]

where superscript $p$ denotes plant.

C. Nominal embedded robust feedback controller

The chosen robust feedback controller $K(s)$, consisting of the CPC $K_{\theta\omega}(s)$ and the IPC $K_{\theta\theta}(s)$, employed in this work is defined as follows:

\[
\begin{bmatrix}
\dot{\theta}(s) \\
\dot{\theta}_1(s) \\
\dot{\theta}_2(s) \\
\dot{\theta}_3(s)
\end{bmatrix} =
\begin{bmatrix}
K_{\theta\omega}(s) & 0 & 0 & 0 \\
0 & K_{\theta\theta}(s) & 0 & 0 \\
0 & 0 & K_{\theta\theta}(s) & 0 \\
0 & 0 & 0 & K_{\theta\theta}(s)
\end{bmatrix}
\begin{bmatrix}
\dot{\omega}(s) \\
\dot{M}_1(s) \\
\dot{M}_2(s) \\
\dot{M}_3(s)
\end{bmatrix}
\]

where $K_{\theta\omega}(s)$ and $K_{\theta\theta}(s)$ obtained from [11], are presented in Appendix I. It is assumed no dynamic coupling exists between the fixed and rotating turbine structures. The simulation results in [11] showed that a controller of the form (9) could be designed to be insensitive to such coupling by shaping the open-loop frequency response to have low gain at the tower frequency. Similar to the plant model, the nominal feedback controller (9) in a discrete time-state space realisation is:

\[
x_{k+1}^\kappa = A^\kappa x_k^\kappa - B^\kappa y_k,
\]

\[
u_k = C^\kappa x_k^\kappa - D^\kappa y_k,
\]

where the vector $x^\kappa$ represents the state of the controller and the superscript $\kappa$ denotes controller.

III. FORMULATION OF THE MPC LAYER

The architecture combining the proposed MPC layer and the nominal feedback controller is shown in Figure 2, where the shaded area depicts the existing closed-loop system. The closed-loop system dynamics in a state-augmented form can be derived from the discrete-time state-space wind turbine model (8) and the feedback controller (10):

\[
x_{k+1}^\kappa = A^\kappa x_k^\kappa + B^\kappa y_k + B_d^\kappa d_k
\]

\[
y_k = C^\kappa x_k^\kappa + D^\kappa y_k
\]

Note that an incremental input $\Delta u_k$ is employed in the state-augmented closed-loop system model (11a) as the input variable because of the simplicity of formulation of blade pitch rate and angle constraints.

A. Augmentation of input perturbations into the underlying feedback control law

The MPC formulation in this work adopts a closed-loop paradigm [13] where the degrees-of-freedom (d.o.f) $c_k$ can be set up around the stabilising feedback control law (11b) $\Delta u_k = K x_k$ such that the input can be parametrised as $\Delta u_k = K x_k + c_k$ with the premise that the perturbation $c_k \neq 0$ if and only if constraints are active or feed-forward knowledge is available. Such a feature is particularly useful in formulating a MPC layer on top of an embedded closed-loop controller. The closed-loop paradigm employed in this work uses a dual-mode approach and these two modes of predictions are the transient mode and the terminal mode. In transient mode, a sequence of input d.o.f, is denoted as $x_k = [c_0|c_1|...|c_{n-1}]^T$, is optimised over the control horizon $n_c$ with respect to handling of constraints and feed-forward information, whilst in the terminal mode, the closed-loop dynamics are governed by the pre-determined control law, which is the embedded robust feedback pitch controller in this case. Considering (11a), the predictions of input and state at sample time $k$ can be described as follows:

\[
\Delta u_{i|k} = \begin{cases} 
K x_{i|k} + c_{i|k}, & \forall i < n_c, \\
K x_{i|k}, & \forall i \geq n_c
\end{cases}
\]

\[
x_{i+1|k} = \begin{cases} 
\Phi x_{i|k} + B c_{i|k} + B_d d_{i|k}, & \forall i < n_c, \\
\Phi x_{i|k} + B_d d_{i|k}, & \forall i \geq n_c
\end{cases}
\]
where $\Phi = A + BK$. Noted that $x_0[k] = x_k$. The predictions of disturbance measurement $d_{i+1,k} = \begin{bmatrix} d_{0,k}, d_{1,k}, ..., d_{n_a-1,k} \end{bmatrix}^T$ is defined as follows:

$$d_{i+1,k} = \begin{cases} d_{k+i}, & \forall i < n_a \\ 0, & \forall i \geq n_a \end{cases} \quad (12c)$$

It is assumed that beyond the preview horizon $n_a$, the upcoming disturbance measurement becomes zero. Subsequently, it is more convenient to represent the dual-mode predictions in one autonomous model such that the model consists of state predictions (12b), input prediction sequence (12a) and advance disturbance measurement (12c). The autonomous model with the augmented state $z_{i,k}$ defined as follows:

$$z_{i+1,k} = \Psi z_{i,k} \quad (13a)$$

where the initial augmented state $z_0[k] = \begin{bmatrix} x_0[k], c_{0,k}, d_{0,k}^T \end{bmatrix}^T$ and $\Psi$ is defined as:

$$\Psi = \begin{bmatrix} \Phi & BE & B_dE \\ 0 & M_c & 0 \\ 0 & 0 & M_d \end{bmatrix} \quad (13b)$$

$$E c_{\rightarrow k} = c_0[k], E \overrightarrow{d}_{\rightarrow k} = d_{0,k}, \quad (13c)$$

$$M_c c_{\rightarrow k} = \begin{bmatrix} c_{1,k}, ..., c_{n_a-1,k} \end{bmatrix}^T, \quad (13d)$$

$$M_d \overrightarrow{d}_{\rightarrow k} = \begin{bmatrix} d_{1,k}, ..., d_{n_a-1,k} \end{bmatrix}^T. \quad (13e)$$

Consequently, the prediction of state and input (employed in the cost function) can be expressed in terms of the autonomous model (13a) as follows:

$$x_{i,k} = \begin{bmatrix} I & 0 & 0 \end{bmatrix} z_{i,k}, \quad \forall i \geq 0, \quad (14a)$$

$$\Delta u_{i,k} = \begin{bmatrix} K & 0 \end{bmatrix} z_{i,k}, \quad \forall i \geq 0. \quad (14b)$$

**B. Formulation of the cost function**

The input perturbation sequence $c_{\rightarrow k}$ is computed by solving a constrained minimisation of the predicted cost where the predicted cost function quantifying the balance between performance and input effort is defined as follows:

$$J := \sum_{i=0}^{\infty} \left[ x_{i+1,k}^T Q x_{i,k} + \Delta u_{i+1,k}^T R \Delta u_{i,k} + 2 x_{i+1,k}^T N \Delta u_{i,k} \right] \quad (15)$$

where $Q$, $R$ and $N$ denote the weighting matrices that specify the penalties on state and input in the cost. For practical reasons, the infinite-horizon cost function (15) needs to be expressed in a finite-horizon form such that it can be solved on-line rapidly by quadratic programming. By expressing the prediction of the deviation variables of state (14a) and input (14b) in terms of the autonomous model, the cost function (15) can be simplified as follows:

$$J := z_0[k]^T \sum_{i=0}^{\infty} \lambda_i^T x_0[k] + \lambda_i^T R x_0[k] + 2 \lambda_i^T N x_0[k] \quad (16)$$

Consequently, the cost function (16) can be further simplified, using the Lyapunov equation $\Psi^T S \Psi = S - W$, as:

$$J := \begin{bmatrix} x_0[k] \\ \Psi \end{bmatrix}^T \begin{bmatrix} S_x & S_{xc} & S_{cd} \\ S_{xc}^T & S_{cc} & S_{cd} \\ S_{cd}^T & S_{cd} & S_d \end{bmatrix} \begin{bmatrix} x_0[k] \\ \Psi \end{bmatrix} \quad (17)$$

**C. Constraint formation in terms of input perturbations**

The physical limits on pitch actuator rate and angle are considered as hard constraints in this work. The limits on pitch rate are ±8 degrees per second, whilst the pitch angle is bounded between 0 degree and 90 degrees:

$$\Delta u \leq \Delta u_{i,k} \leq \Delta \bar{u}, \quad \forall i \geq 0, \quad (18a)$$

$$\bar{u} \leq u_{i,k} \leq \bar{u}, \quad \forall i \geq 0. \quad (18b)$$

These inequalities can be written in terms of the autonomous model (13a), with $z_{i,k} = \Psi^T z_0[k]$, as follows:

$$H \Psi^T z_0[k] \leq f, \quad \forall i \geq 0. \quad (18c)$$

where $H z_{i,k} = \begin{bmatrix} u_{i,k} - u_{i,k}, -\Delta u_{i,k}, -\Delta u_{i,k} \end{bmatrix}^T$ and $f = \begin{bmatrix} \bar{u}, \bar{u}, \bar{u}, \bar{u} \end{bmatrix}^T$. It is noted that to ensure no constraint violations, possible violations must be checked over an infinite prediction horizon. Nevertheless, there exists a sufficiently large horizon where any additional linear equalities become redundant [14]. Consequently, for a practical approach, this study formulates the inequalities by checking the constraints over twice the control horizon and the inequalities can be described by a set of suitable matrices ($M, N, V$ and $b$) as follows:

$$M x_k + N c_{\rightarrow k} + V d_{\rightarrow k} \leq b. \quad (19)$$

To sum up the discussion so far, the optimal input perturbation sequence $c_{\rightarrow k}$ from the MPC layer can be computed by solving a minimisation of the predicted cost function (17) subject to constraints (19). This is summarised in Algorithm 1:

**Algorithm 1:** At each sampling instant perform the optimisation below. The first block element of the perturbation $c_{\rightarrow k}$ is applied within the embedded control law (12a):

$$c_{\rightarrow k} = \begin{cases} c_{T_{\rightarrow k}} c_{\rightarrow k} + 2 c_{T_{\rightarrow k}} S c_{\rightarrow k} x_{0[k]} + 2 c_{T_{\rightarrow k}} S_{cd} d_{\rightarrow k} \\ \text{s.t.} \quad M x_k + N c_{\rightarrow k} + V d_{\rightarrow k} \leq b \end{cases} \quad (20a)$$

**D. Key result: Conditions for separating the original closed-loop dynamics from the additional layer design**

The unconstrained optimal input sequence can be obtained by solving the minimisation of the cost (17) as follows:

$$c_{\rightarrow k} = -S_{c_{\rightarrow k}}^{-1} S_{c_{\rightarrow k}} x_{0[k]} - S_{c_{\rightarrow k}}^{-1} S_{cd} d_{\rightarrow k} \quad (21)$$

Close inspection of (21) suggests that, to retain the closed-loop robust properties, the perturbation sequence $c_{\rightarrow k}$ must be independent of the state $x_{0[k]}$ (i.e., $S_{c_{\rightarrow k}} = 0$ in the cost).

**Theorem 1:** The input perturbation sequence $c_{\rightarrow k}$ in normal operation from the MPC additional layer has no impact on the original closed-loop dynamics if $S_{c_{\rightarrow k}} = 0$. This can be
true only if the cost function in Algorithm 1 embeds some knowledge of the nominal output-feedback control law (10) such that the weights $Q$, $R$, $N$ and $S_\tau$ satisfy the following conditions:

\[
\begin{align*}
\Phi^T S_\tau \Phi - S_\tau + Q + K^T R K &= 0, \\
B^T S_\tau \Phi + RK + N^T &= 0.
\end{align*}
\]

Proof: This is straightforward to demonstrate by investigating the cost function (17) and the Lyapunov equation $\dot{\Psi}^T S \dot{\Psi} = S - W$.

Corollary 1: This theorem is significant because it demonstrates that the extra MPC layer will not impact on the underlying robust closed-loop properties unless constraints are predicted to be active. Consequently, in normal operation, the properties of the underlying robust law are retained.

Nevertheless, a key point in the observation above is that the control horizon $n_c$ is much smaller than the preview horizon, for the reason that the MPC controller looks far enough ahead to allow beneficial feed-forward compensation; it was found that $n_a = 15$ samples was a reasonable choice in this simulation setting. The operating frequency of the MPC controller was 5 Hz which gives a good compromise between performance and computational burden; hence the preview horizon is 3 seconds ahead. It is clear that a similar idea also holds true for the control horizon $n_c$. The control horizon must be at least as large as the preview horizon, for the reason that the MPC controller can then plan effective control sequences to compensate for the wind disturbances.

C. Simulation results

The closed-loop simulation was performed under a turbulent wind field characterised by the mean speed of 13 ms$^{-1}$ and turbulence intensity of 14%. Three controllers were investigated: (i) the baseline robust feedback controller based on the control law (10) denoted as (FB); (ii) (FB/FF) represents the unconstrained additional layer on top of the baseline feedback compensator where the unconstrained input perturbation (21) is simply added to the feedback control law and (iii) the constraint-aware additional layer augmented with the embedded baseline feedback controller, where the input perturbation is computed on-line by solving Algorithm 1, denoted as (FB/MPC).

Figure 3 shows the sample time history excerpted from a 20-minute simulation result. Figure 3(a) illustrates the time history for the pitch angle of blade 1 where the controllers reached the pitch angle constraints and behaved differently. Consequently, in Figure 3(b), the rotor speed deviation for FB/MPC was slightly better than FB/FF. More importantly, Figure 3(c) shows significant reductions in flap-wise blade bending moment achieved by FB/MPC compared to FB/FF. The results from the full 20 minute simulation are summarised in Table I. As shown in Table I, it is not surprising that FB/FF and FB/MPC achieved lower standard deviations on rotor speed and blade load reconstructions compared to FB since they used of approaching wind measurements. Furthermore, the results showed that the constraint-aware controller FB/MPC also outperformed FB/FF slightly. The difference is not significant because violations of pitch actuator constraints were infrequent. It is surmised that better improvement could be achieved by FB/MPC if soft-constraints on rotor speed and blade loads were also included.

V. Conclusion

This work has shown the MPC layer design on top of a given output-feedback blade-pitch controller where the layer handles the upstream wind measurements and constraints. The conditions for separating the original closed-loop dynamics from the additional control design were also proposed in this paper. Such MPC layer design retains the robustness properties of the given feedback controller unless constraint violations are expected. Closed-loop simulations on a high-fidelity turbine were performed, showing the benefits gained
Fig. 3. Simulation results upon the NREL 5MW turbine, showing the performance of the various controllers studied in this paper.

by the proposed MPC-based preview controller. Future work will include constraints on rotor speed and blade loads.

**APPENDIX I**

The model parameters for (7) are shown in Table II and the closed-loop robust controllers are described as follows:

\[
K_{\theta_w}(s) = \frac{10.74s^2 + 3.845}{3.142s} \\
K_{\theta_M}(s) = 10^4 \times \frac{2.3s^4 + 6.1s^3 + 25.4s^2 + 18.1s + 39}{(s^3 + 0.20s^2 + 8.00s + 0.46 + 10.38)}
\]

**REFERENCES**


